

# Hybrid Hadronization of Jet Showers from $e^+e^-$ to $AA$ with JETSCAPE

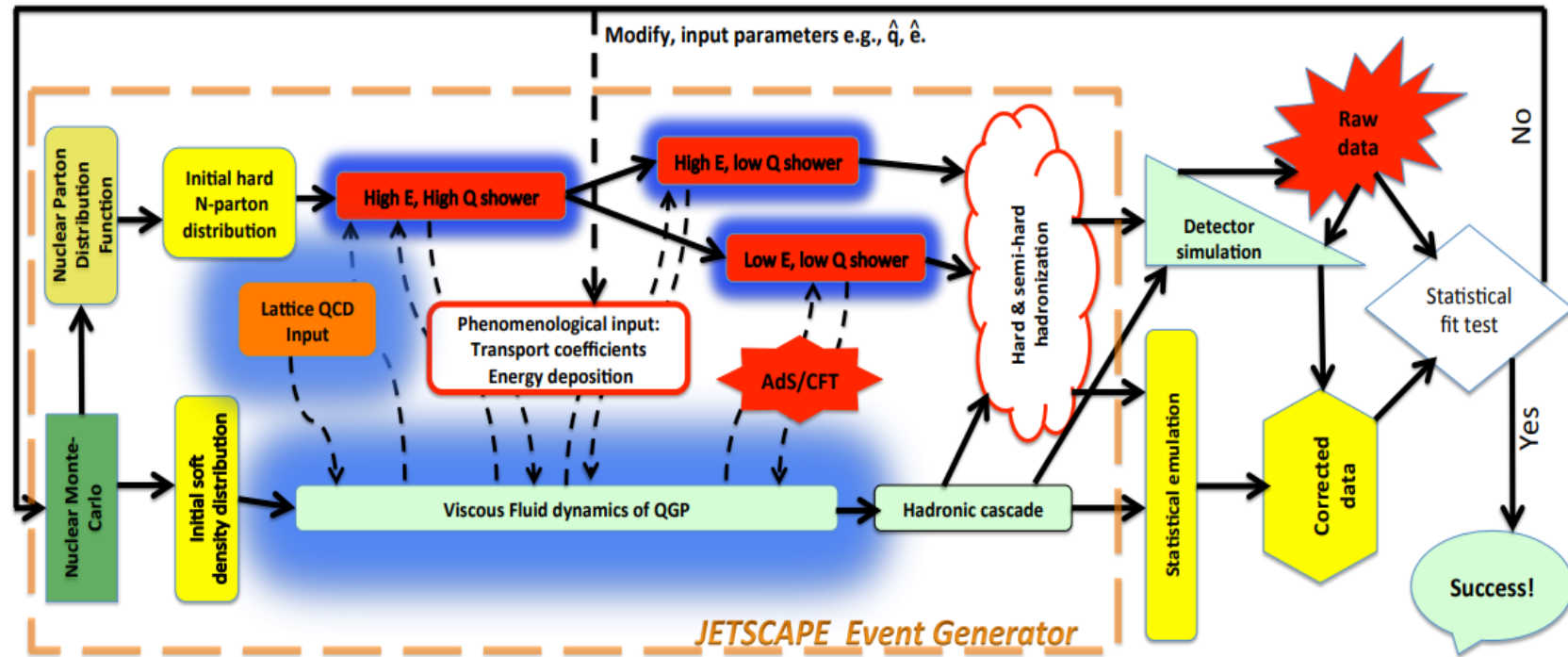
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CAMERON PARKER, TEXAS A&M  
UNIVERSITY, ON BEHALF OF THE  
JETSCAPE COLLABORATION: 30/3/2023

# JETSCAPE Framework<sup>1,2,3</sup>

Many modules for soft and hard physics. We use 3 modules that deal with jets in quark-gluon plasma (QGP):

1. MATTER – propagates and splits an initial jet parton rapidly dropping its virtuality until it falls below a threshold  $Q_0$
2. LBT – propagates low-virtuality and real partons through the medium (QGP)
3. Hybrid Hadronization – hadronizes partons through recombination and string fragmentation



**“A modular, task-based framework for simulating all aspects of heavy-ion collisions”**

<sup>1</sup> J.H. Putschke et. al., arXiv:1903.07706

<sup>2</sup> A. Kumar et. al., Phys. Rev. C 102, 054906 (2020)

<sup>3</sup> A. Kumar et. al., arXiv:2204.01163

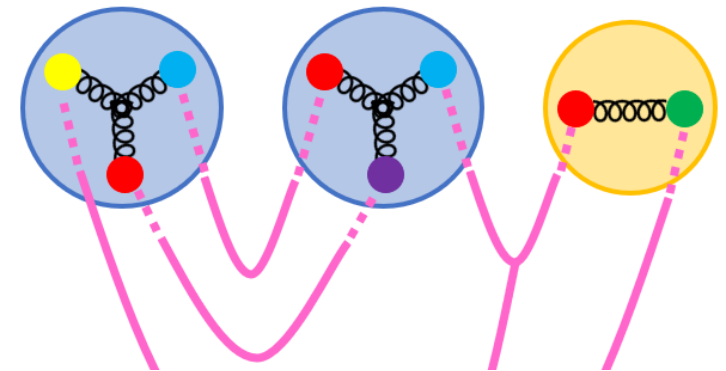
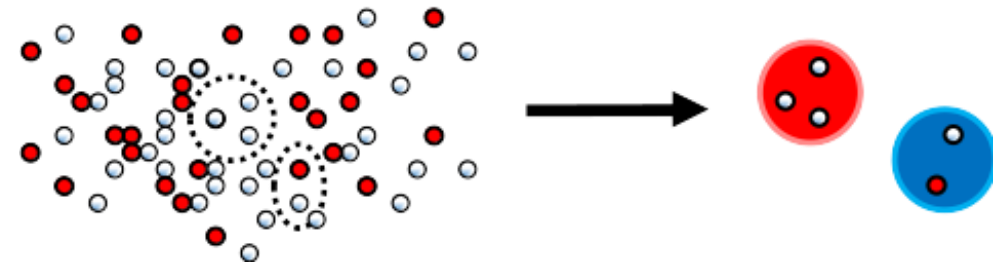
# Hybrid Hadronization<sup>4</sup>

Hadronization of partons cannot be described from first principles.

Phenomenological models can be tuned to fit experimental data.

**Hybrid Hadronization (HH)** combines two of these models:

1. **Quark recombination** (high-density systems)
  - Quarks can directly recombine into hadrons
2. **Lund string fragmentation** (low-density systems)
  - Color flux tubes in QCD vacuum at large distances → string-like behavior.
  - Quarks connected with strings; gluons are part of these strings – these strings are then broken to form hadrons.



<sup>4</sup> K.C. Han et. al., Phys. Rev. C **93** (2016) 4, 045207

# Rationale

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JETSCAPE is the ideal framework to test Hybrid Hadronization with and without a medium

Want to see how Hybrid Hadronization does in vacuum when fragmentation alone does a good job

QGP as the medium of interest, probed with jets

# Vacuum Systems

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# Tuning Parameters

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Hybrid	MATTER	<b>Virtuality factor (0.1-1):</b> determines starting virtuality for every shower initiating parton as a portion of its initial momentum
		<b><math>Q_0</math> (0.9-3 GeV):</b> Virtuality threshold for when perturbative QCD stops
		<b><math>\lambda_{QCD}</math> (0.1-0.4 GeV):</b> strength of QCD interactions in MATTER
	Hadronization	<b>Hadron scales (0.5-2):</b> factor multiplying the measured wavefunction widths
		<b>Strange to up-down ratio (0.2-0.5):</b> rate strange quarks are produced compared to 1 <sup>st</sup> generation quarks in string fragmentation
		<b>Diquark to quark ratio (0.07-0.2):</b> rate diquarks are produced compared to single quarks in string fragmentation

# Collision Systems

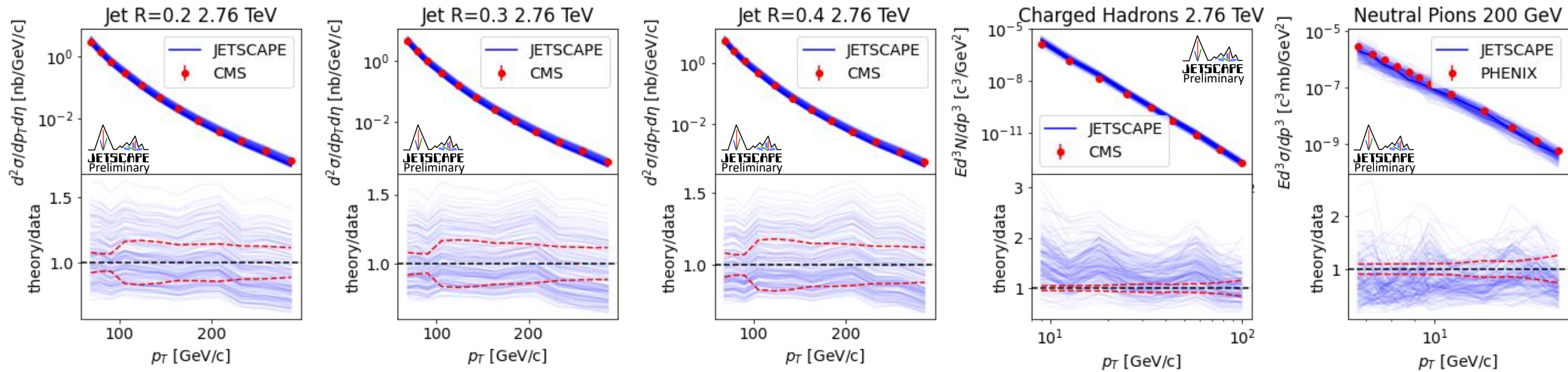
## Data sets:

- CMS charged hadron spectra and jets at 2.76 TeV ( $pp$ )
- PHENIX neutral pion spectra at 200 GeV ( $pp$ )
- ALEPH unidentified and identified hadron spectra at 91.2 GeV ( $e^+e^-$ )

Sample parameter space with Latin Hypercube to maximize coverage for Bayesian tuning

						<b>X</b>	
			<b>X</b>				
	<b>X</b>						
				<b>X</b>			
							<b>X</b>
<b>X</b>							
					<b>X</b>		
		<b>X</b>					

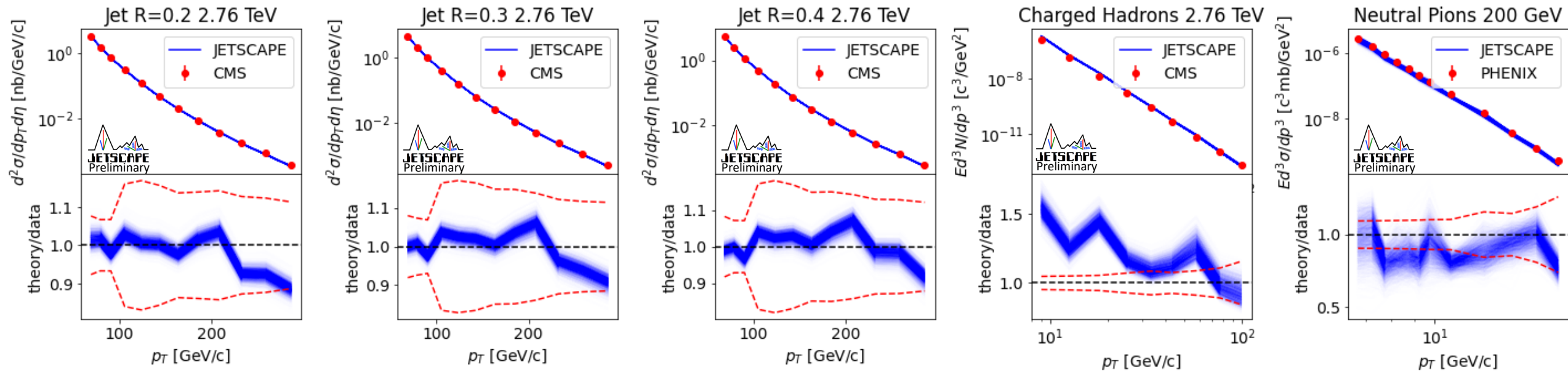
# Priors



CMS: <https://doi.org/10.17182/hepdata.77601>  
PHENIX: <https://doi.org/10.48550/arXiv.0704.3599>



# Posteriors

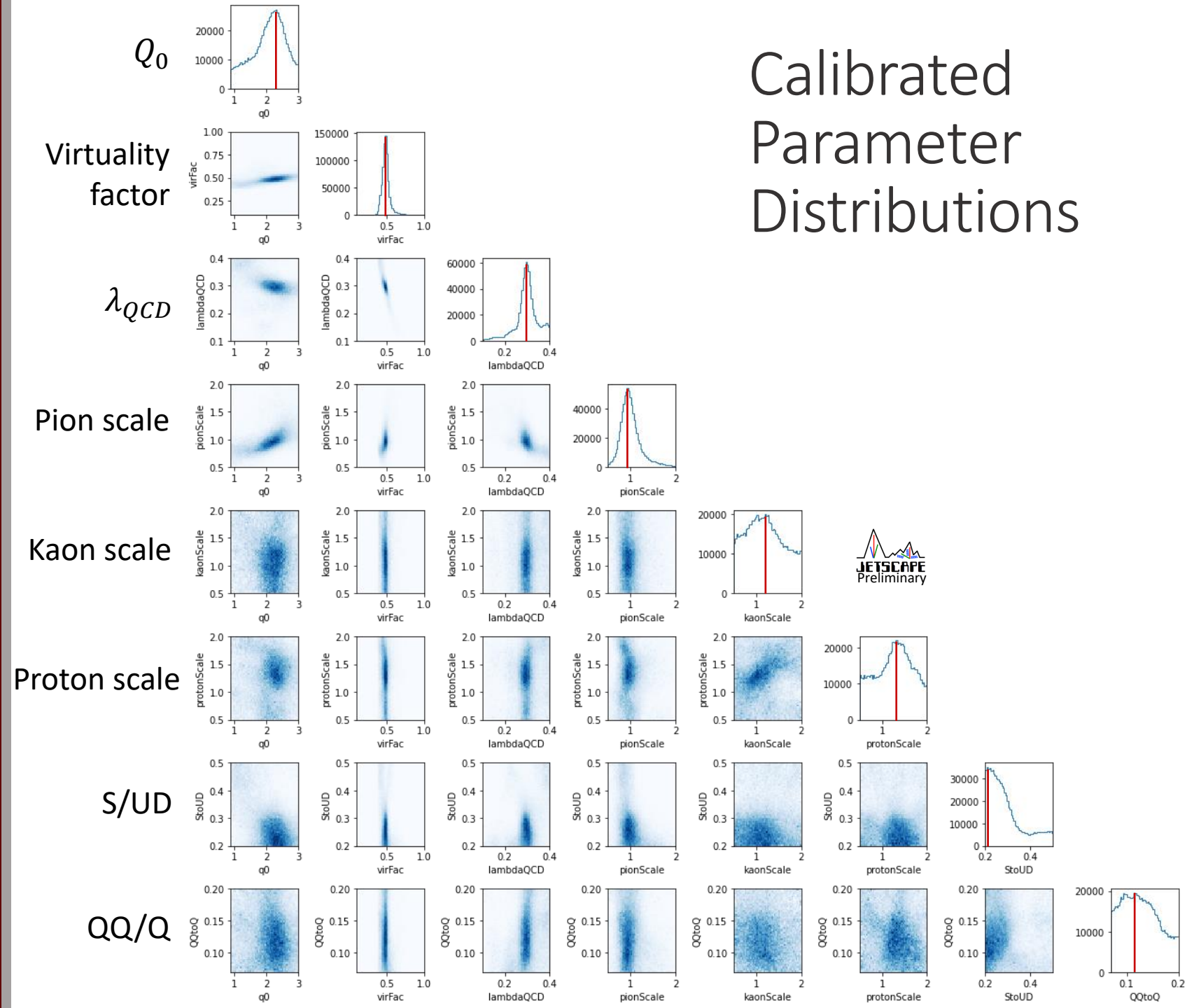


CMS: <https://doi.org/10.17182/hepdata.77601>  
PHENIX: <https://doi.org/10.48550/arXiv.0704.3599>

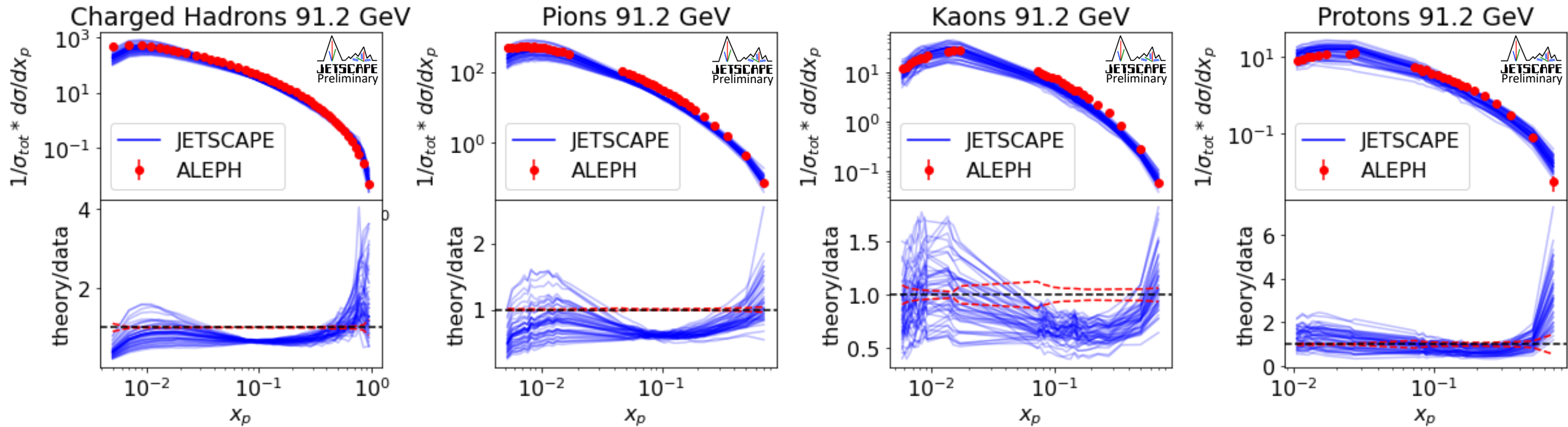
# Calibrated Parameter Maximums

- $Q_0$ : 2.29
- Virtuality factor: 0.478
- $\lambda_{QCD}$ : 0.292
- Pion scale: 0.92
- Kaon scale: 1.19
- Proton scale: 1.31
- Strange to up-down: 0.206
- Diquark to quark: 0.114

# Calibrated Parameter Distributions



# $e^+e^-$ at 91.2 GeV Hadron Observables



ALEPH: <https://doi.org/10.17182/hepdata.47582>

# Medium Effects

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# In-Medium Setup

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Simulate jets of set energy  $E$  in QGP medium of size  $L$

X direction in direction of jet (longitudinal)

Y-Z in plane perpendicular to jet (transverse)

Parton flow can be switched on and off independently during propagation and hadronization

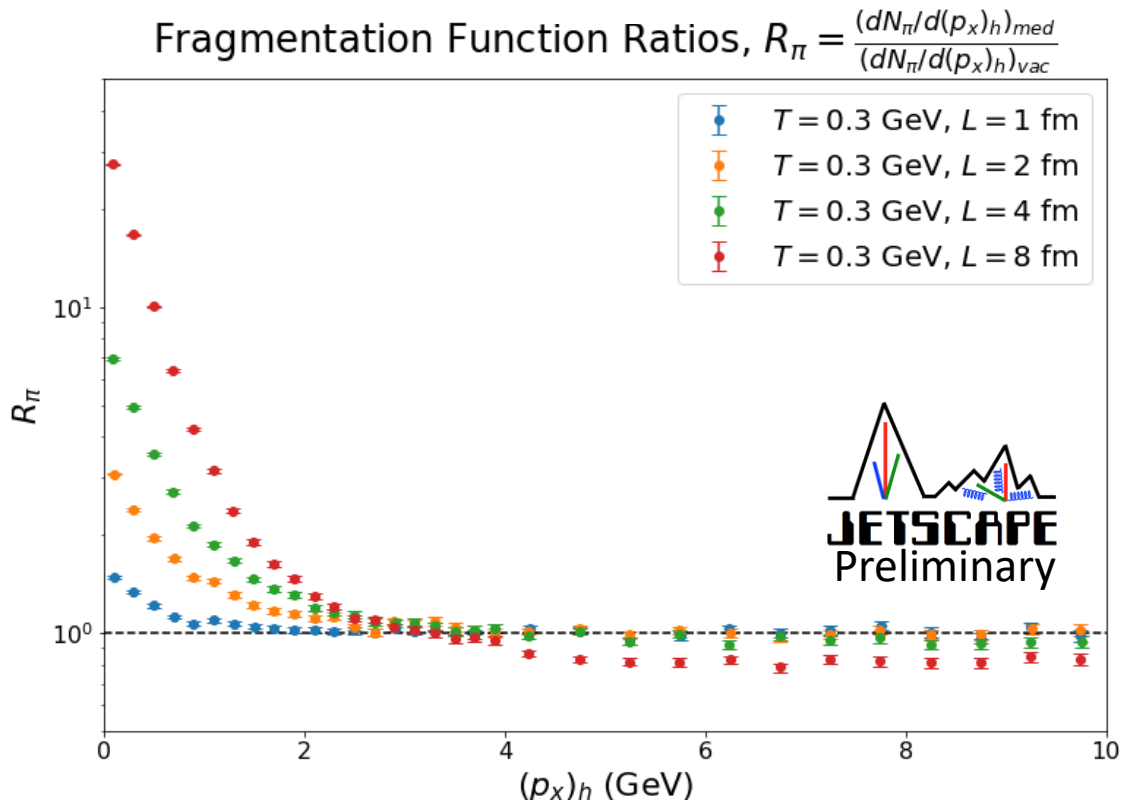
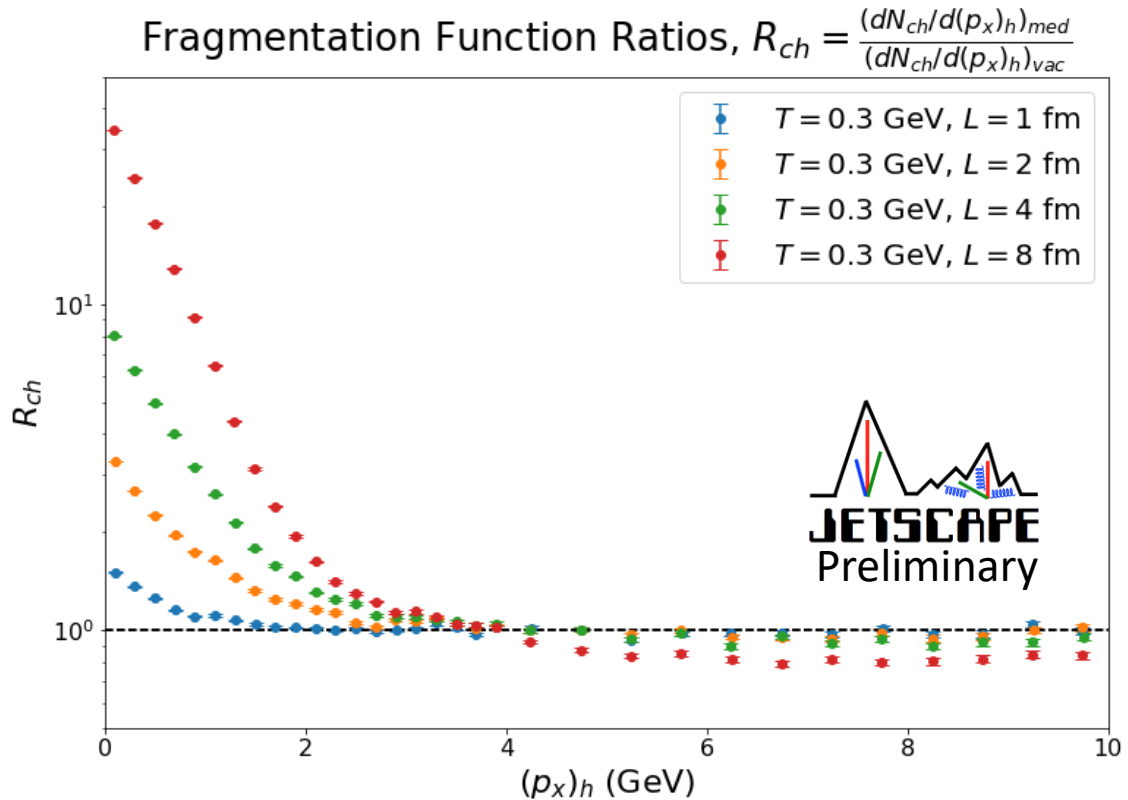
# Fragmentation Function Ratios (no flow)

Up quark jet,  $E = 100$  GeV in medium vs. in vacuum

Soft shower debris + thermal pickup, growing with medium size

$$R_{AA} = \frac{[dN_{[ ]}/dp_x]_{medium}}{[dN_{[ ]}/dp_x]_{vacuum}}$$

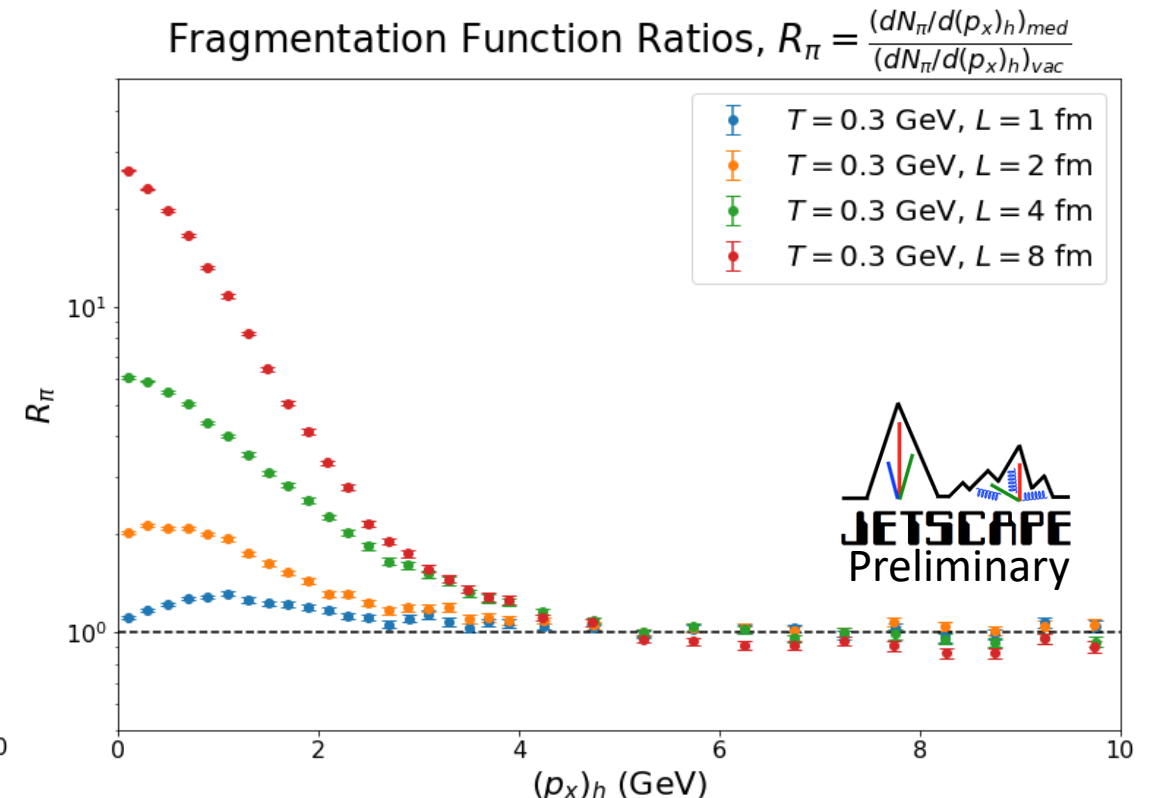
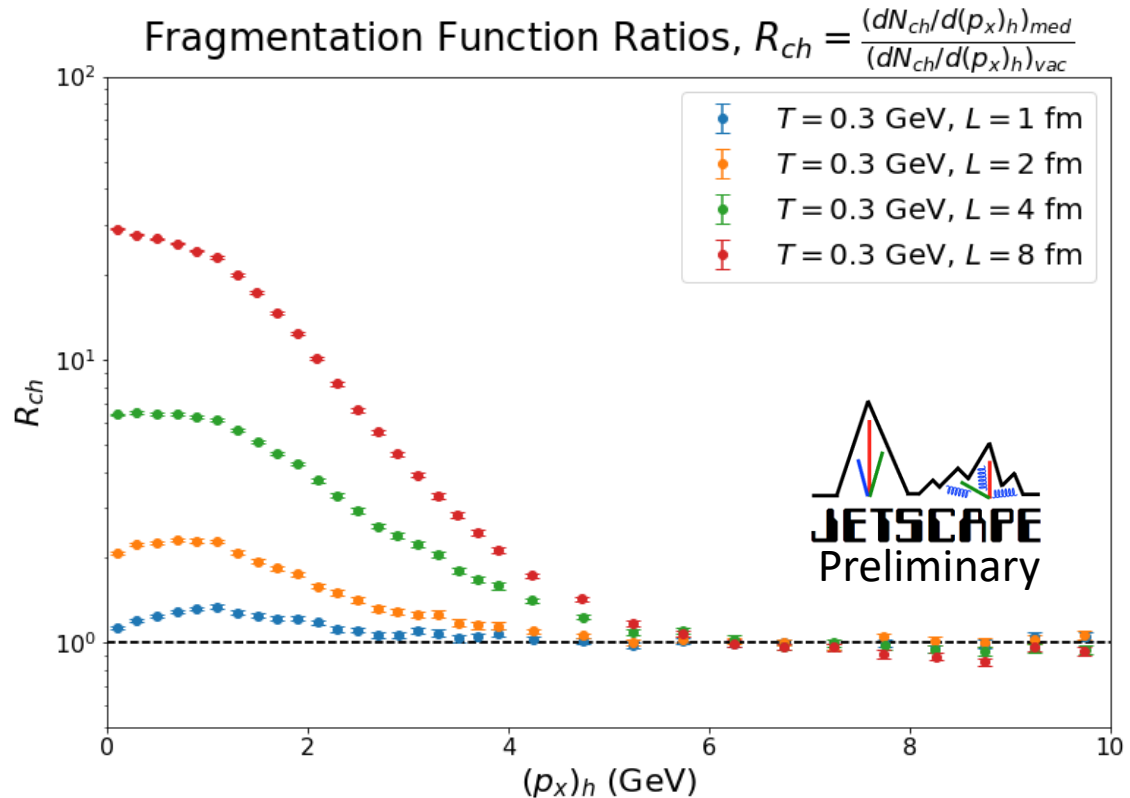
$E_{jet} = 100$  GeV, No Flow



# Fragmentation Function Ratios (with flow)

Longitudinal flow at hadronization ( $v_x^{HH} = 0.8c$ ) shifts the enhancement of soft partons to larger momenta, raises peak

$E_{jet} = 100$  GeV, Flow = (0.8, 0, 0)

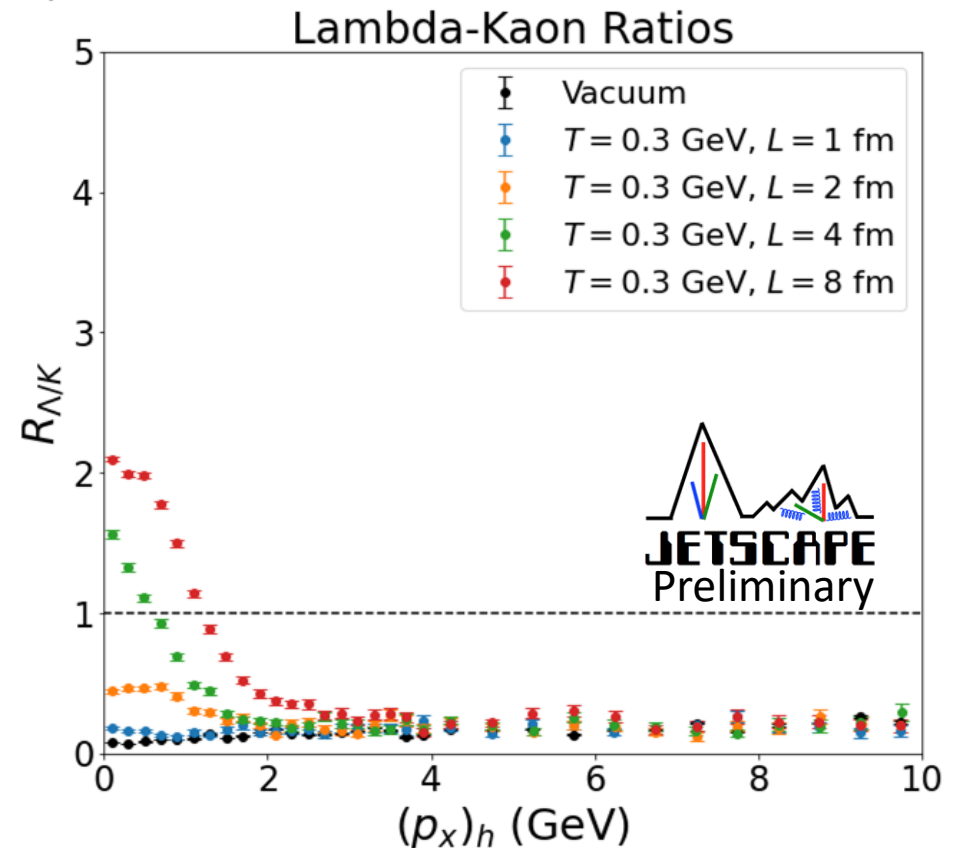
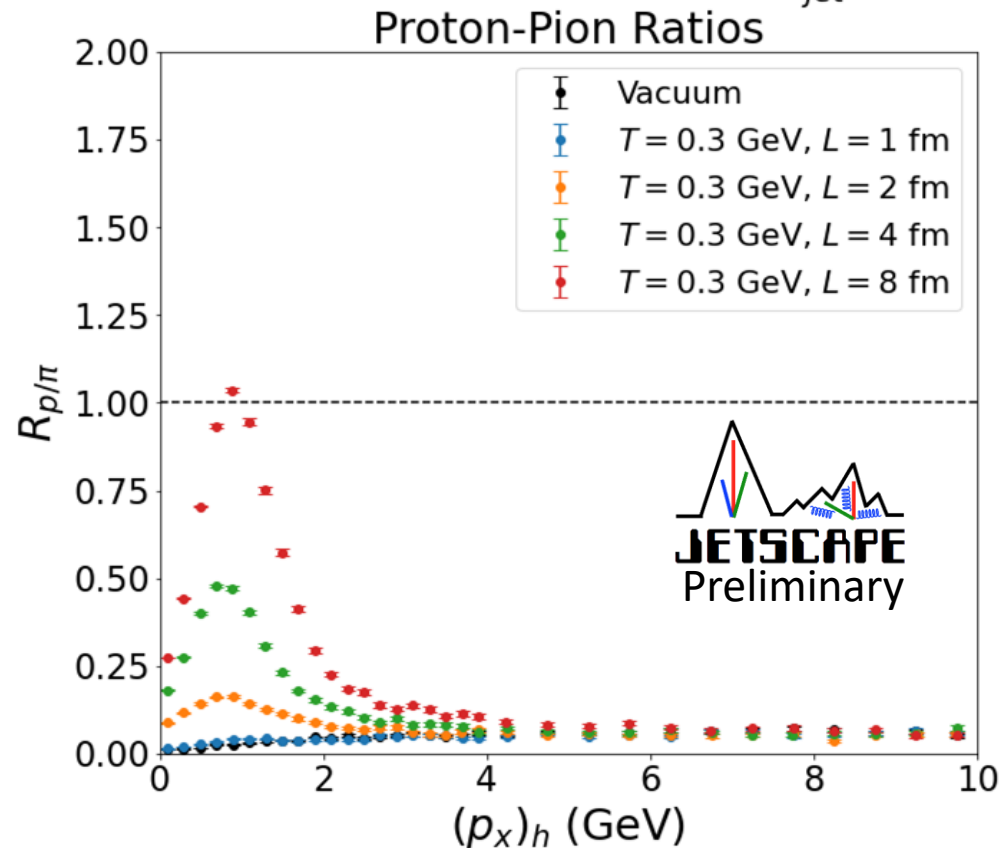


# Baryon/Meson Enhancement (no flow)

Up quark jet,  $E = 100$  GeV, baryons/mesons for different mediums

Baryon/meson enhancement below 10 GeV increases as the medium gets larger, as we expect

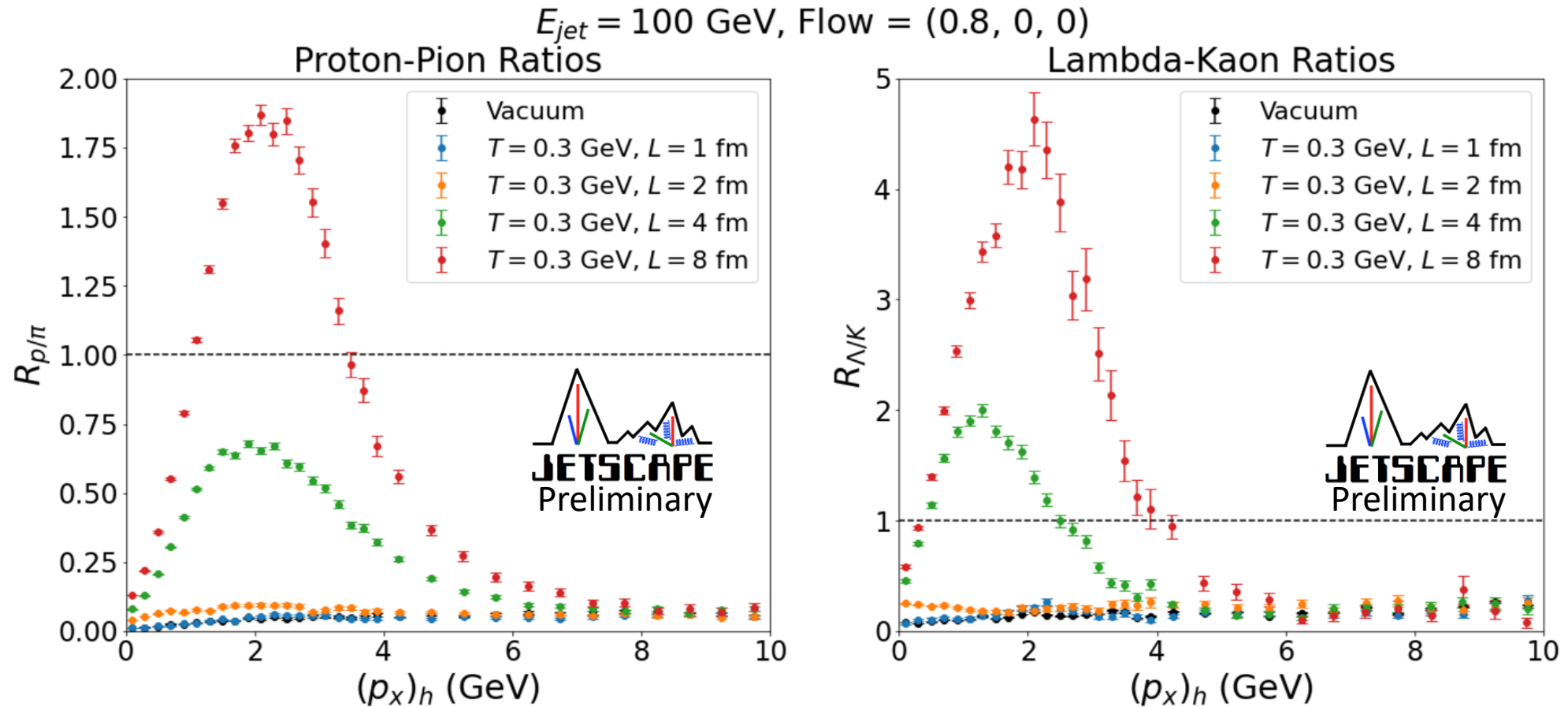
$E_{jet} = 100$  GeV, No Flow





# Baryon/Meson Enhancement (with flow)

Longitudinal flow at hadronization ( $v_x^{HH} = 0.8c$ ) **enhances** the B/M signal tremendously and **shifts** it to larger momenta.



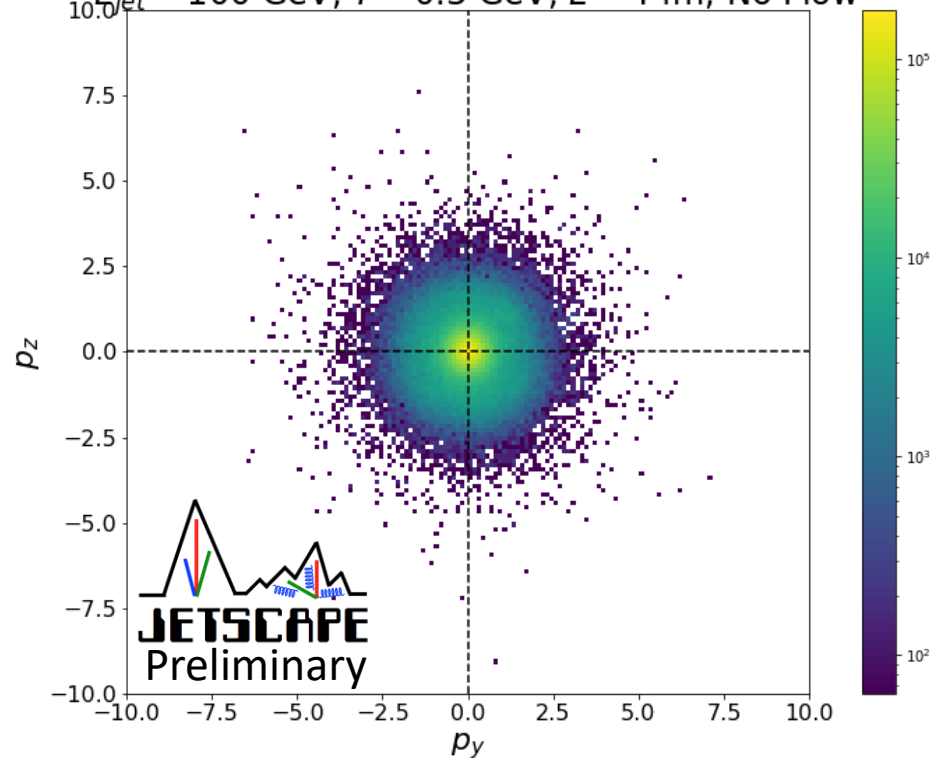
# Transverse Flow Effects

Up quark jet,  $E = 100$  GeV,  $L = 4$  fm, liquefier on, soft hadrons transverse momentum shown

**Soft** jet partons are likely to recombine with thermal partons during hadronization  
→ Transverse flow at hadronization ( $v_y^{HH} = 0.8c$ ) induces flow for soft jet hadrons.

$d^2N / (dp_y dp_z)$  of Soft (2-10 GeV) Hadrons, Liquefied

$E_{jet} = 100$  GeV,  $T = 0.3$  GeV,  $L = 4$  fm, No Flow

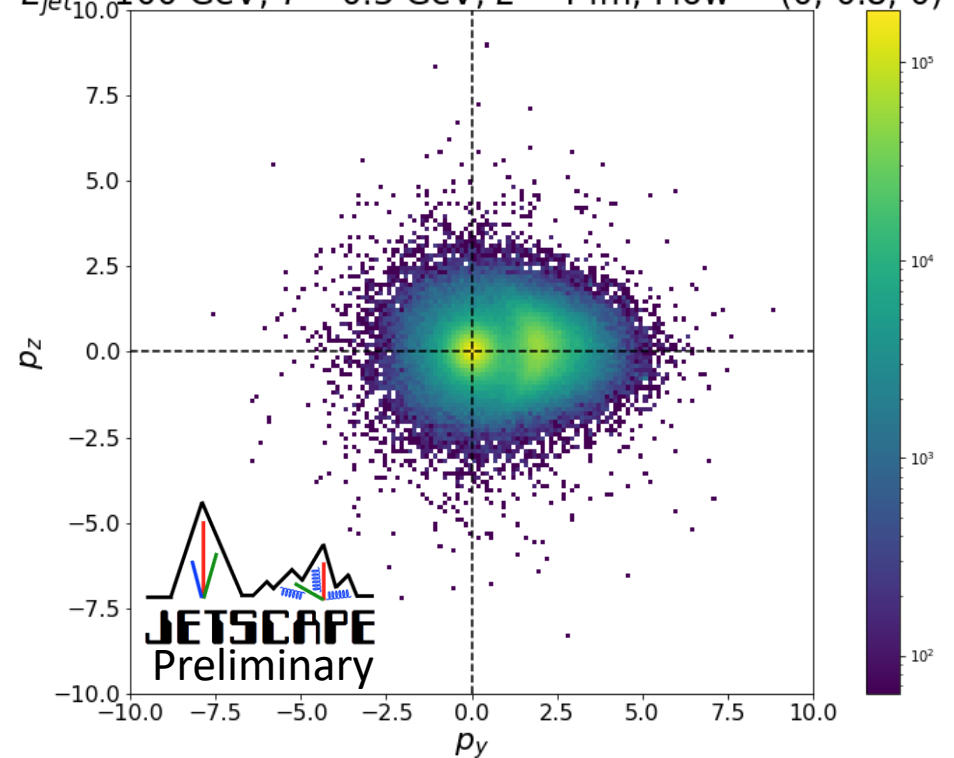


$v_{med} = 0.8c\hat{y}$



$d^2N / (dp_y dp_z)$  of Soft (2-10 GeV) Hadrons, Liquefied

$E_{jet} = 100$  GeV,  $T = 0.3$  GeV,  $L = 4$  fm, Flow = (0, 0.8, 0)

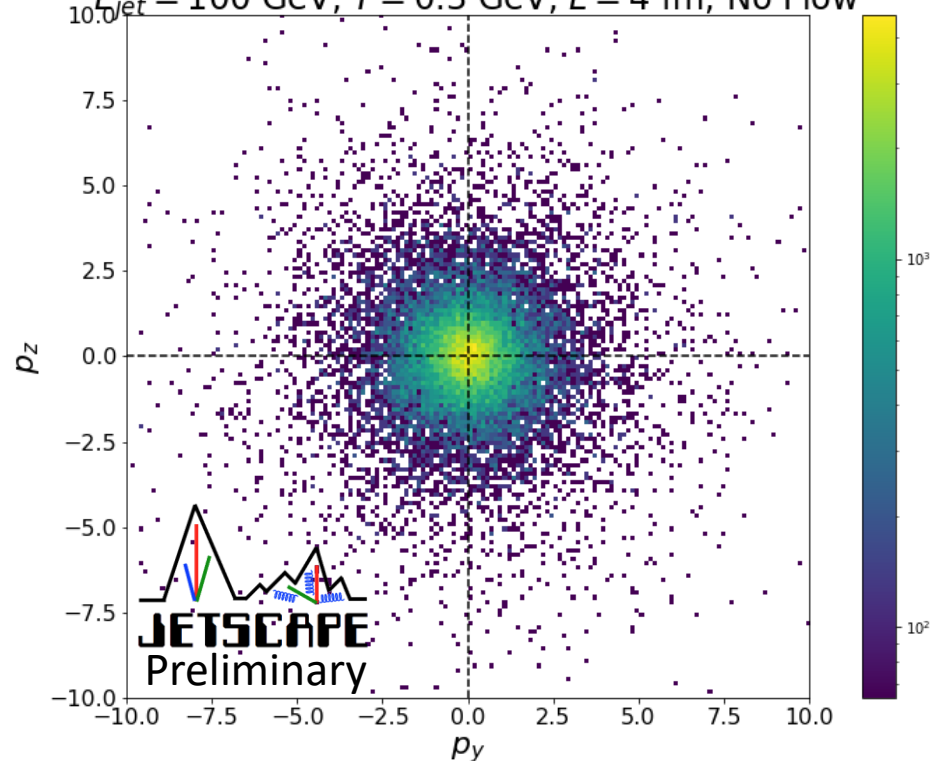


# Transverse Flow Effects

Leading hadrons only

**Hard** jet partons are unlikely to recombine with thermal partons, and don't pick up the flow.

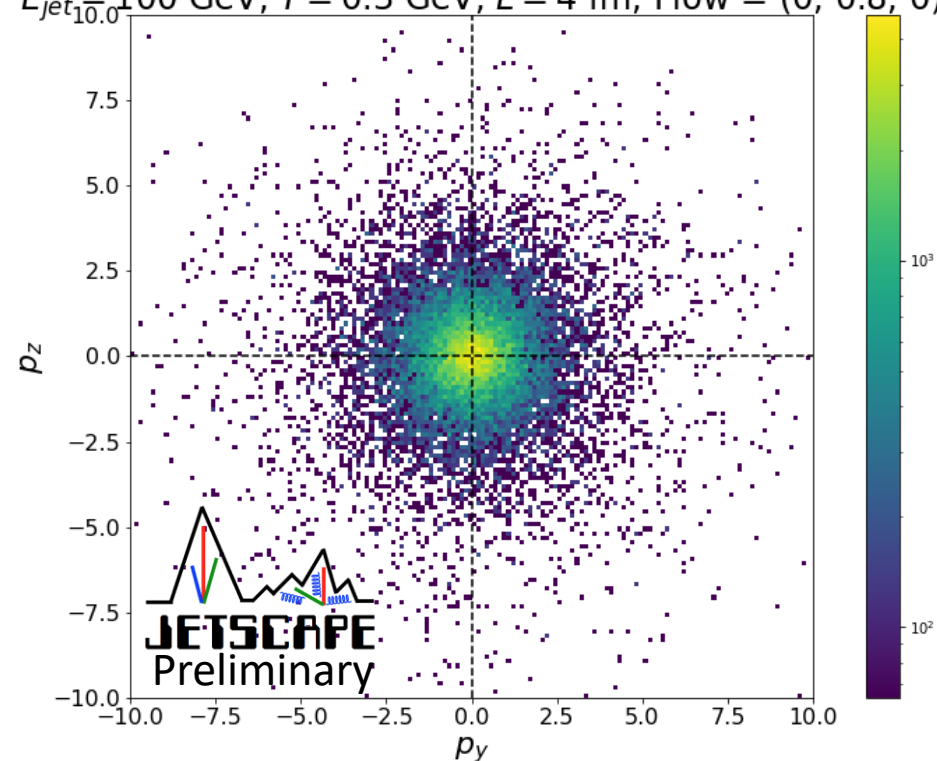
$d^2N / (dp_y dp_z)$  of Most Energetic Hadron, Liquefied  
 $E_{jet} = 100$  GeV,  $T = 0.3$  GeV,  $L = 4$  fm, No Flow



$$v_{med} = 0.8c\hat{y}$$



$d^2N / (dp_y dp_z)$  of Most Energetic Hadron, Liquefied  
 $E_{jet} = 100$  GeV,  $T = 0.3$  GeV,  $L = 4$  fm, Flow = (0, 0.8, 0)



# Takeaways

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Successfully describe jets and high  $p_T$  hadrons

Can reproduce signature recombination effects, like baryon/meson enhancement

Jet hadrons can pick up significant flow from a flowing medium

# Outlook

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Expansion to identified hadrons electron-positron systems in progress

- Extending analysis to soft hadrons in  $pp$

Challenge in getting enough protons

Comparing different PYTHIA tunes

Heavy quark jet analysis

- Charm jets

# Thanks to:

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The JETSCAPE collaboration and the NSF for funding this project

The Texas A&M University HPRC center for providing the computational resources

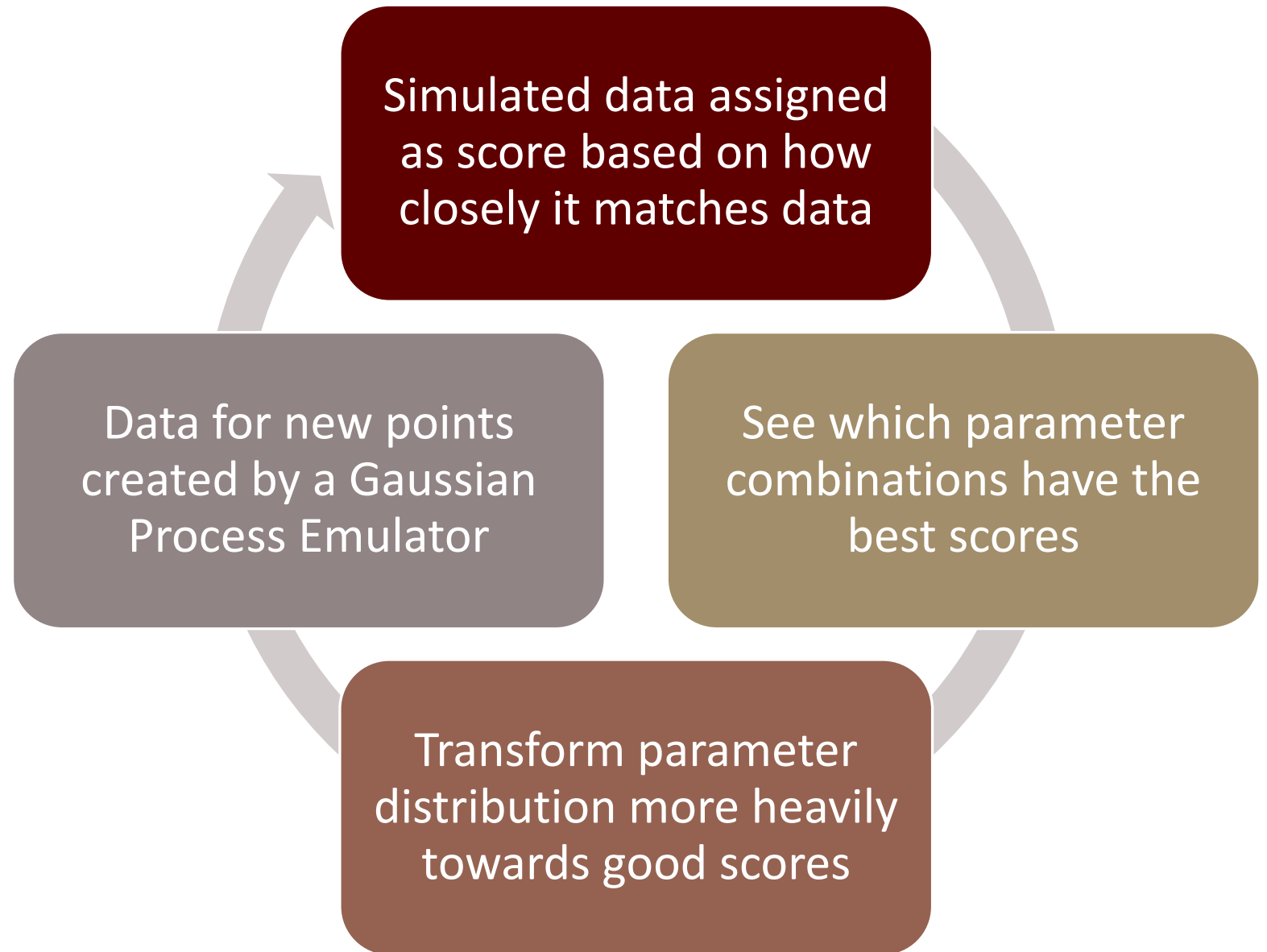


# Bayesian Tuning Methods

Iterative method of  
multi-parameter tuning

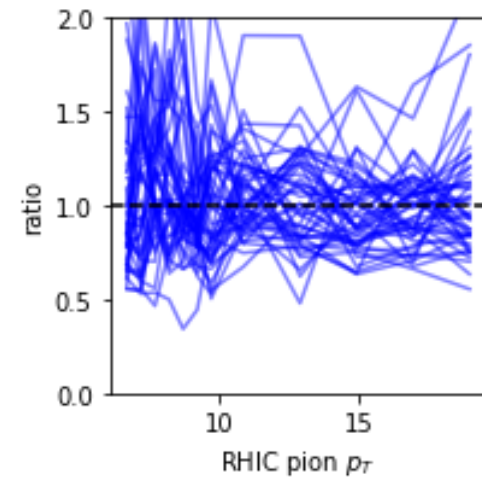
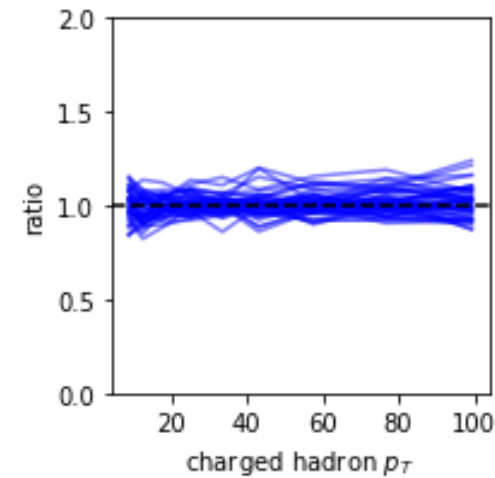
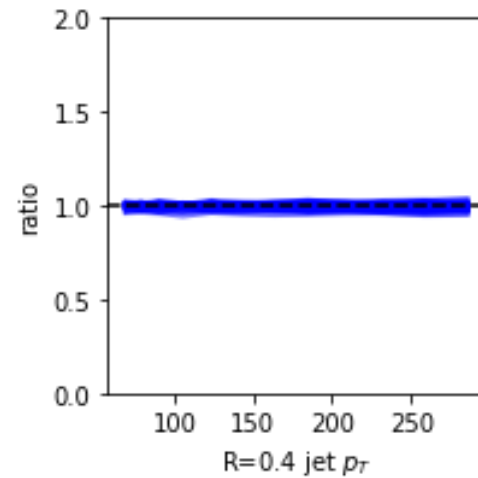
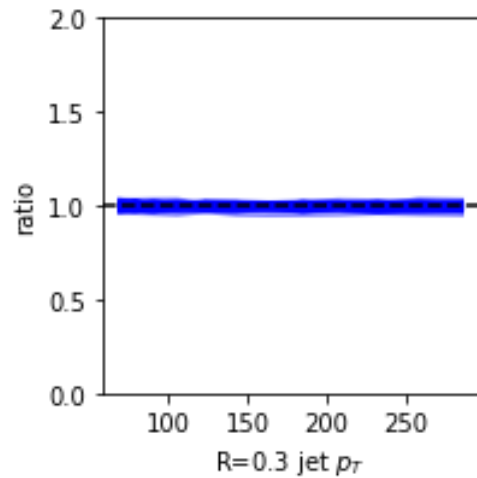
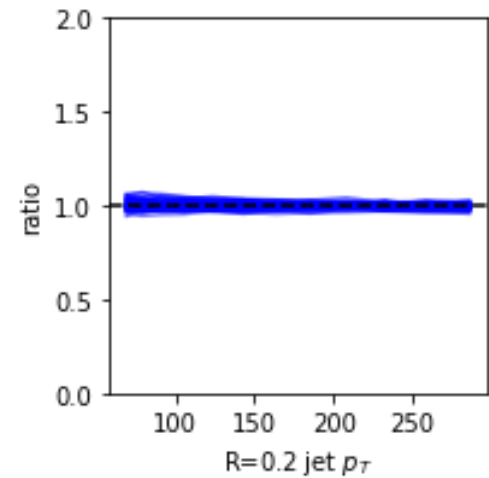
Scores assigned with  
Bayesian inference

Each cycle is a step  
performed for each  
walker



# Emulator Validation

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# HH Study Parameter Space

	Parameter	Range
<b><u>Jet Properties</u></b>	Flavor	Up (light), Charm & Bottom (heavy)
	Energy, $E$	5 - 100 GeV (x-direction)
<b><u>QGP Brick Properties</u></b>	Temperature, $T$	0.2 - 0.3 GeV (hadronization at 0.165 GeV)
	Size, $L$	0 - 8 fm
	Hadronization flow velocity, $\mathbf{v}^{HH}$	0 - 0.8c $\hat{\mathbf{x}}$ (longitudinal), 0 - 0.8c $\hat{\mathbf{y}}$ (transverse)
	Medium flow velocity, $\mathbf{v}^{Eloss}$	0 - 0.8c $\hat{\mathbf{x}}$ (longitudinal), 0 - 0.8c $\hat{\mathbf{y}}$ (transverse)
	Liquefier	On/off (cutoff at $E < 3.2 T$ )
<b><u>Jet Clustering</u></b>	Jet radius, $R$	0.1 - 1.2

# JETSCAPE<sup>1,2,3</sup> Setup for HH Studies

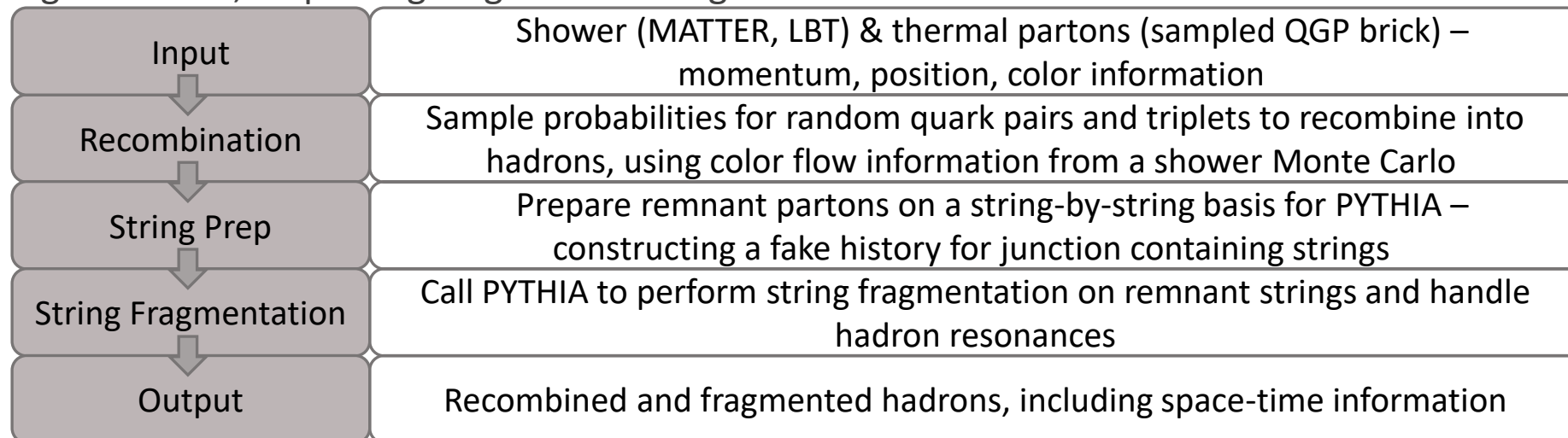
<sup>1</sup>J.H. Putschke et. al., arXiv:1903.07706, <sup>2</sup>A. Kumar et. al., Phys. Rev. C **102**, 054906 (2020), <sup>3</sup>A. Kumar et. al., arXiv:2204.01163

Run 3 modules in a QGP brick medium:

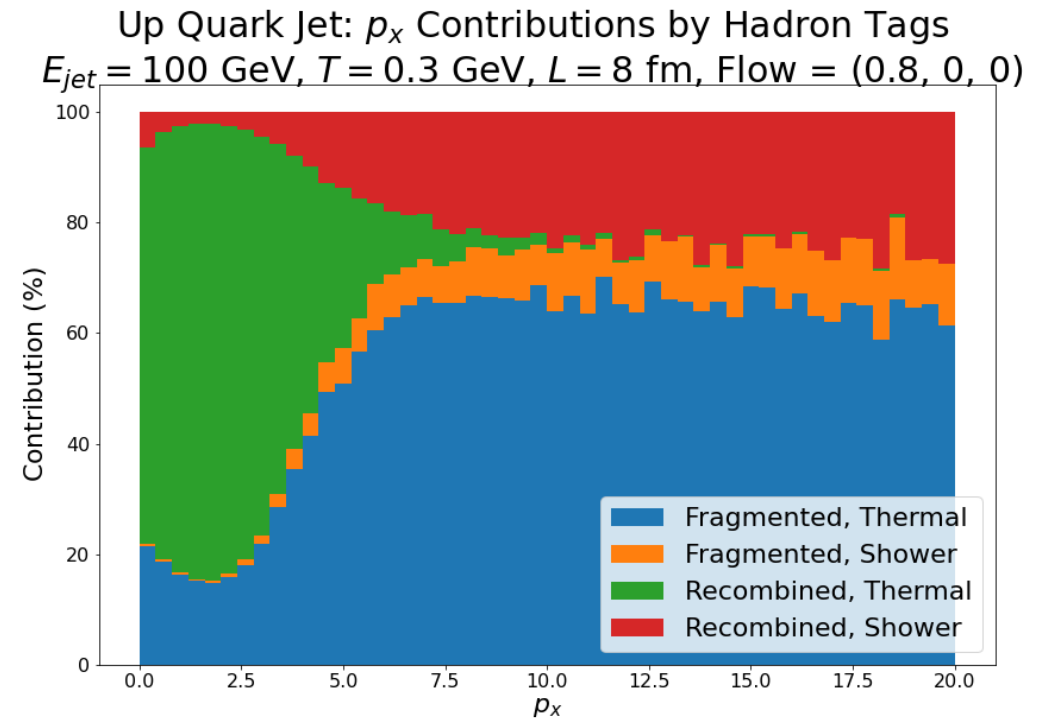
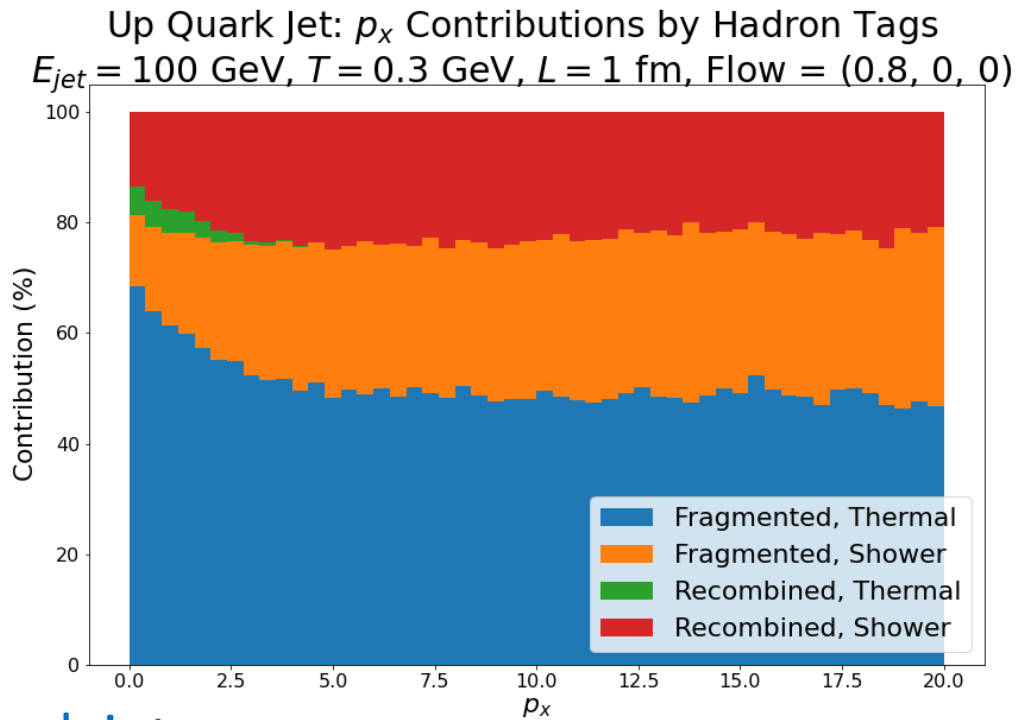
1. **MATTER** – propagates and splits an initial jet parton (in the **x-direction**), rapidly dropping its virtuality until it falls below a threshold  $Q_0$  ( $= 1.2$  GeV)
2. **LBT** – propagates low-virtuality and real partons through the QGP
3. **Hybrid Hadronization** – hadronizes partons through recombination and string fragmentation, respecting all given color tags:

PYTHIA decays  
switched ON

$c\tau = 10$  mm



# Contribution of Different Channels to Total Hadron Production



Up quark jet

Shower-thermal recombination increases drastically with medium size at low and intermediate momenta

# Transverse Jet Profile

Up quark jet,  $E = 100$  GeV,  $L = 1,4$  fm.

Jet axis determined by taking the most energetic pseudojet, using the anti- $k_T$  algorithm with  $R = 0.6$ .

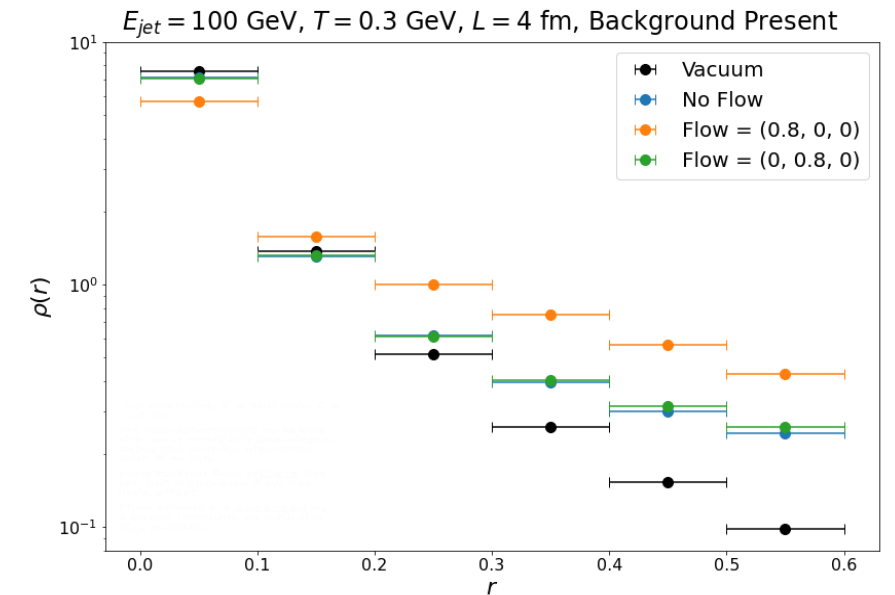
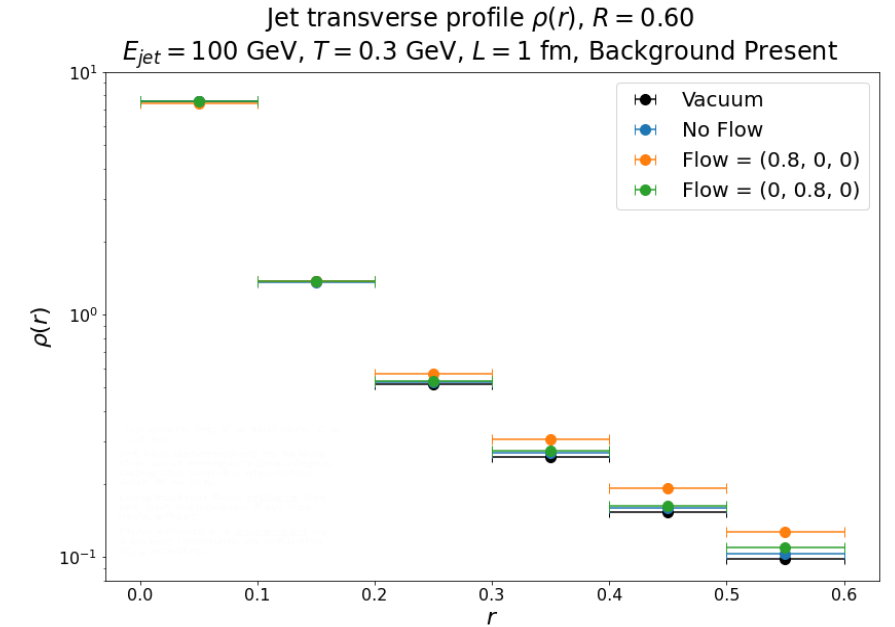
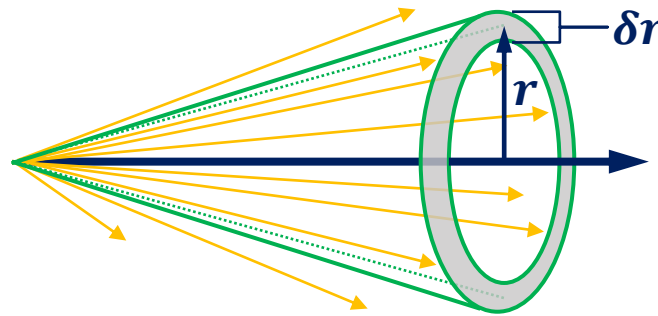
Longitudinal flow widens the jet, but transverse flow has little effect.

Flow effects are enhanced by a larger medium, as with the  $R_{AA}$  spectra.

## Up quark jet

Jet transverse profile defined as:

$$\rho(r) = \frac{1}{N^{jet}} \sum_{jets} \left[ \frac{1}{\delta r} \frac{\sum_{i \in (r \pm \delta r/2)} p_T^i}{\sum_{i \in (0, R)} p_T^i} \right]$$



# Collision Systems

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PythiaGun > Matter > Hybrid Hadronization > Pythia

- CMS charged hadron spectra at 2.76 TeV ( $pp$ )
  - 50  $\hat{p}_T$  bins
- PHENIX neutral pion spectra at 200 GeV ( $pp$ )
  - 22  $\hat{p}_T$  bins

epemGun > Matter > Hybrid Hadronization > Pythia

- ALEPH charged hadron spectra at 91.2 GeV ( $e^+e^-$ )

Run each for every design point

146 design points, 48 validation points, 48 exploratory runs

# Other Parameters

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Recombination excited states allowed: 1

Energy loss max time = 200 fm/c

- Set so that MATTER has enough time to step every parton down from its initial virtuality to  $Q_0$

Decay time: how long particles have to decay before being determined a final state hadron

- Changed to match detector specifications (usually in mm)
- Hybrid hadronization

Bayesian analysis code from JETSCAPE