

# Dijet azimuthal correlations in p-p and p-Pb collisions at forward LHC calorimeters



NCN



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Based on

arXiv:2210.06613

M. Abdullah Al-Mashad, A. van Hameren,

H. Kakkad, P. Kotko, K. Kutak, P. van Mechelen, S. Sapeta

# ITMD

ITMD = small x Improved Transverse Momentum Dependent factorization

- accounts for saturation
- correct gauge structure i.e. uses gauge links to define TMD's
- takes into account kinematical effects – the whole phase space is available at LO
- is implemented in MC event generator KaTie
- valid in region  $p_T > Q_s$ ,  $k_T$  can be any.  $p_T$  is hard final state momentum,  $k_T$  is imbalance

$$\frac{d\sigma^{pA \rightarrow \text{dijets} + X}}{d^2P_t d^2k_t dy_1 dy_2} = \frac{\alpha_s^2}{(x_1 x_2 s)^2} \sum_{a,c,d} \frac{x_1 f_{a/p}(x_1)}{1 + \delta_{cd}} \sum_{i=1}^2 K_{ag^* \rightarrow cd}^{(i)}(P_t, k_t) \Phi_{ag \rightarrow cd}^{(i)}(x_2, k_t)$$

(one of representations of the ITMD formula)

Generic structure: transverse momentum enters hard factors and gluon distributions  
gluon distribution depends on color flow

P. Kotko, K. Kutak, C. Marquet, E. Petreska, S. Sapeta, A. van Hameren, JHEP 1509 (2015) 106

P. Kotko, K. Kutak, C. Marquet, E. Petreska, S. Sapeta, A. van Hameren, JHEP 12 (2016) 034

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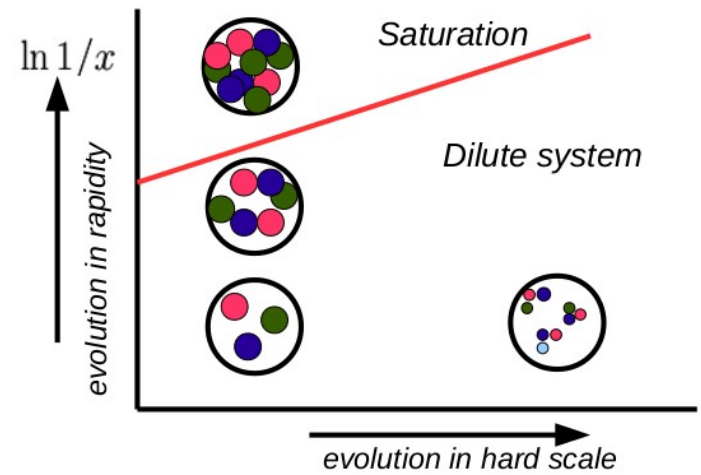
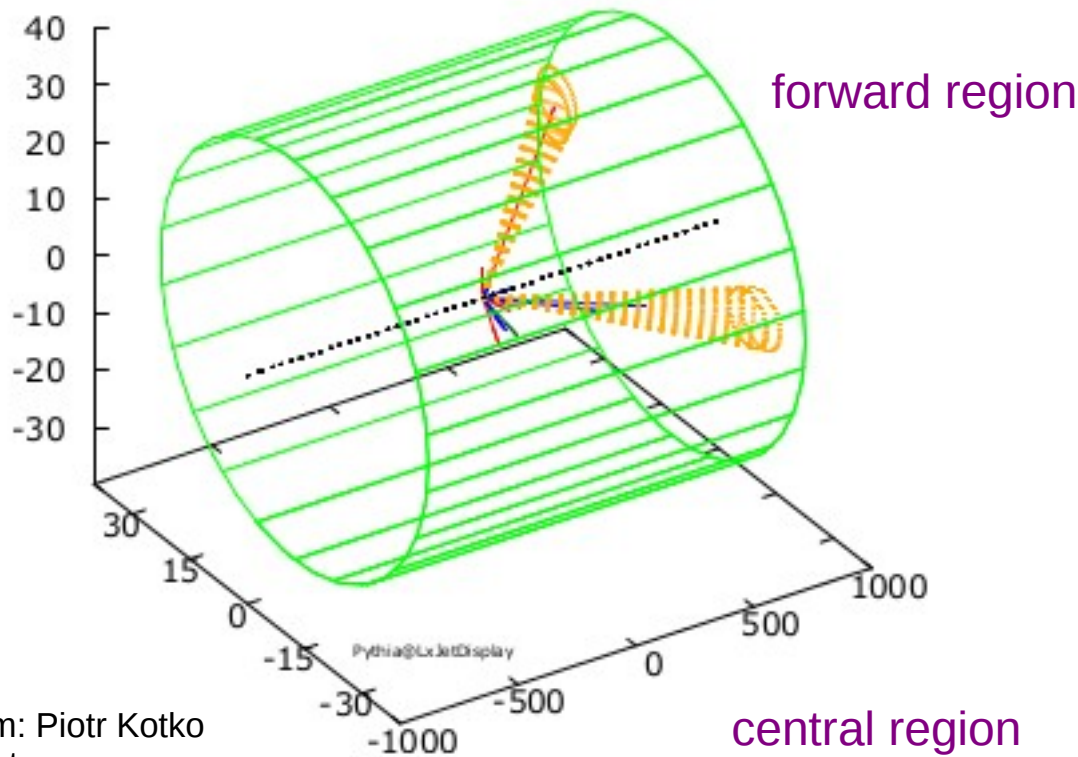
P. Kotko, K. Kutak, C. Marquet, E. Petreska, S. Sapeta, A. van Hameren  
JHEP 12 (2016) 034

See also:

T. Altinoluk, C. Marquet, P. Tael  
JHEP 06 (2021) 085

For developments for massive final states

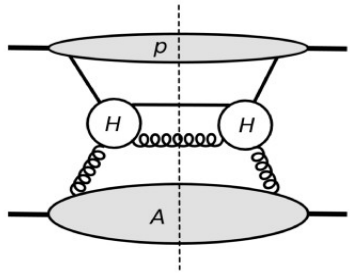
# $p - A$ (dilute-dense) forward-forward di-jets



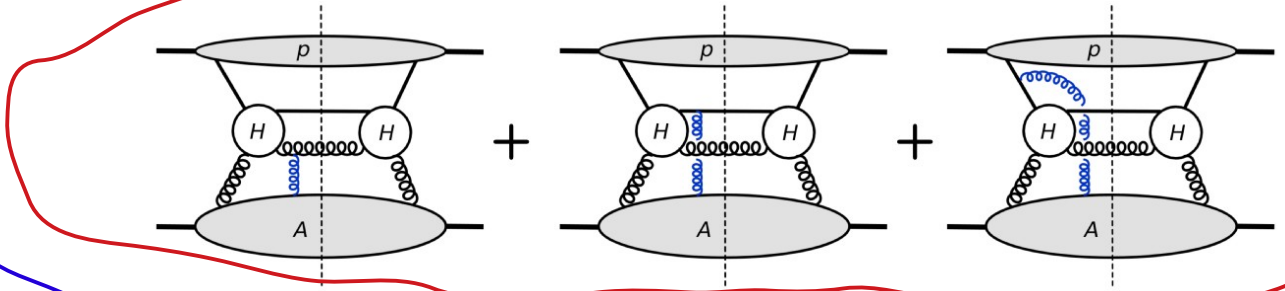
It originated from the aim to provide predictions for forward-forward jet production at the LHC

# Formula for TMD gluons and gauge links

$$\mathcal{F}(x, k_T) = 2 \int \frac{d\xi^- d^2\xi_T}{(2\pi)^3 P^+} e^{ixP^+\xi^- - i\vec{k}_T \cdot \vec{\xi}_T} \langle P | \text{Tr} \left\{ \hat{F}^{i+}(0) \hat{F}^{i+}(\xi^+ = 0, \xi^-, \vec{\xi}_T) \right\} | P \rangle$$



Valid for large transversal momentum and was obtained in a specific gauge



similar diagrams with 2,3,...gluon exchanges. All this need to be resummed

From *S. Sapeta*

*C.J. Bomhof, P.J. Mulders, F. Pijlman  
Eur.Phys.J. C47 (2006) 147-162*

$$\mathcal{F}(x, k_T) = 2 \int \frac{d\xi^- d^2\xi_T}{(2\pi)^3 P^+} e^{ixP^+\xi^- - i\vec{k}_T \cdot \vec{\xi}_T} \langle P | \text{Tr} \left\{ \hat{F}^{i+}(0) \mathcal{U}_{C_1} \hat{F}^{i+}(\xi) \mathcal{U}_{C_2} \right\} | P \rangle$$

Hard part defines the path of the gauge link  $\mathcal{U}^{[C]}(\eta; \xi) = \mathcal{P} \exp \left[ -ig \int_C dz \cdot A(z) \right]$

# The saturation problem: suppressing gluons below $Q_s$

Originally formulated in coordinate space

Balitsky '96, Kovchegov '99

Fit AAMQS '10

NLO accuracy

Balitsky, Chirilli '07

and solved

Lappi, Mantysaari '15

Kinematic corrections

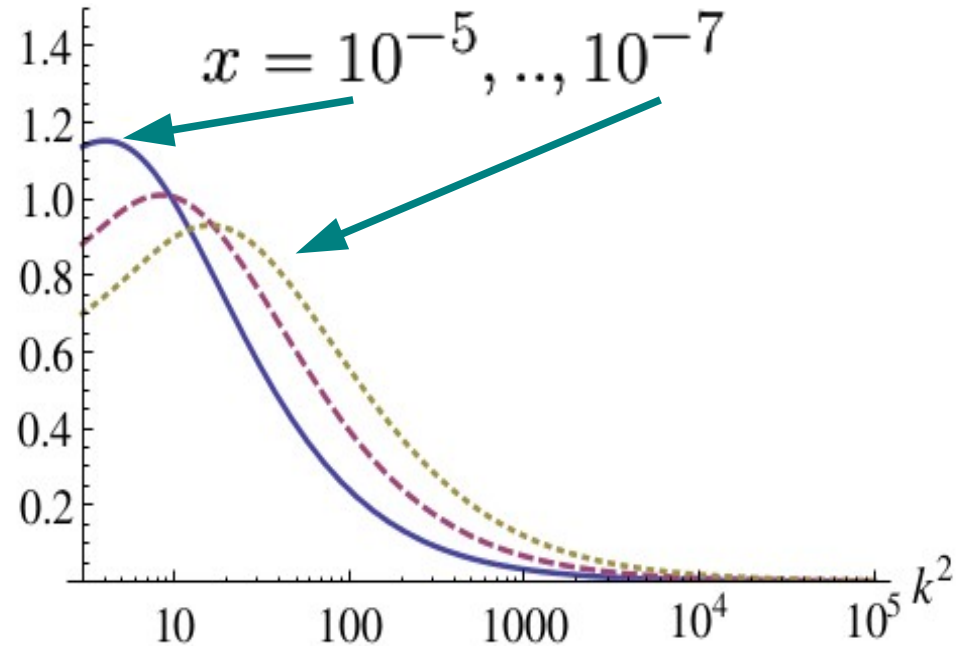
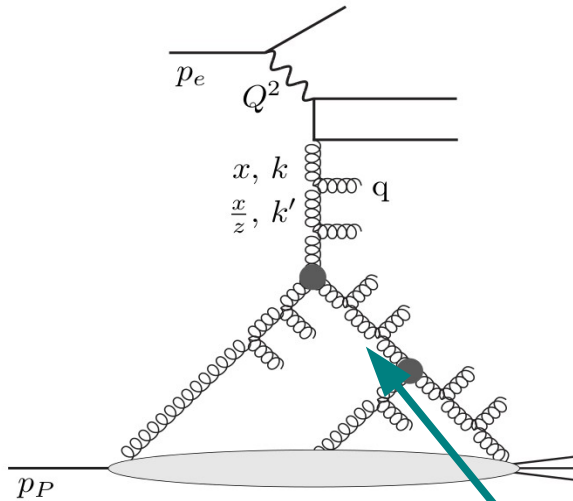
Iancu et al

Solved  $b$  dependent

Stasto, Golec-Biernat '02

with kinematic corrections and  $b$

Cepila, Contrares, Matas '18



solution of Balitsky-Kovchegov directly for dipole gluon density

Kwiecinski, Kutak '02

Nikolaev, Schafer '06

Fit to  $F_2$  data

KK. Sapeta '12

The momentum space BK equation for dipole gluon density

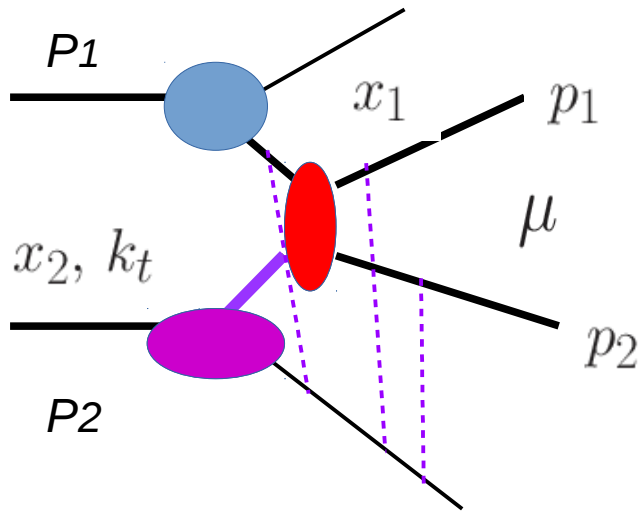
$$\mathcal{F} = \mathcal{F}_0 + K \otimes \mathcal{F} - \frac{1}{R^2} V \otimes \mathcal{F}^2$$

hadron's radius

Accounts for kinematical constraint,

Nonsingular parts of splitting function, running coupling

# The ITMD factorization for di-jets



- The color structure is separated from kinematic part of the amplitude by means of the color decomposition.
- The TMD gluon distributions are derived for the color structures following

P. Kotko, K. Kutak, C. Marquet, E. Petreska, S. Sapeta, A. van Hameren, JHEP 1509 (2015) 106

A. van Hameren, P. Kotko, K. Kutak, C. Marquet, E. Petreska JHEP 12 (2016) 034

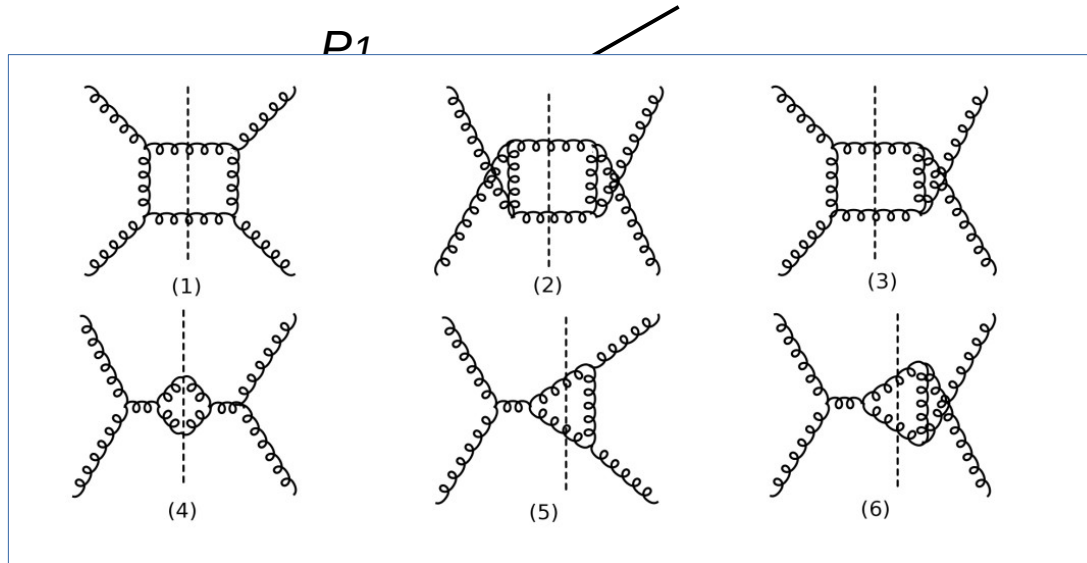
Formalism implemented in Monte Carlo programs KaTie by A. van Hameren

gauge invariant amplitudes with \$k\_t\$ and TMDs

Example for \$g^\* g \to g g\$

$$\frac{d\sigma^{pA \to ggX}}{d^2 P_t d^2 k_t dy_1 dy_2} = \frac{\alpha_s^2}{(x_1 x_2 s)^2} x_1 f_{g/p}(x_1, \mu^2) \sum_{i=1}^6 \mathcal{F}_{gg}^{(i)} H_{gg \to gg}^{(i)}$$

# Improved Transverse Momentum Dependent Factorization



from

F. Dominguez, C. Marquet,  
Bo-Wen Xiao, F. Yuan  
Phys.Rev. D83 (2011) 105005

The same gauge link and as in TMD 's

Fabio Dominguez, Bo-Wen Xiao, Feng Yuan  
Phys.Rev.Lett. 106 (2011) 022301

P. Kotko K. Kutak , C. Marquet , E. Petreska , S. Sapeta,  
A. van Hameren, JHEP 1509 (2015) 106

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Phys.Rev. D83 (2011) 105005

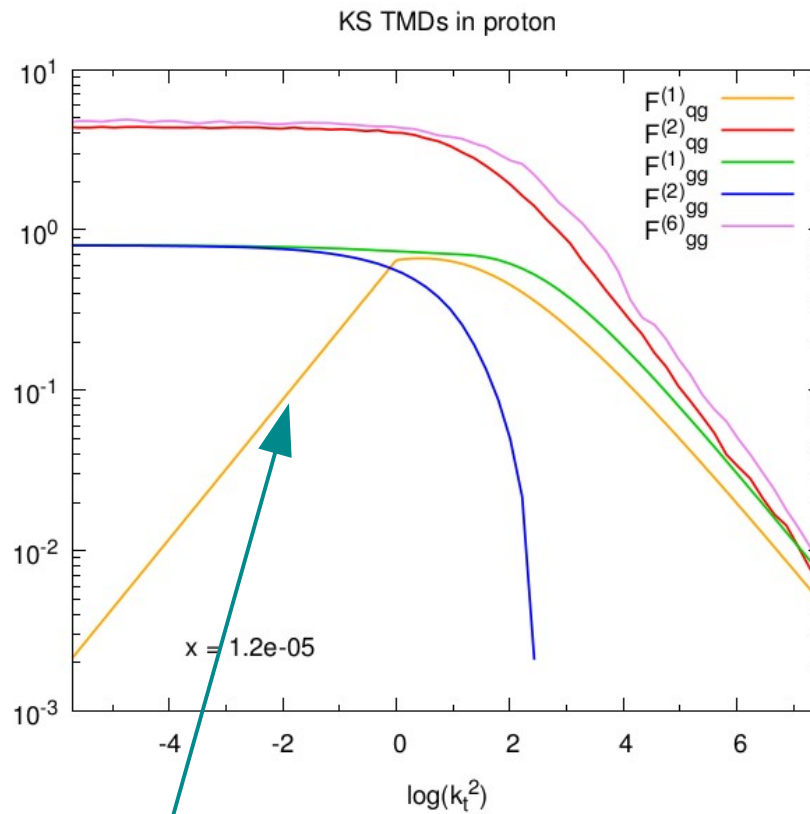
*gauge invariant amplitudes with  $k_t$  and TMDs*

*example for  $g^* g \rightarrow g g$*

$$\frac{d\sigma^{pA \rightarrow ggX}}{d^2 P_t d^2 k_t dy_1 dy_2} = \frac{\alpha_s^2}{(x_1 x_2 s)^2} x_1 f_{g/p}(x_1, \mu^2) \sum_{i=1}^6 \mathcal{F}_{gg}^{(i)} H_{gg \rightarrow gg}^{(i)}$$



# Plots of ITMD gluons



All gluons can be calculated from the dipole one. KS gluon used.

*Kotko, K.K, Marquet, Petreska, Sapeta, van Hameren JHEP 1612 (2016) 034*

**Standard HEF gluon density**

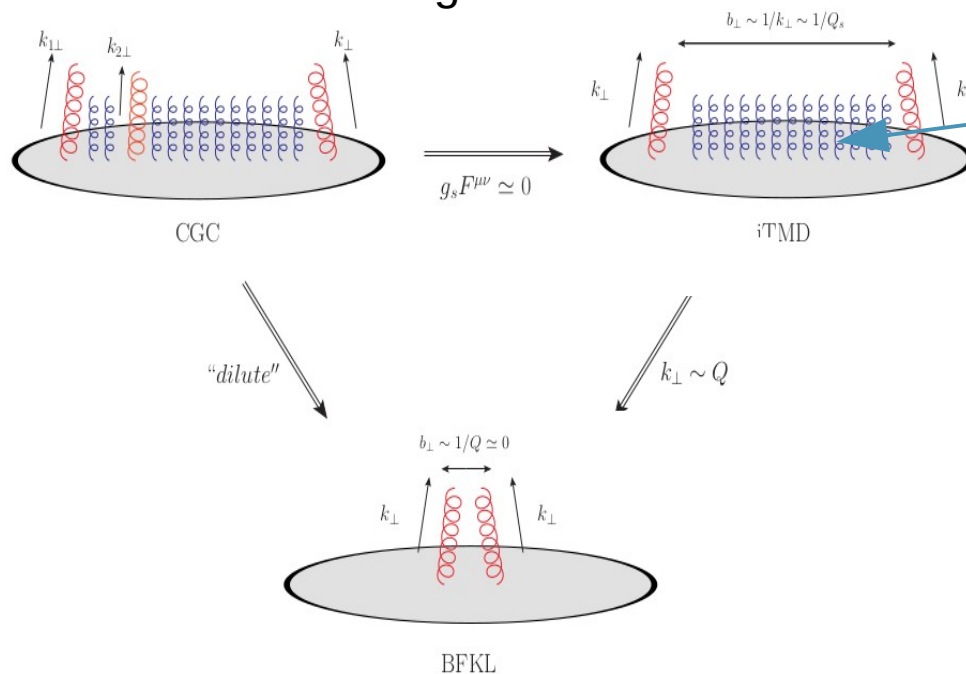
The other densities are flat at low  $k_t \rightarrow$  less saturation

Not negligible differences at large  $k_t \rightarrow$  differences at small angles

# ITMD from CGC

T. Altinoluk, R. Boussarie, P. Kotko JHEP 1905 (2019) 156  
 T. Altinoluk, R. Boussarie, JHEP10(2019)208

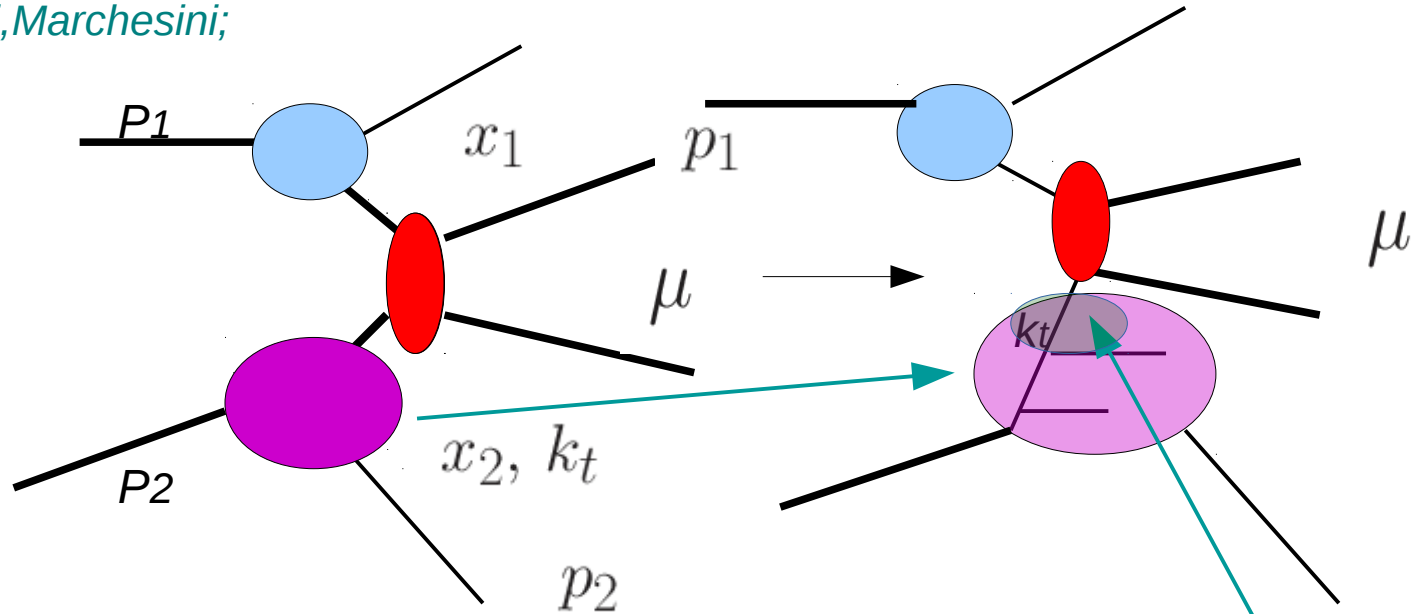
Expansion in distance - parameter entering as argument Wilson lines appearing in generic CGC amplitude i.e. amplitude for propagation in strong color field of target



# Other relevant effects – Sudakov form factor in ISR

The relevance in low  $x$  physics  
 at linear level recognized by:  
 Catani, Ciafaloni, Fiorani, Marchesini;  
 Kimber, Martin, Ryskin;  
 Collins, Jung

Survival probability  
 of the gap without  
 emissions



If hard scale is larger than  $kt$  the phase space  
 opens for hard scale resummation

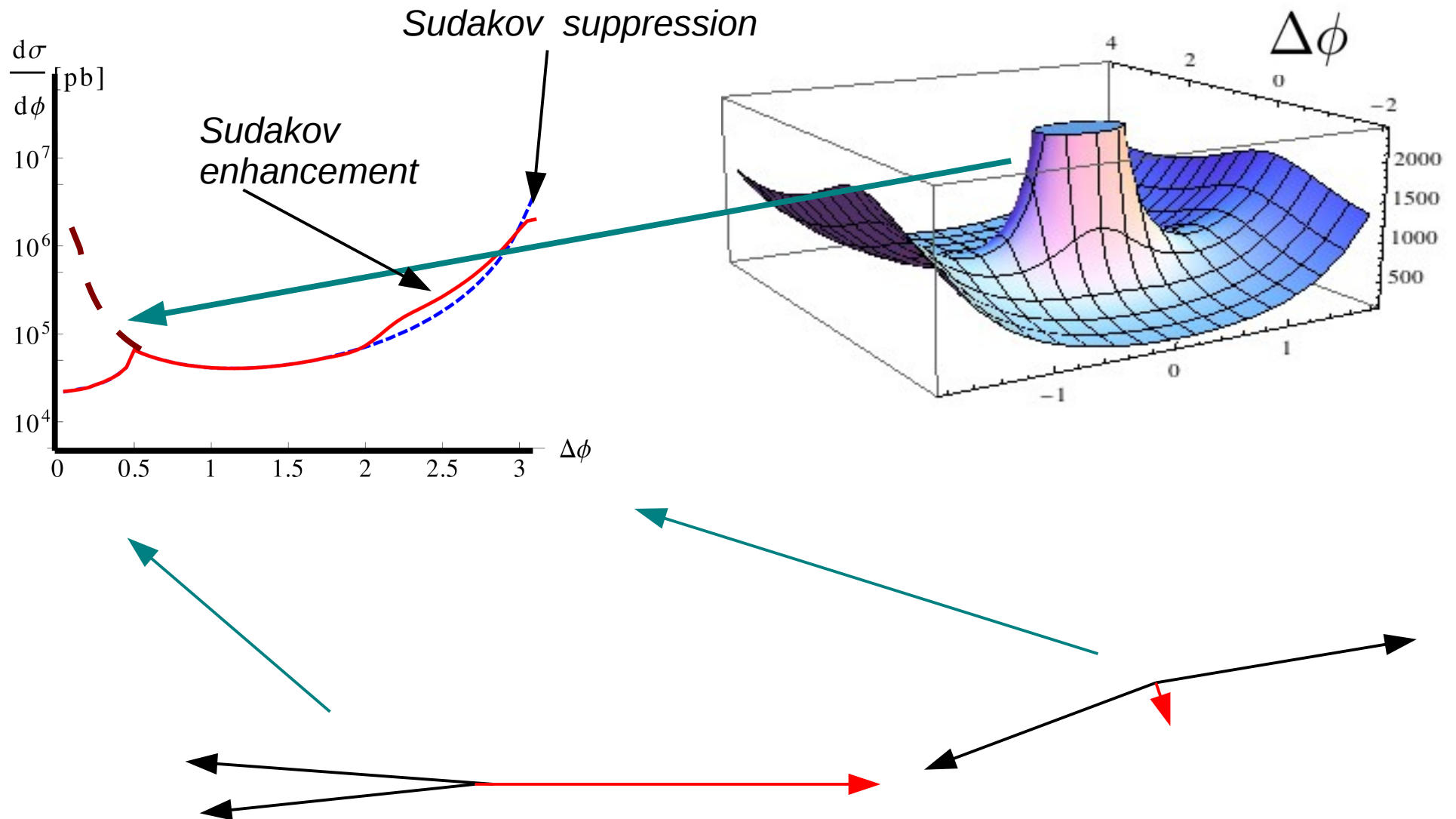
Survival probability of the gap  
 without emissions

Mueller, Xiao, Yuan '12  
 Mueller, Xiao, Yan '13  
 Van Hameren, Kotko, Kutak, Sapeta '14  
 Xiao, Yuan, Zhou '17  
 Zhou '16  
 Kutak '14

# Other relevant effects – Sudakov form factor

Divergence regularized  
by jet algorithm

K.K '14



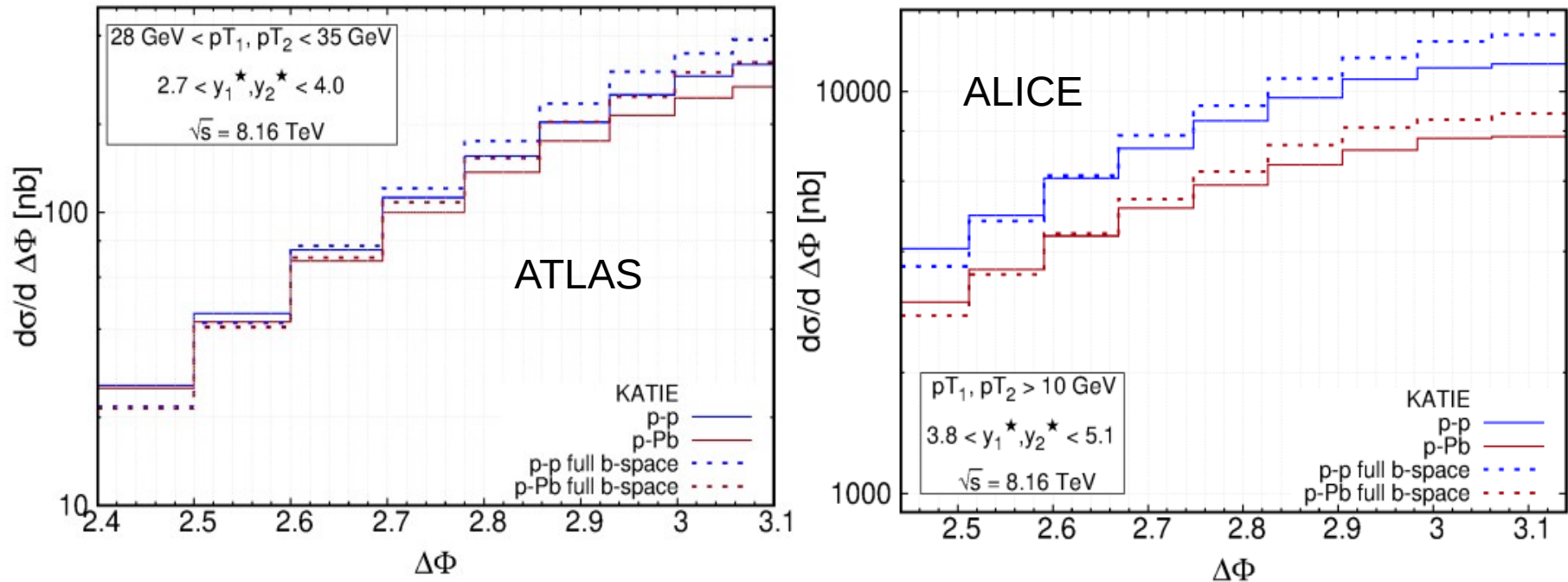
## ITMD +Sudakov

$$\frac{d\sigma^{\text{pA} \rightarrow j_1 j_2 + X}}{d^2 P_T d^2 k_T dy_1 dy_2} = \sum_{a,c,d} x_p f_{a/p}(x_p, \mu) \sum_{i=1}^2 \mathcal{K}_{ag^* \rightarrow cd}^{(i)}(P_T, k_T; \mu) \Phi_{ag \rightarrow cd}^{(i)}(x_A, k_T)$$

$$\begin{aligned} \frac{d\sigma^{\text{pA} \rightarrow j_1 j_2 + X}}{d^2 P_T d^2 k_T dy_1 dy_2} &= \sum_{a,c,d} x_p \sum_{i=1}^2 \mathcal{K}_{ag^* \rightarrow cd}^{(i)}(P_T, k_T; \mu) \\ &\times \int db_T b_T J_0(b_T k_T) f_{a/p}(x_p, \mu b) \tilde{\Phi}_{ag \rightarrow cd}^{(i)}(x_A, b_T) e^{-S^{ag \rightarrow cd}(\mu, b_\perp)} \end{aligned}$$

Depending on the choice of scale the collinear pdf can be put in front of the integral or kept under the integral. We consider both options and call them factorized and unfactorized. The Sudakov is at DLL accuracy.

# Azimuthal angle dependence – parton level



Visible differences especially for ALICE FoCal between p-p and p-Pb results.

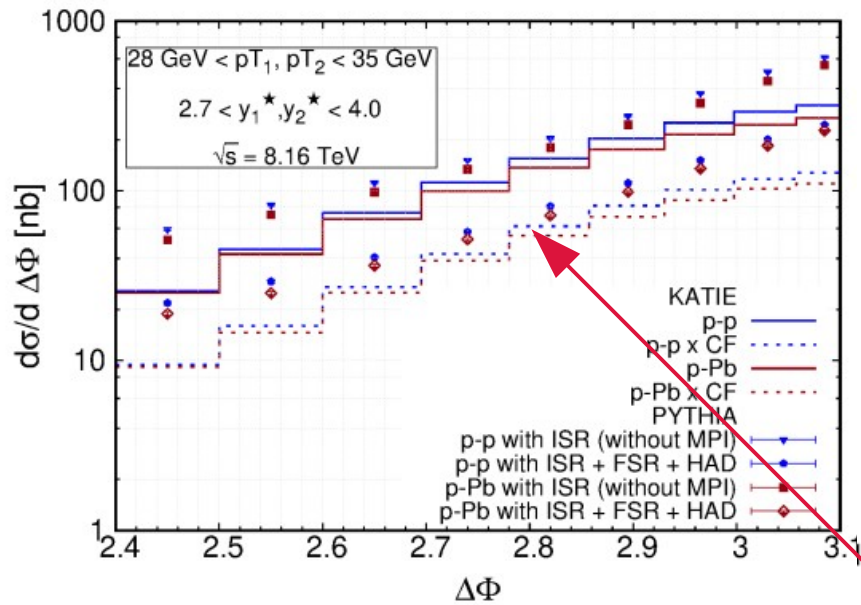
Lower pt cut and more forward rapidities.

Not large differences between to approaches to account for Sudakov form factor.

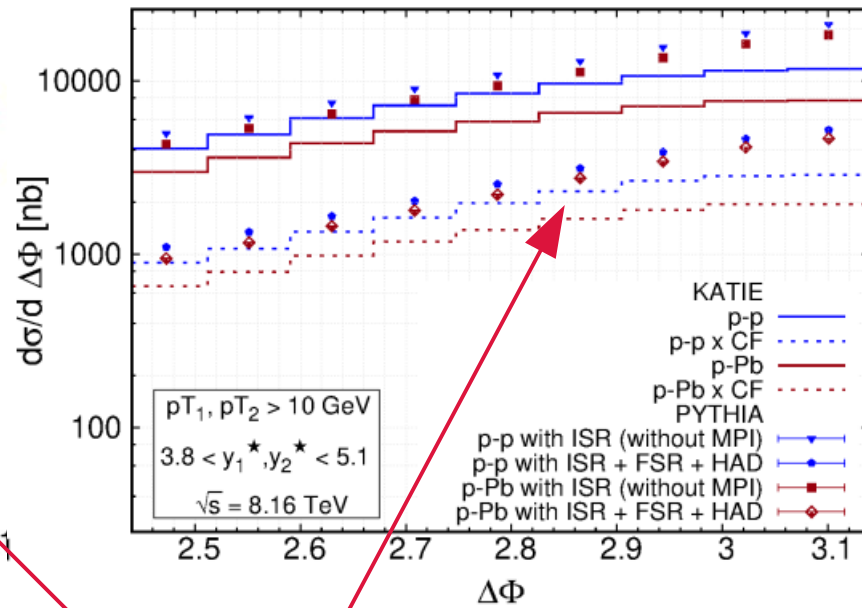
For earlier results see

*A. Hameren, P. Kotko, K. Kutak, S. Sapeta  
Phys.Lett. B795 (2019) 511-515*

# Azimuthal angle dependence – adding correction factor



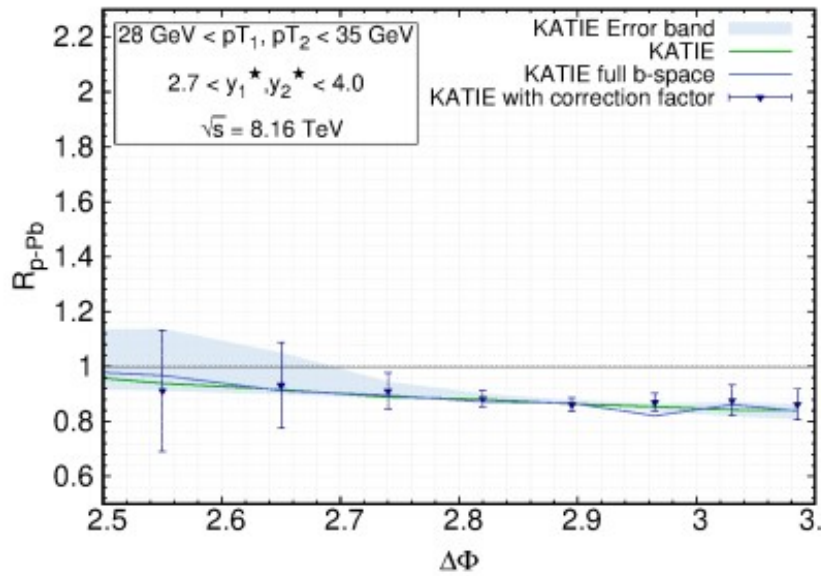
ATLAS



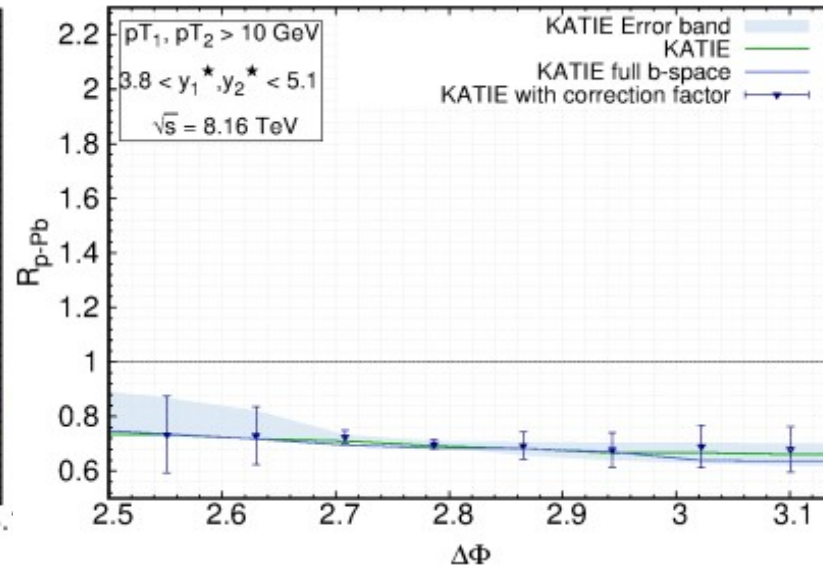
ALICE

“Corrected” parton level  
PYTHIA and KATIE

# Nuclear modification ratio



ATLAS



ALICE

Visible suppression in both ATLAS and ALICE kinematical setup.  
Correction factor effectively cancels. Strong saturation signal.

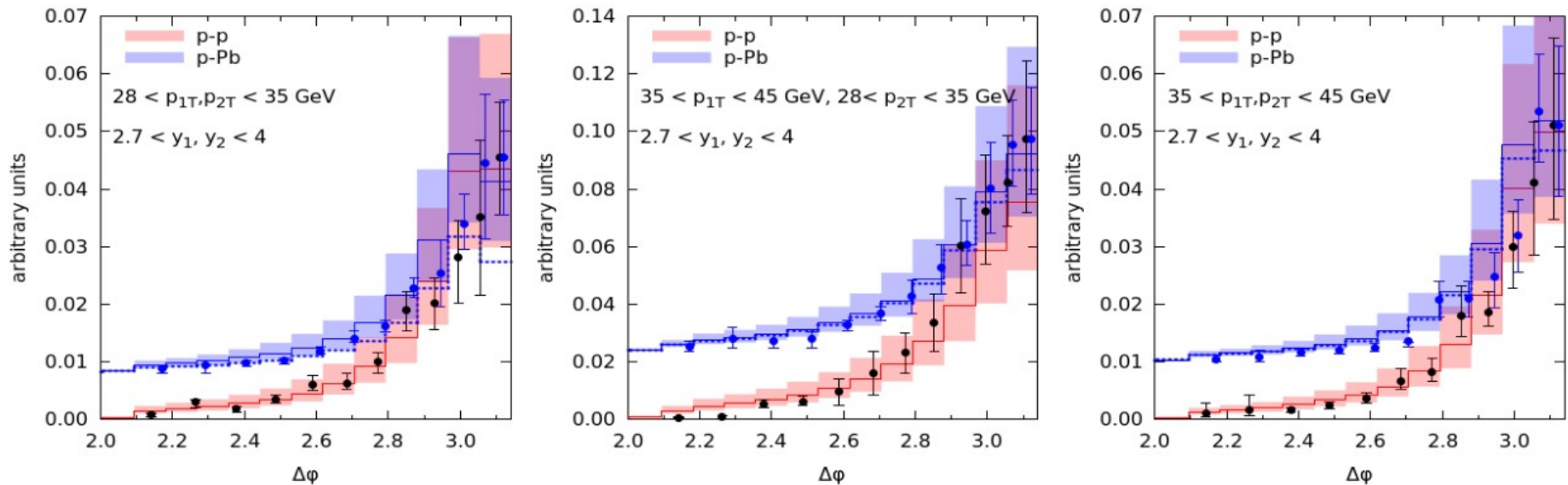
$$R_{p-Pb} = \frac{d\sigma^{p+Pb}}{A \frac{d\sigma^{p+p}}{d\mathcal{O}}}$$



# Signature of saturation in forward-forward dijets

ATLAS 1901.10440

van Hameren, Kotko, Kutak, Sapeta '19

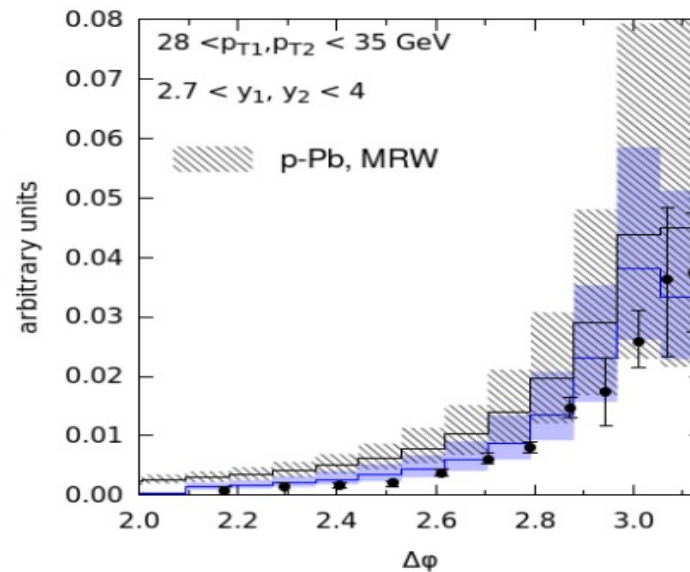
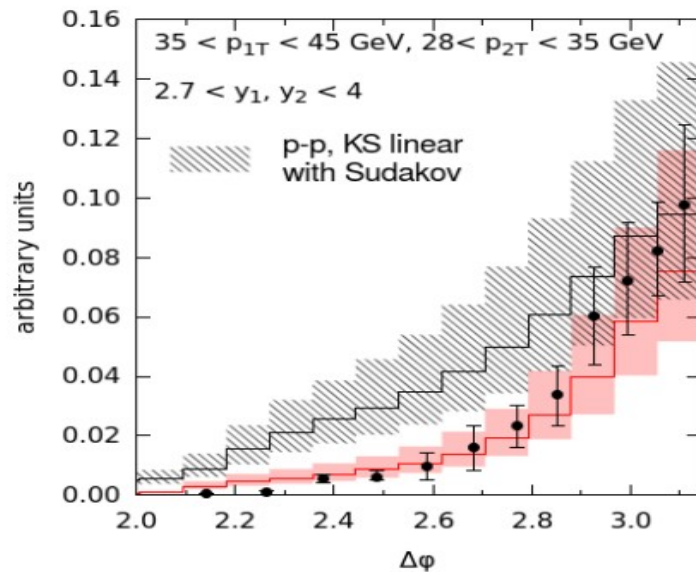
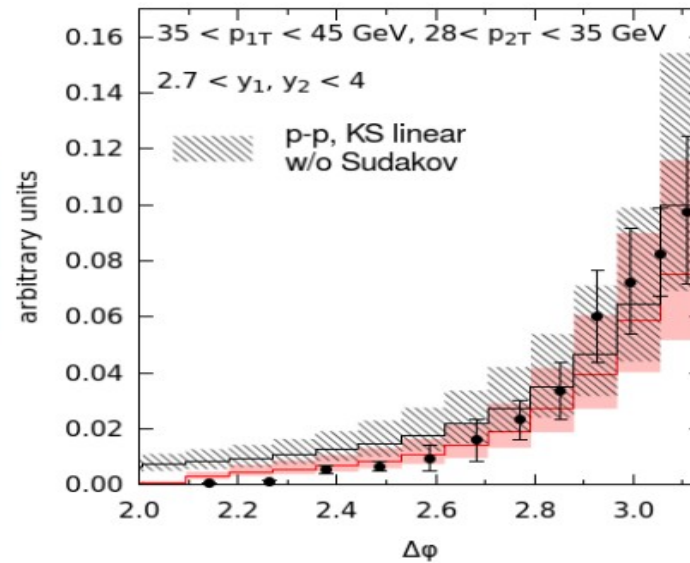
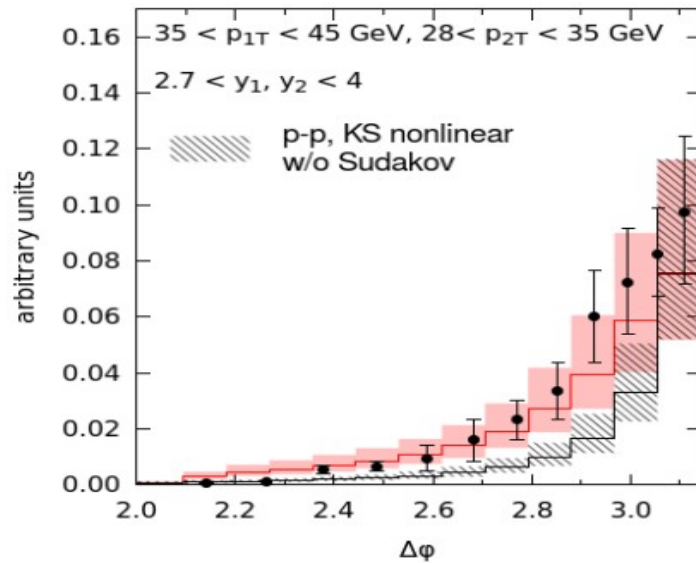


Data: number of dijets normalized to number of single inclusive jets. We can not calculate that.  
We can compare shapes.

Procedure: fit normalization to p-p data. Use that both for p-p and p-Pb. Shift p-Pb data

The procedure allows for visualization of broadening

# Other possible scenarios



Backup

# Azimuthal angle dependence – adding correction factor

