



IN THE GLASMA

by Dana Avramescu

University of Jyväskylä, Center of Excellence in Quark Matter

based on [2303.05599]

Supervisors: T. Lappi, H. Mäntysaari (Uni Jyväskylä)

Collaborators: A. Ipp, D. Müller (TU Wien), V. Greco, M. Ruggieri (Uni Catania),
V. Băran (Uni Bucharest)

Hard Probes in Aschaffenburg, March 2023

General outline

1 Introduction

Framework • Literature • This study

2 Hard probes in Glasma

Glasma • Probes in Glasma • Numerics

3 Key results

Heavy quarks • Jets

4 Highlights

Heavy-ion collisions

Heavy-ion collision \leftrightarrow multi-stage process with each stage \mapsto effective theory

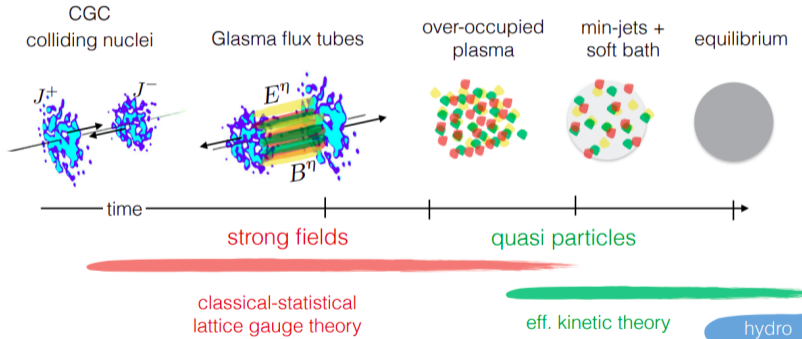


Figure from S. Schlichting's talk [1]

Initial stage

Initial stage using **Color Glass Condensate** \leftrightarrow EFT for high energy QCD
High energy nucleus \rightsquigarrow many gluons \Rightarrow classical colored fields \equiv **Glasma**

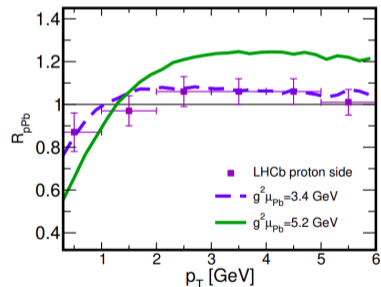


Figure from F. Salazar's talk [2]

Literature timeline

- 2018 ● Coci, Das, Greco, Ruggieri, Plumari, Sun
[1805.09617], [1902.06254]
- 2020 ● Ipp, Müller, Schuh
- 2020 ● Boguslavski, Kurkela, Lappi, Peuron
- 2021 ● Carrington, Czajka, Mrowczynski
- 2023 ● Avramescu, Băran, Greco, Ipp, Müller, Ruggieri

Heavy quarks in Glasma
Highlights: Diffusion, v_2 , R_{AA}

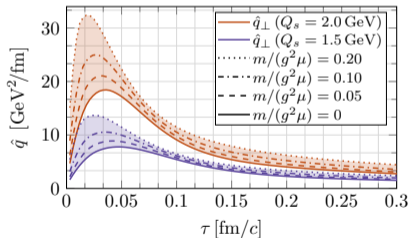


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[2001.10001], [2009.14206]
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Lightlike jets in Glasma
Highlight: Large \hat{q} at small τ

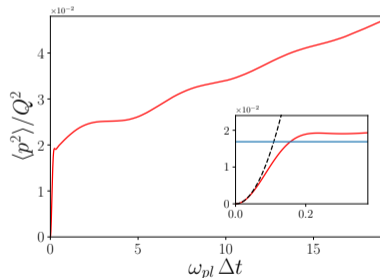


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[2005.02418], [2001.11863]
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Static quarks in gluon plasma
Highlight: Rapid increase in $\langle p^2 \rangle$

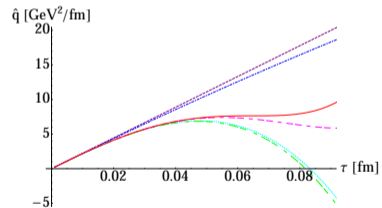


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[2112.06812], [2202.00357]
- 2023 ● Avramescu, Băran, Greco, Ipp, Müller, Ruggieri

Analytical hard probes in Glasma
Highlight: Significant \hat{q} in early τ



Literature timeline



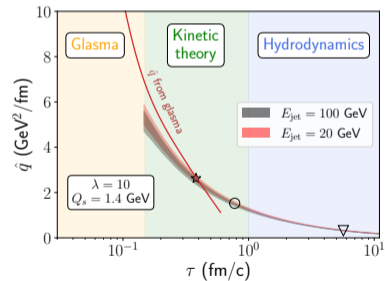
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[2303.05599]

This talk. No spoilers.

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- 2023 ● Boguslavski, Kurkela, Lappi, Lindenbauer, Peuron
[2303.12520], [2303.12595]

Hard probes with kinetic theory
Highlight: Fill gap Glasma \mapsto hydro



Motivation



Literature \Rightarrow qualitatively significant impact

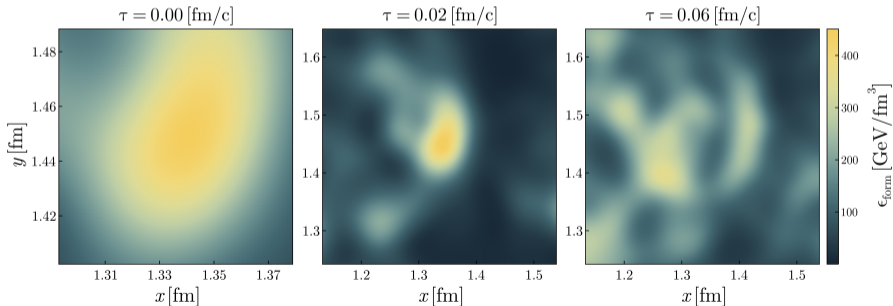
This study: How much? \Leftrightarrow refinements: $\left\{ \begin{array}{l} \text{fields} \mapsto \text{SU}(3) \text{ lattice} \\ \text{particles} \mapsto \text{full dynamics} \end{array} \right. \Rightarrow \text{GPU solver}$

Approach



Prerequisite: Classical lattice gauge theory $\xrightarrow{\text{solver}}$ Glasma fields

Task: Glasma fields $\xleftrightarrow{\text{background}}$ ensemble of particles $\xleftarrow{\text{solver}}$ colored particle-in-cell method

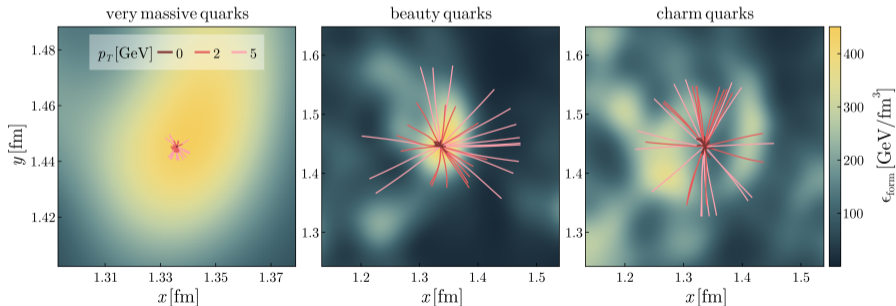


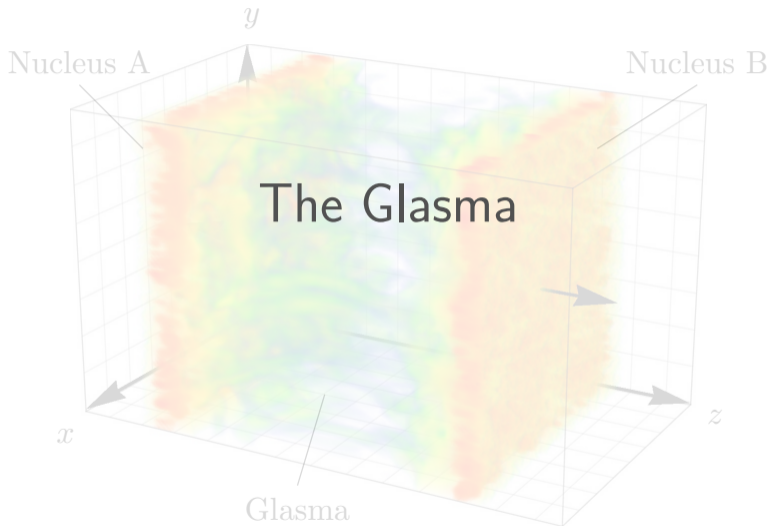
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CGC basics *(technicalities)*



Separation of scales between **small- x** and **large- X** degrees of freedom
Small- x \Leftrightarrow classical gluon fields \mapsto **Yang-Mills** equations with sources \Leftrightarrow **large- X**

$$\begin{array}{c} \text{covariant derivative} \quad \text{field strength tensor} \\ \hline \left(\mathcal{D}_\mu \quad F^{\mu\nu} \right) \left[A^\mu \right] = J^\nu \\ \text{gluons gauge field} \quad \text{color current of nucleus} \end{array}$$

$$\text{McLerran-Venugopalan model} \mapsto J^{\mu,a}(x) \propto \delta^{\mu+} \rho^a(x^-, \mathbf{x}_\perp)$$

$\underbrace{\hspace{10em}}_{\text{large nuclei}} \quad \underbrace{\hspace{10em}}_{\text{stochastic variable}}$

Two-point function $\langle \rho^a \rho^a \rangle \propto Q_s^2$ saturation momentum

CGC basics *(technicalities)*



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large nuclei \uparrow stochastic variable

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Collision of CGC nuclei

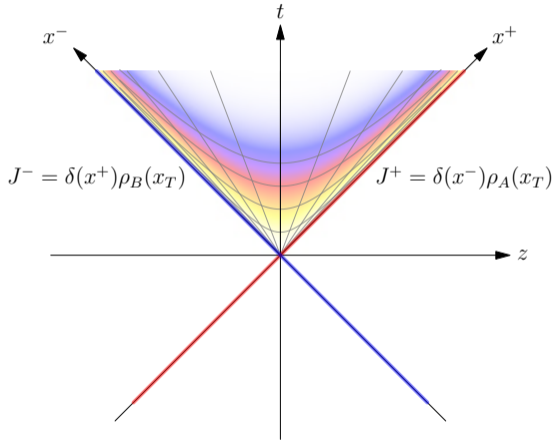


Figure credits to D. Müller

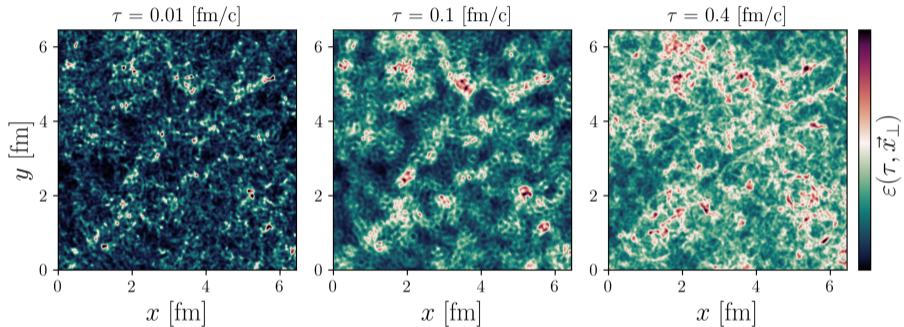
- Thin nuclei along light-cone
- Glasma fields in the forward light-cone

Milne coordinates (τ, η)
 $\tau = \sqrt{2x^+x^-}$, $\eta = \ln(x^+/x^-)/2$

Boost-invariant approximation
fields = indep(η)

Numerical solution of Yang-Mills
equations \Rightarrow Glasma

Glasma fields



Relevant scale Q_s

Fields *dilute* after $\delta\tau \simeq Q_s^{-1}$, arrange themselves in *correlation domains* of $\delta x_T \simeq Q_s^{-1}$

Boost-invariant, highly anisotropic

Nucleus A

y

Probes in Glasma

z

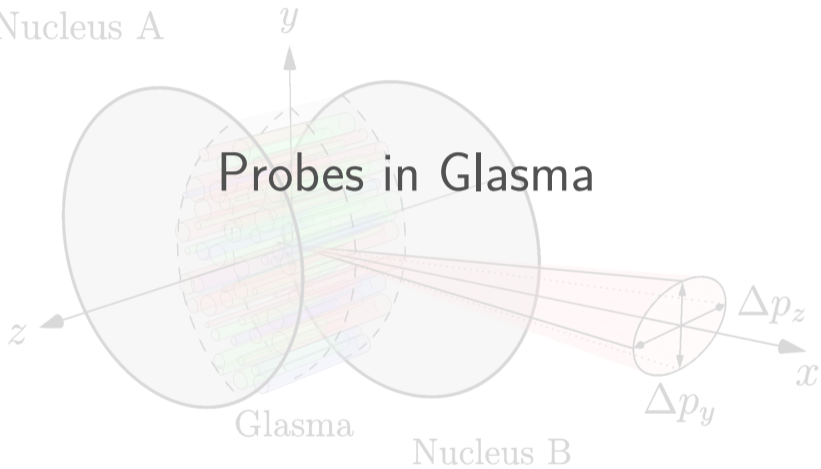
Glasma

Nucleus B

Δp_z

x

Δp_y



Particles in YM fields *(technicalities)*

Wong's equations \leftrightarrow classical equations of motion for particles (x^μ, p^μ, Q) evolving in Yang-Mills fields A^μ

$$\frac{d}{d\tau} x^\mu = \frac{p^\mu}{m},$$

coordinate (pointing to x^μ)
 mass (pointing to m)
 proper time (pointing to $d\tau$)

$$\frac{D}{d\tau} p^\mu = 2g \text{Tr} \left\{ Q F^{\mu\nu} [A^\mu] \right\} \frac{p_\nu}{m},$$

momentum (pointing to p^μ)
 gauge field (pointing to A^μ)
 coupling constant (pointing to g)
 covariant derivative (pointing to $\frac{D}{d\tau}$)

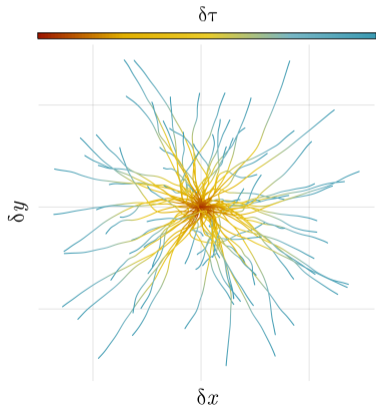
$$\frac{d}{d\tau} Q = -ig [A_\mu, Q] \frac{p^\mu}{m}$$

color charge (pointing to Q)
 color rotation $\rightarrow U \in \text{SU}(3)$
 $Q(\tau) = U(\tau, \tau') Q(\tau') U^\dagger(\tau, \tau')$

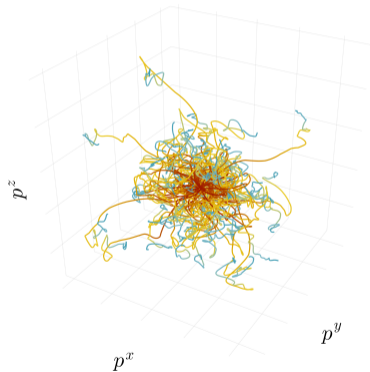
CPIC solver $\xrightarrow{\text{assures}}$ $Q \in \text{SU}(3)$, conservation of Casimir invariants

Glasma plate *(just before lunch...)*

Spaghetti coordinate trajectories



Noodles momentum trajectories



Quantifying the effect of Glasma



Momentum broadening

$$\delta p_\mu^2(\tau) \equiv p_\mu^2(\tau) - p_\mu^2(\tau_{\text{form}})$$

Instantaneous transport coefficient

$$\frac{d}{d\tau} \langle \delta p_i^2(\tau) \rangle \equiv \begin{cases} \kappa_i(\tau), & \text{heavy quarks} \\ \hat{q}_i(\tau), & \text{jets} \end{cases}$$

$$\text{Anisotropy} \equiv \langle \delta p_L^2 \rangle / \langle \delta p_T^2 \rangle$$

Toy model particle setup

- Uniformly distributed in (x, y)
- Formed at $\tau_{\text{form}} \propto 1/m$
- Fixed initial $p_T(\tau_{\text{form}})$

Glasma setup

- Large nuclei, central collisions
- Saturation scale $Q_s = 2 \text{ GeV}$

Quantifying the effect of Glasma



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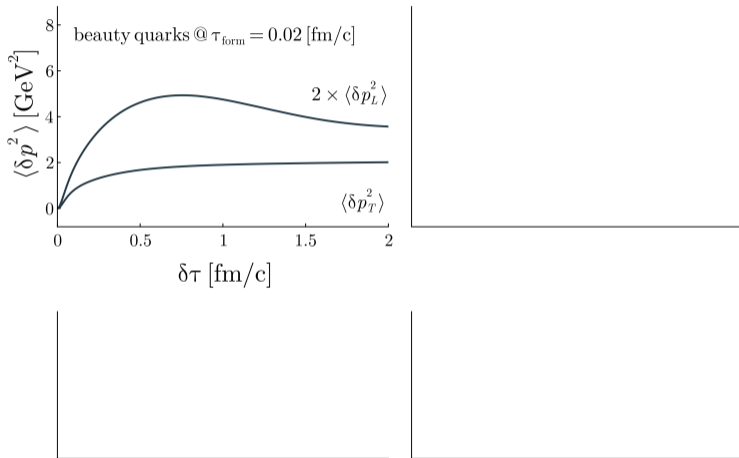
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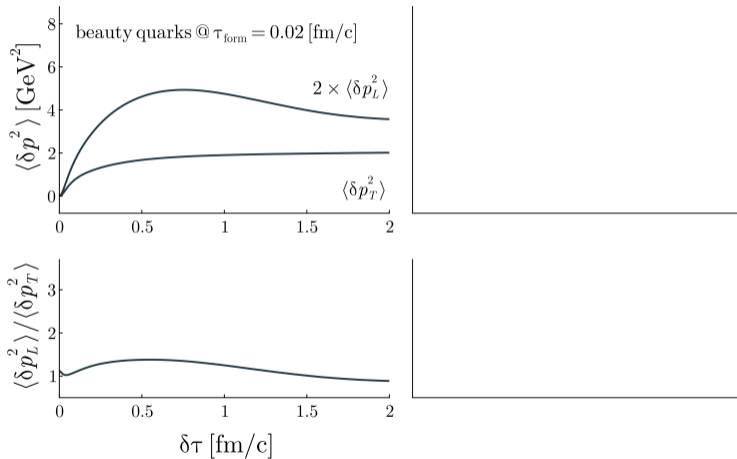
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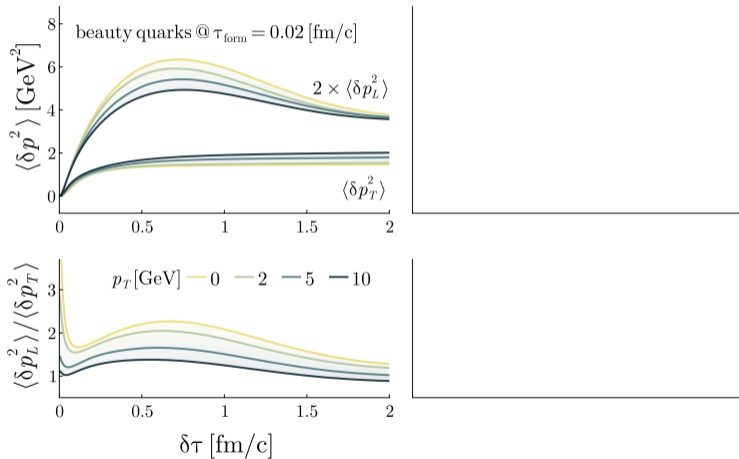
Heavy quark momentum broadening



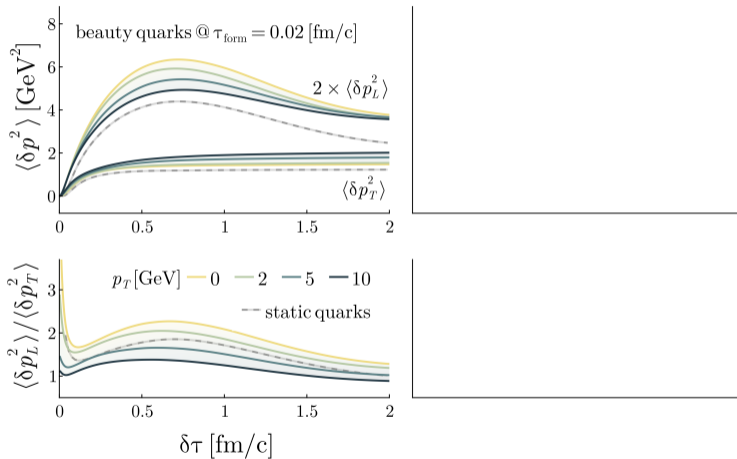
Heavy quark momentum broadening



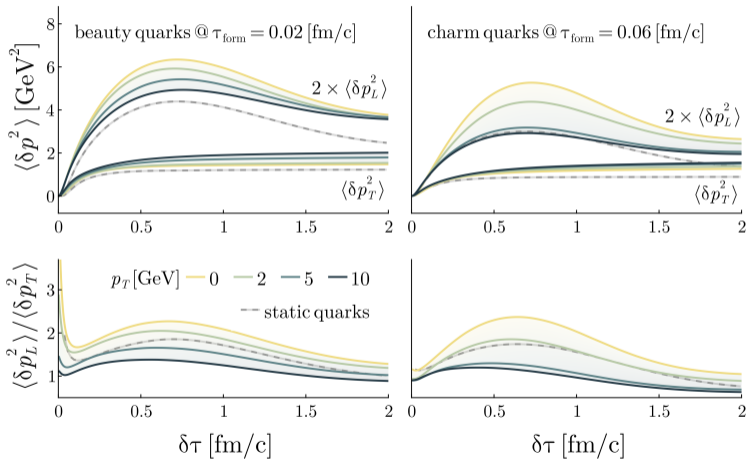
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Heavy quark momentum broadening

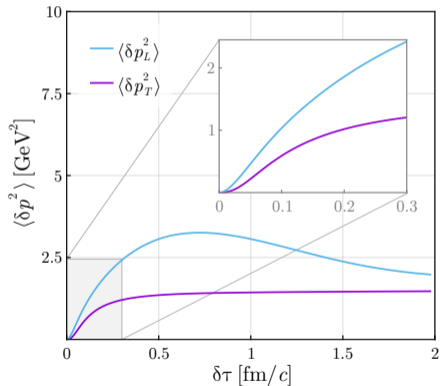


Heavy quark momentum broadening

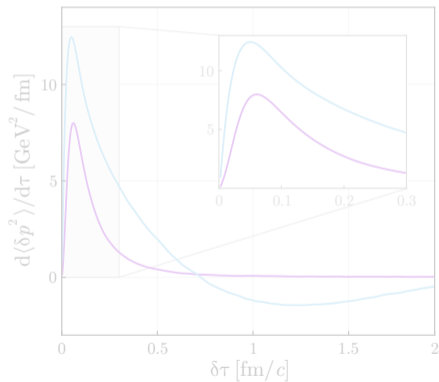


Transport in Glasma *(study case: beauty quarks)*

Rapid increase in $\langle p^2 \rangle$



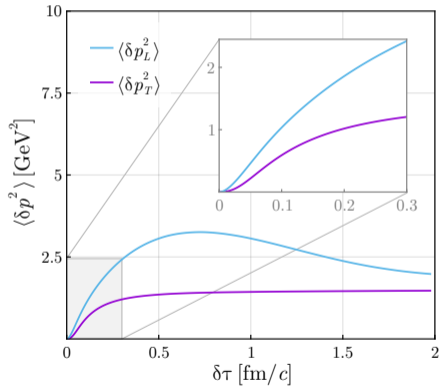
\Rightarrow Early peak* in κ



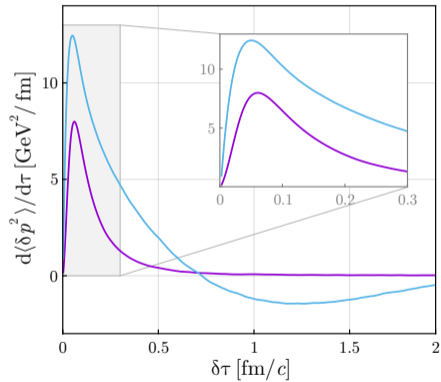
* $\kappa_{\text{peak}} \approx 15 \text{ GeV}^2 / \text{fm}$ but peak value depends on particle (m , τ_{form} , initial p_T) and Glasma (Q_s)

Transport in Glasma *(study case: beauty quarks)*

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Jet momentum broadening

Schematic geometry of jets in Glasma

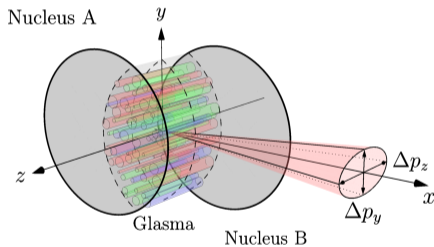
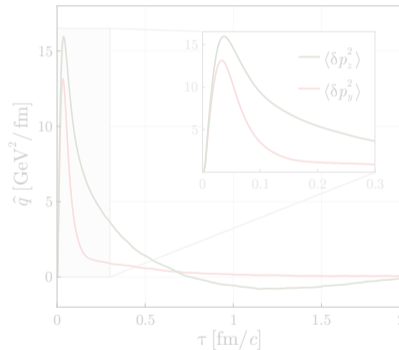


Figure from [2009.14206]

Early larger peak* in \hat{q}



* $\hat{q}_{\text{peak}} \approx 25 \text{ GeV}^2/\text{fm}$ with weak dependence on particle (m or initial p^x) but affected by Glasma (Q_s)

Jet momentum broadening

Schematic geometry of jets in Glasma

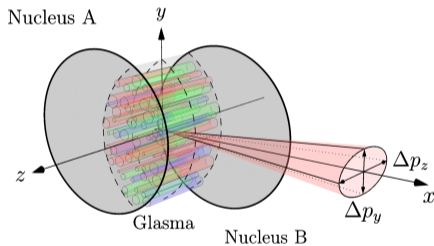
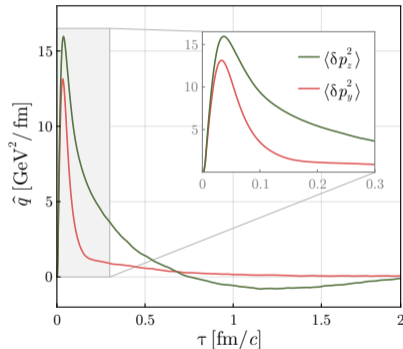


Figure from [2009.14206]

Early larger peak* in \hat{q}



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This is plausible!

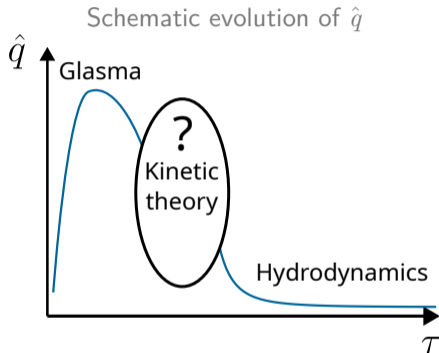
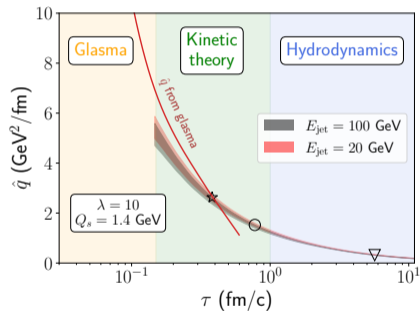


Figure from [2303.12595]

Kinetic theory* connects large \hat{q} in Glasma to subsequent hydrodynamics



* Bottom-up thermalization scenario

Recall Kirill Boguslavski's plenary @ Monday, see Jarkko Peuron's talk @ Wednesday
Moreover, see Marcos González Martínez's talk @ Wednesday

Highlights



This work:

Numerical solver for hard probes in Glasma

$\langle \delta p^2 \rangle \Rightarrow d\langle \delta p^2 \rangle / d\tau \mapsto \kappa$ or \hat{q} **large** and **peaked**, $\langle \delta p_L^2 \rangle / \langle \delta p_T^2 \rangle$
Effect of τ_{form} , m and $p_T(\tau_{\text{form}})$

Work in progress:

Behavior of $\langle \delta p^2 \rangle \rightsquigarrow$ Glasma field correlators
 $Q\bar{Q}$ angular correlations in Glasma

Improvements:

Jet energy loss
Hard probes in 3+1D Glasma

Highlights



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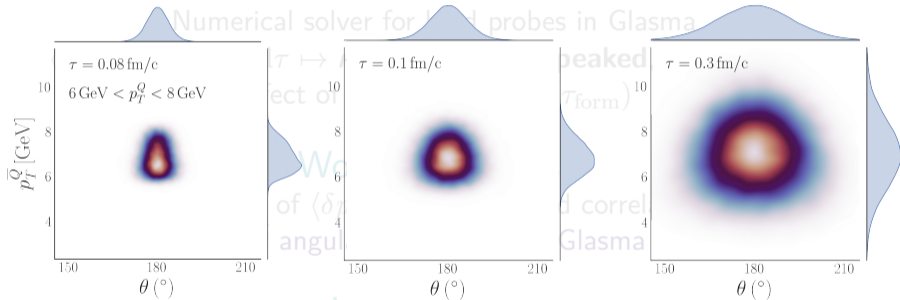
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This work:



$c\bar{c}$ pairs initially produced back-to-back, measure θ pair angle in Glasma, FONLL initial p_T

Hard probes in 3+1D Glasma

Highlights



This work:

Numerical solver for hard probes in Glasma

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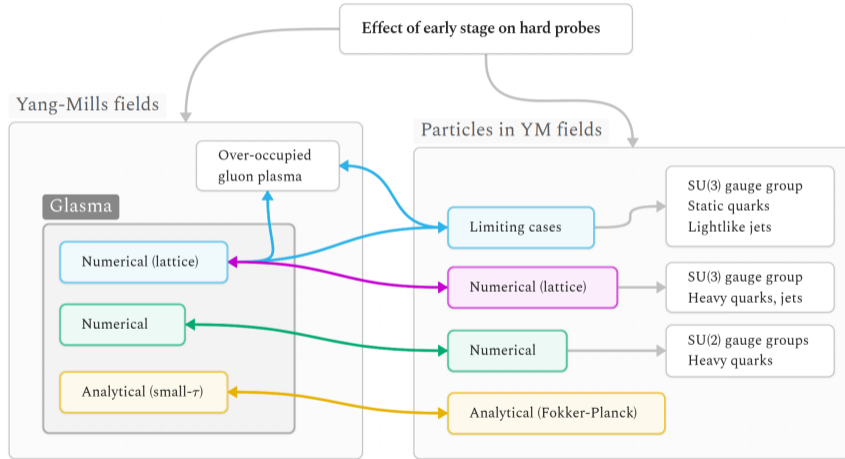
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Thank you!

Back-up

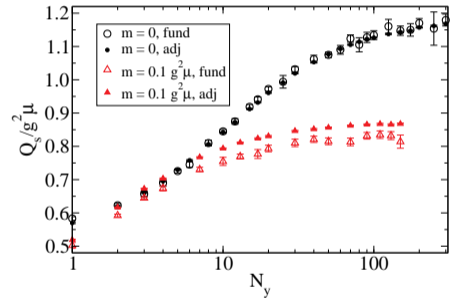
Synthesis of hard probes in initial stages



Features of the Glasma fields



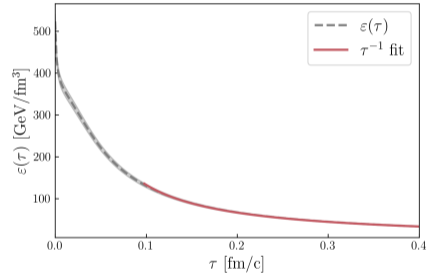
- ▶ Relevant scale \rightarrow **saturation momentum** Q_s
from DIS $\Rightarrow Q_s/g^2\mu$ [7]
- ▶ Fields \rightsquigarrow dilute after $\delta\tau \simeq Q_s^{-1}$
- ▶ Fields \rightsquigarrow correlation domains of transverse size
 $\delta x_T \simeq Q_s^{-1}$
- ▶ Anisotropic field configurations



Features of the Glasma fields



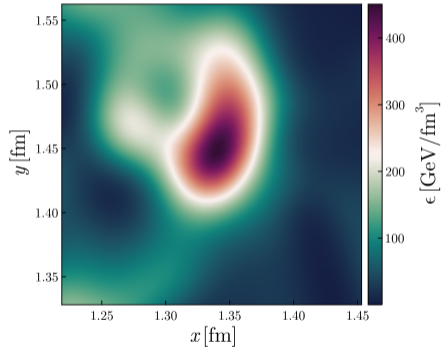
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Features of the Glasma fields



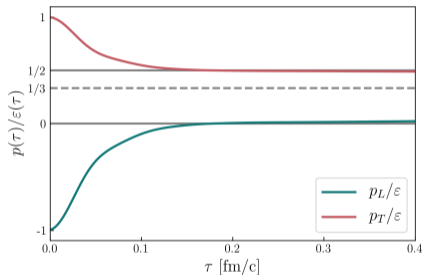
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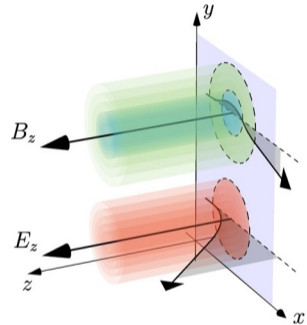
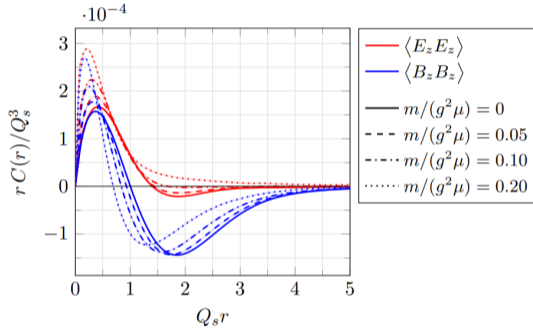
Features of the Glasma fields



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- ▶ **Anisotropic** field configurations



Glasma electromagnetic fields



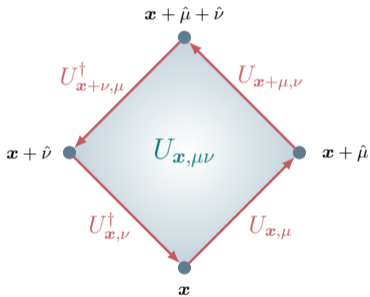
Correlation domains of typical size $1/Q_s$
Longitudinal electric fields **correlated**, magnetic fields exhibit **anti-correlation**

Figures from [2001.10001], [2009.14206]

Numerical implementation *(technicalities)*



Boost-invariant Yang-Mills equations for $A_i(\tau, \vec{x}_\perp, \cancel{\mathcal{H}})$ and $A_\eta(\tau, \vec{x}_\perp, \cancel{\mathcal{H}})$



Trace of a plaquette \mapsto gauge invariant
Wilson lines on the lattice \leftrightarrow **gauge links**

$$U_{x,\mu} = \exp\{igaA_\mu(x)\}$$

Wilson loops on lattice \leftrightarrow **plaquettes**

$$U_{x,\mu\nu} \equiv U_{x,\mu} U_{x+\mu,\nu} U_{x+\mu,\mu}^\dagger U_{x,\nu}^\dagger$$

Glasma $\xrightarrow{\text{boost invariance}}$ transverse gauge links $U_i(\tau, \vec{x}_\perp)$, while $A_\eta(\tau, \vec{x}_\perp)$

Color rotation on the lattice *(oversimplified)*



Color charge $\xrightarrow{\text{evolved by}}$ color lattice rotation $Q(\tau) = \mathcal{U}(\tau, \tau_0) Q(\tau_0) \mathcal{U}^\dagger(\tau, \tau_0)$
particle Wilson line $\mathcal{U} \in \text{SU}(3) \leftrightarrow$ path-ordered exponential from Glasma gauge fields

Initial color charge $Q_0 = Q_0^a T^a$ constructed with fixed quadratic q_2 and cubic q_3 Casimirs

$$q_2(R) = Q_0^a Q_0^a, \quad q_3(R) = d_{abc} Q_0^a Q_0^b Q_0^c, \quad R \mapsto \text{representation}$$

Particle temporal Wilson line $\mathcal{U}(\tau, \tau_0) = \mathcal{P} \exp \left\{ ig \int_{\tau_0}^{\tau} d\tau' \frac{dx^\mu}{d\tau'} A_\mu(x^\mu) \right\}$

Color rotation on the lattice *(details)*



In the Glasma, it simplifies to:

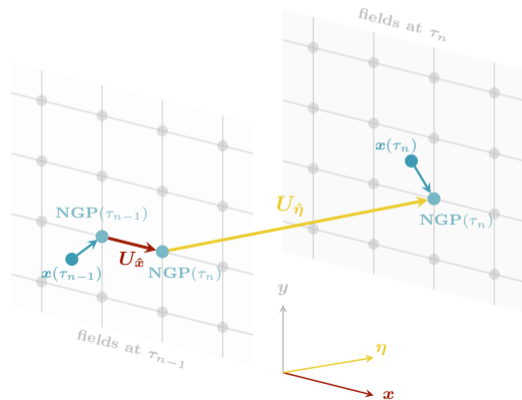
$$\mathcal{U}(\tau_0, \tau) = \mathcal{P} \exp \left\{ ig \int_{\tau_0}^{\tau} d\tau' \overrightarrow{A}_{\tau'} + ig \int_{\vec{x}_{\perp}(\tau_0)}^{\vec{x}_{\perp}(\tau)} dx'^i \mathbf{A}_i(\vec{x}'_{\perp}(\tau)) + ig \underbrace{\int_{\eta(\tau_0)}^{\eta(\tau)} d\eta'}_{\eta(\tau) - \eta(\tau_0)} \underbrace{A_{\eta}(\vec{x}_{\perp}(\tau))}_{\text{indep}(\eta')} \right\}$$

$$\text{Numerically: } \mathcal{U}(\tau_{n-1}, \tau_n) \approx \underbrace{\exp \left\{ ig \int_{\mathbf{x}_{n-1}}^{\mathbf{x}_n} dx'^i \mathbf{A}_i(\mathbf{x}'_n) \right\}}_{U_{\mathbf{x}_{n-1}, \hat{i}}(\tau_n)} \times \underbrace{\exp \{ ig \delta \eta_n A_{\eta}(\mathbf{x}_n) \}}_{\equiv U_{\mathbf{x}_n, \hat{\eta}}(\tau_n)}$$

Color rotation on the lattice (visualization)



$$Q(\tau_n) = \mathcal{U}(\tau_{n-1}, \tau_n) Q(\tau_{n-1}) \mathcal{U}^\dagger(\tau_{n-1}, \tau_n) \text{ with } \mathcal{U}(\tau_{n-1}, \tau_n) = U_{x_{n-1}, \hat{x}} \cdot U_{x_{n-1}, \hat{\eta}}$$

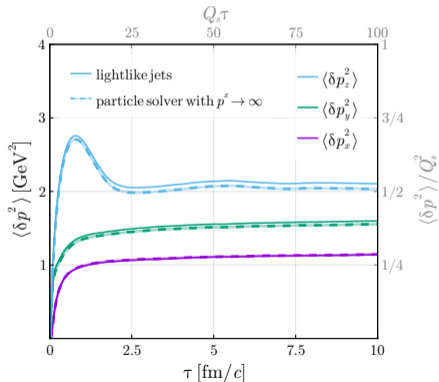
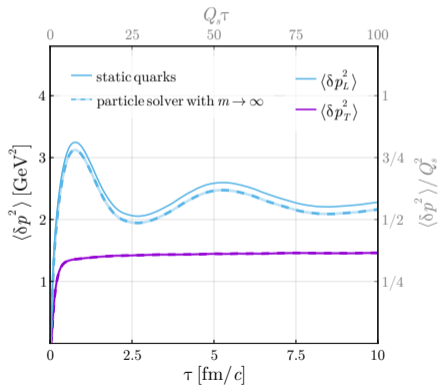


Limiting cases



Static quarks $\langle \delta p^2 \rangle_{m \rightarrow \infty} \propto \langle EE \rangle_{\text{Glasma}}$

Lightlike quarks $\langle \delta p^2 \rangle_{p^x \rightarrow \infty} \propto \langle \tilde{F} \tilde{F} \rangle_{\text{Glasma}}$



$\langle p^2 \rangle$ in limiting cases

Static heavy quark limit $m \rightarrow \infty \Rightarrow$ electric field correlators

$$\langle \delta p_i^2(\tau) \rangle_{m \rightarrow \infty} = g^2 \int_0^\tau d\tau' \int_0^\tau d\tau'' \langle \text{Tr} \{ \mathbf{E}_i(\tau') \mathbf{E}_i(\tau'') \} \rangle$$

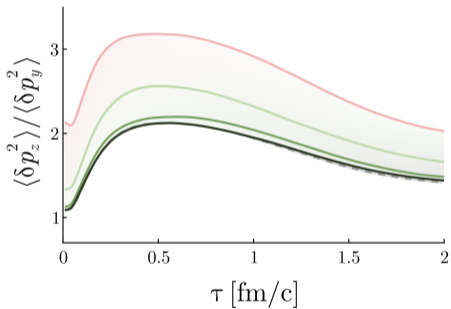
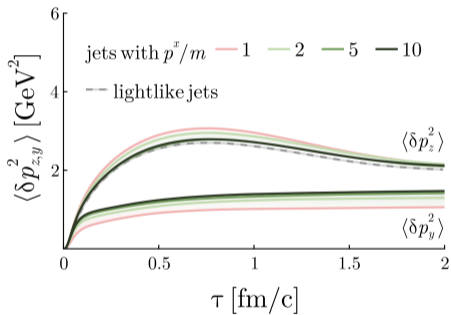
Fast light-like jet quark limit $p^x \rightarrow \infty \Rightarrow$ electromagnetic field correlators

$$\langle \delta p_i^2(\tau) \rangle_{p^x \rightarrow \infty} = g^2 \int_0^\tau d\tau' \int_0^\tau d\tau'' \langle \text{Tr} \{ \tilde{\mathbf{F}}_i(\tau') \tilde{\mathbf{F}}_i(\tau'') \} \rangle$$

Color force components $\mathbf{F}_x \equiv E_x$, $\mathbf{F}_y \equiv E_y - B_z$, $\mathbf{F}_z \equiv E_z + B_y$, parallel transported

$$\tilde{\mathbf{F}}_i(\tau) \equiv \mathcal{U}_x^\dagger(\tau, \tau_0) \mathbf{F}_i(\tau) \mathcal{U}_x(\tau, \tau_0) \text{ with Wilson lines } \mathcal{U}_x(\tau, \tau_0) = \mathcal{P} \exp \left(-ig \int_0^\tau d\tau' A_x(\tau') \right)$$

Jet momentum broadening



Dependence on Q_s

