

*Efficient Description of medium response
to jet energy loss*

Jorge Casalderrey-Solana

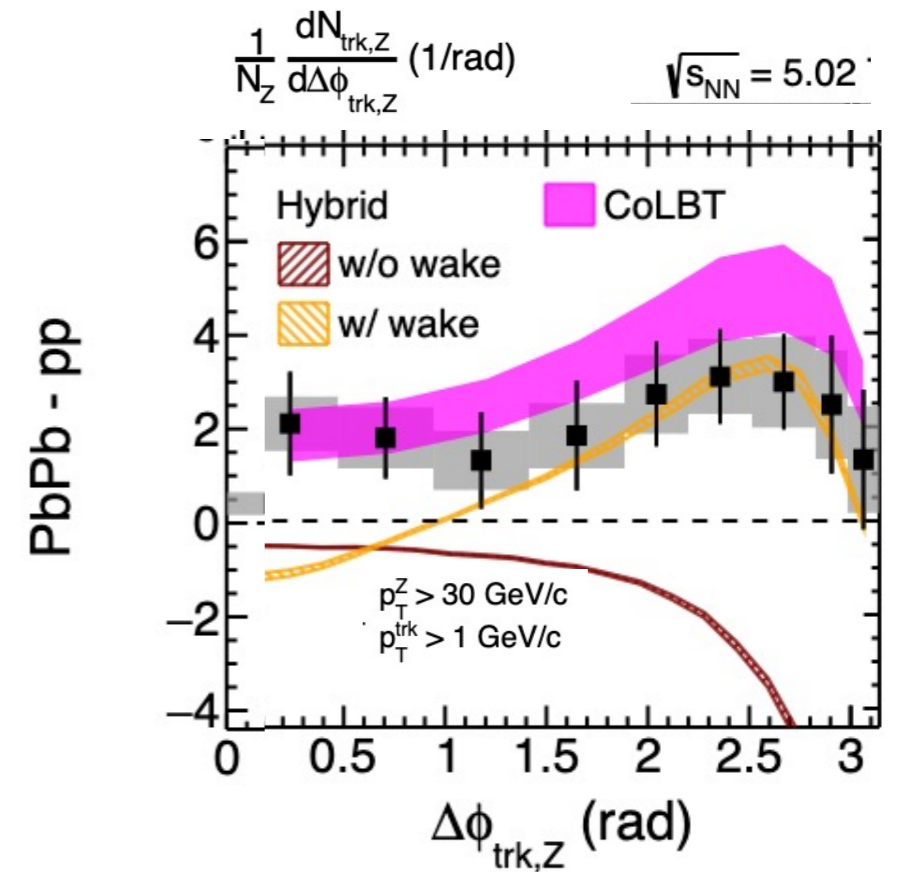
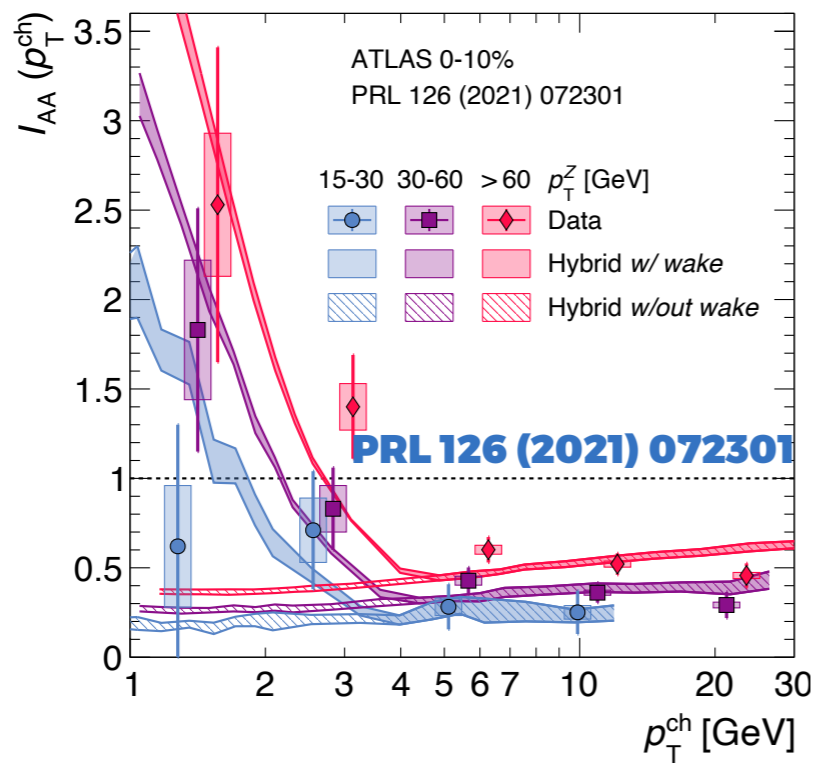
In collaboration with

G. Milhano, D. Pablos, K. Rajagopal and Xiaojun Yao



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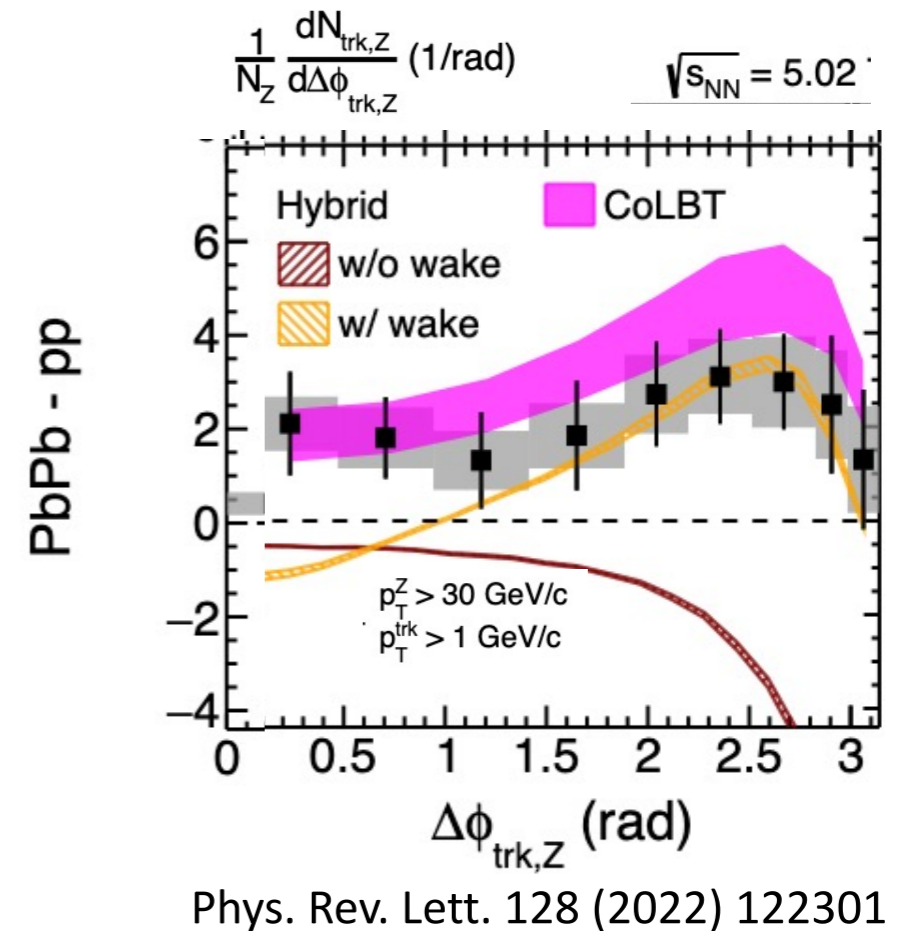
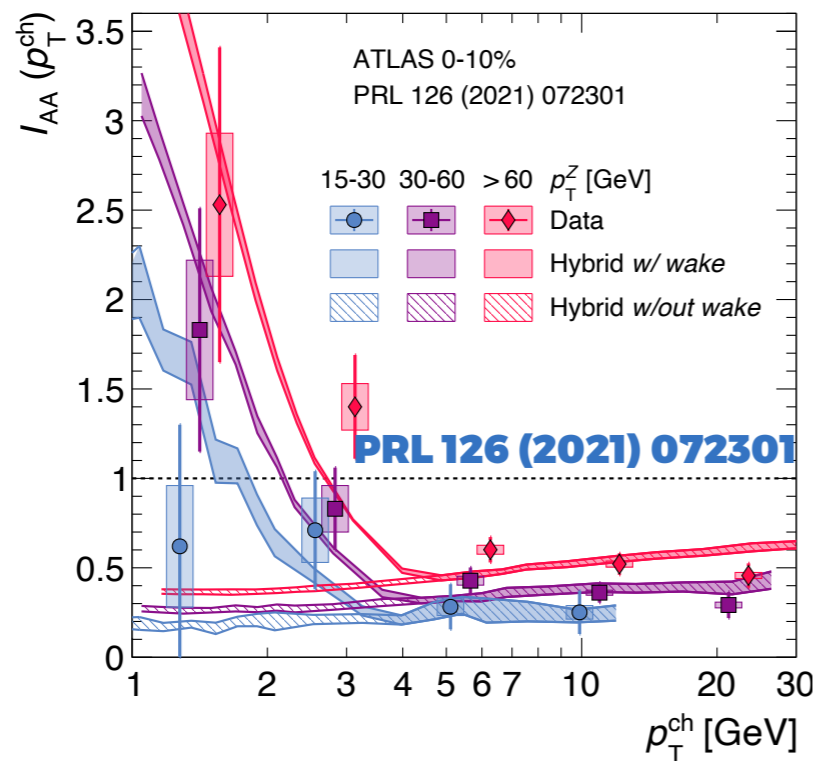
Jet Wakes



Phys. Rev. Lett. 128 (2022) 122301

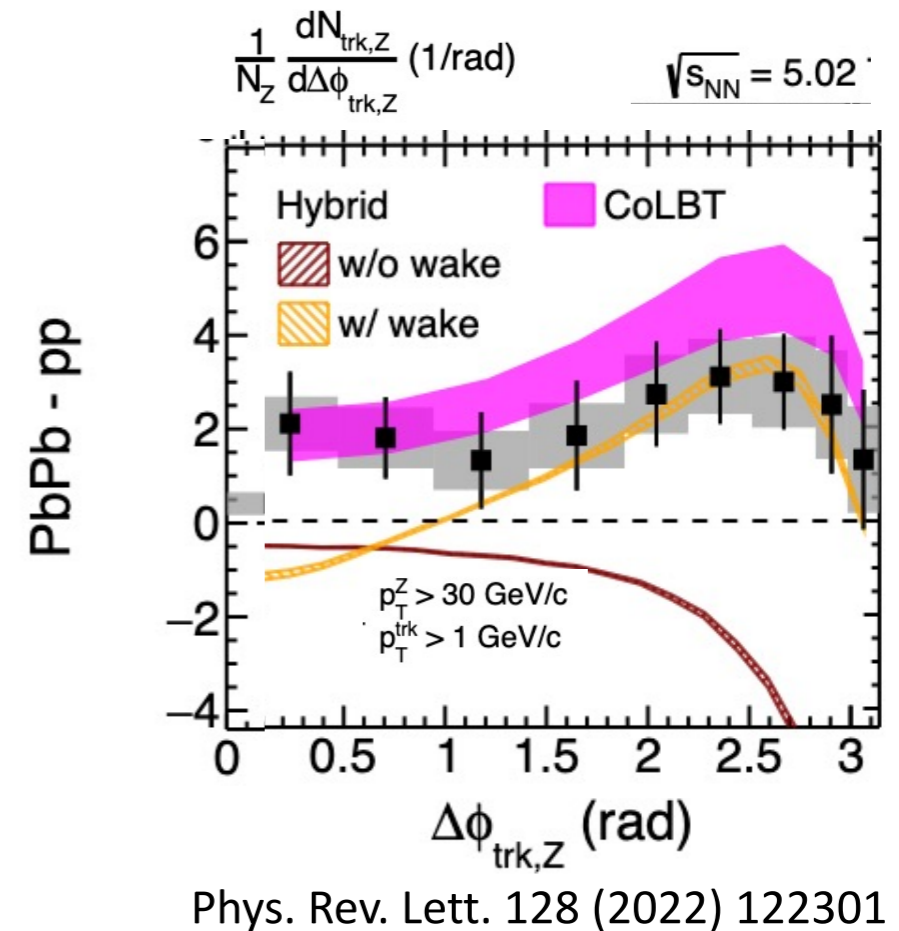
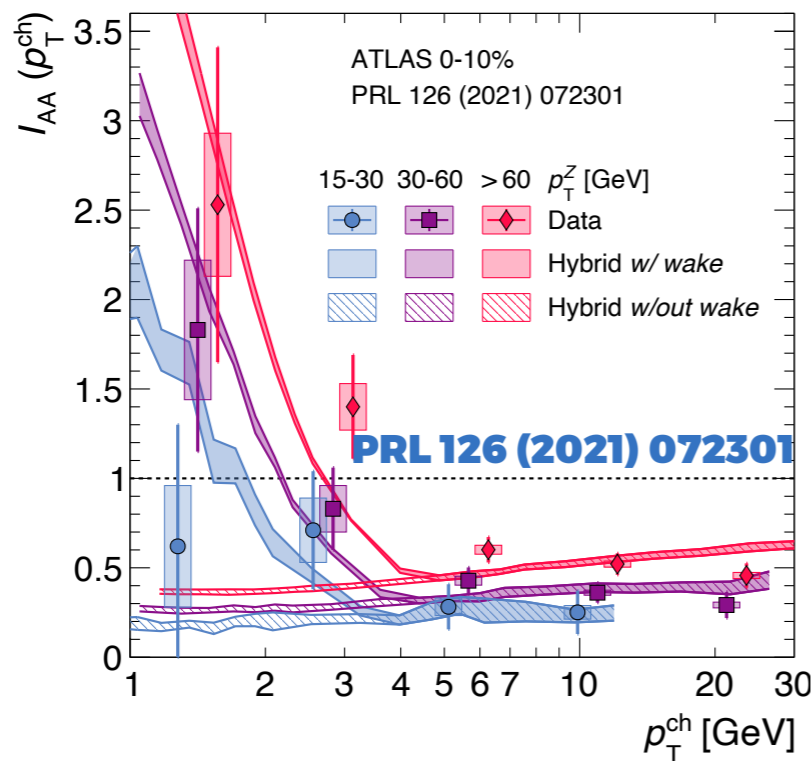
- Soft structure of jets is modified in heavy ion collisions

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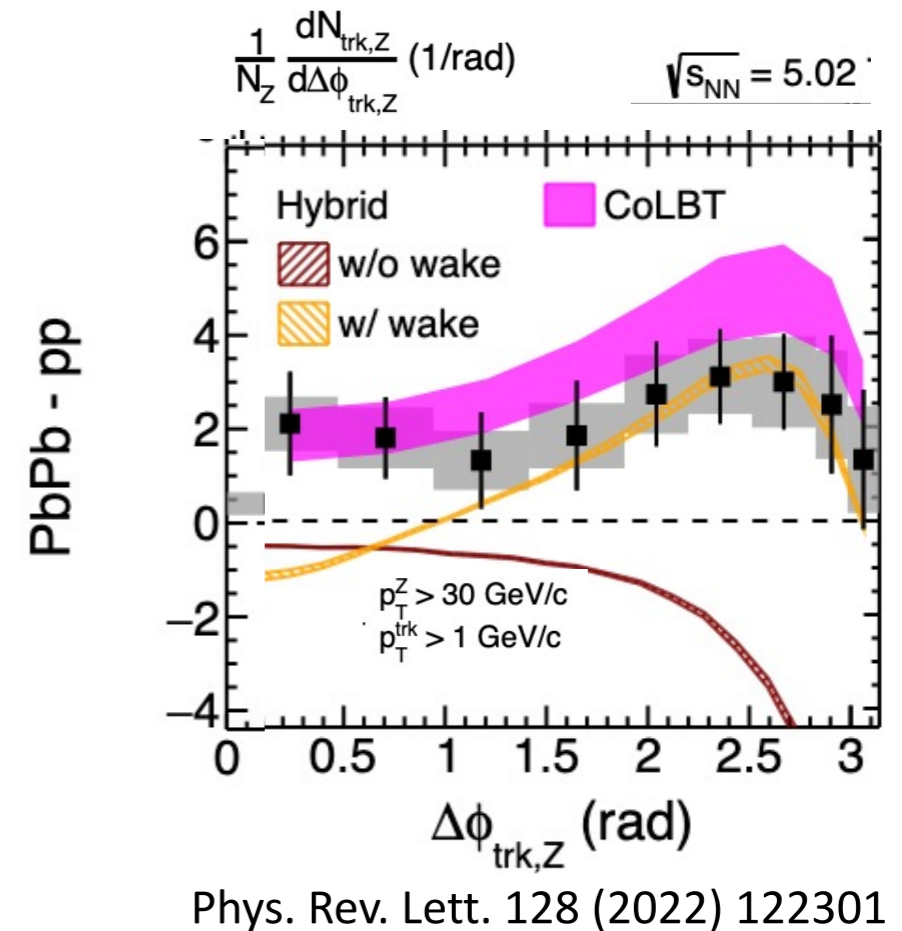
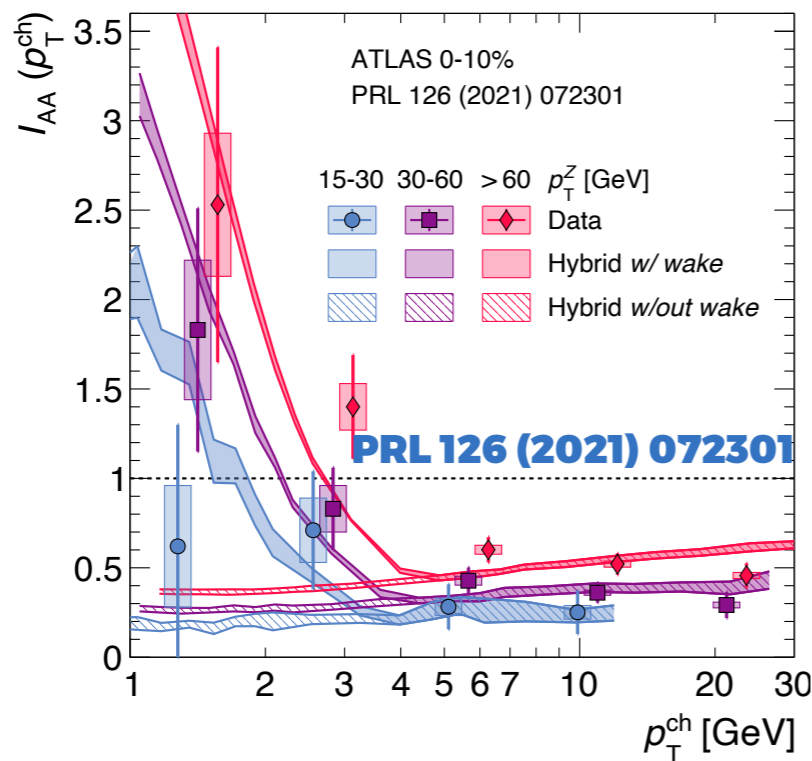
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- Soft structure of jets is modified in heavy ion collisions

- Soft particle production is enhanced
- Soft emission persists to very large angles
- Well understood in terms of hydrodynamic response

Hydro response studied by many groups: Hybrid, CoLBT, Tachibana et al, MUSIC, ...


Hydrodynamic Procedure

- Hydrodynamics with a source

$$\nabla_{\mu} T^{\mu\nu} = J^{\nu}$$

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- Injection of energy by the jet
 - Integrates to the total deposited energy
 - Depends on the thermalization process

Chesler and Yaffe 07; Hong, Teaney and Chesler 12, ...
Mehtar-Tani, Schlichting, Soudi 22;
Brewer, Mazeliauskas, Zhou HP23

- Concrete form still unknown
(here modelled by a Gaussian)

Hydrodynamic Procedure

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$$\nabla_{\mu} T^{\mu\nu} = J^{\nu}$$

- Collective response

- Transports energy away from jet
- Produces sound and diffusion
- Interplay with radial flow

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- Integrates to the total deposited energy
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- Monte Carlo analysis: millions of events
- Full hydro analysis of back-reaction:

Simulating an event is very time consuming

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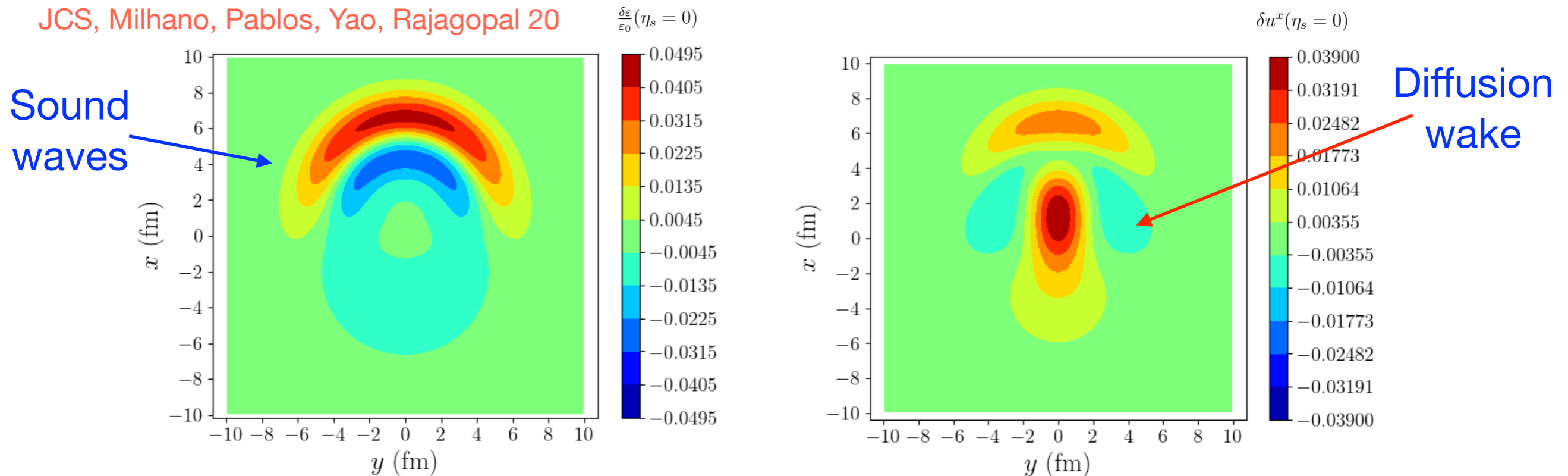
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- Energy injection is small as compared to the fireball \implies linearization
 - COLBT: linearised Boltzman equation
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 - But not everything is linear:
 - Deposition rate
 - Particle production $E \gg T$
- } Non-linear dependence on jet energy

Response without Transverse Flow

- Building block: perturbation on-top of Bjorken flow

JCS, Milhano, Pablos, Yao, Rajagopal 20



- Sound waves \Rightarrow take energy away from jet
- Diffusion wake
 \Rightarrow lost momentum becomes moving fluid along the jet path
- On average:
diffusion wake dominates over sound waves in particle production

JCS, Teaney and Shuryak 05

See for Yang, He, Chen, Ke, Pang and Wang attempts to disentangle Mach and wake in COLBT

Incorporating Transverse Flow

- Linearized solution on top of radial flow is inefficient:
 - Different simulations for each collision configuration

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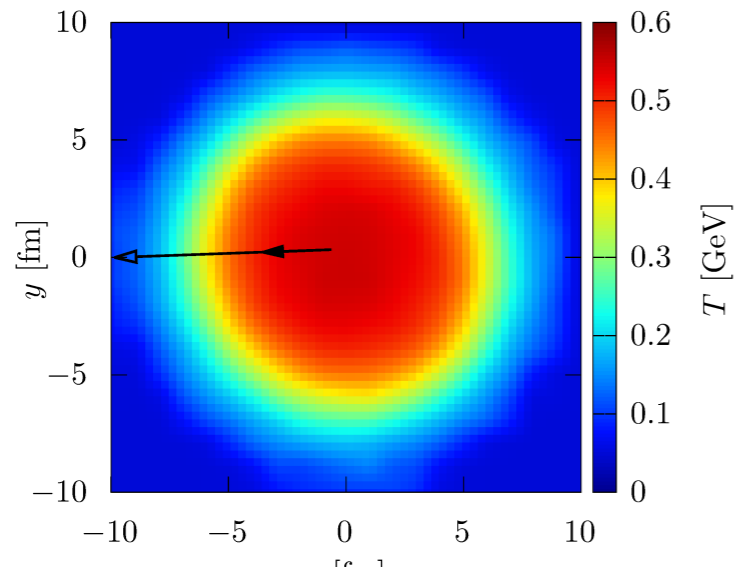
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 - Correct for the direction of the jet after this boost
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- Applicable to any transverse flow
- Fast generation of flow fields induced by jets
 - Library of cases for each deposition point + linear superposition

Calibration Against Full Hydro



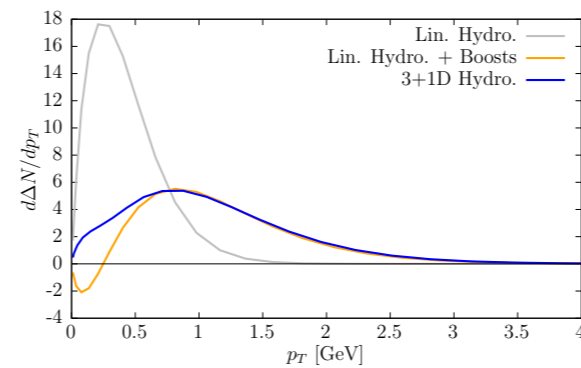
⊙ Excellent agreement with non-linear hydro

⊙ Effects of transverse flow

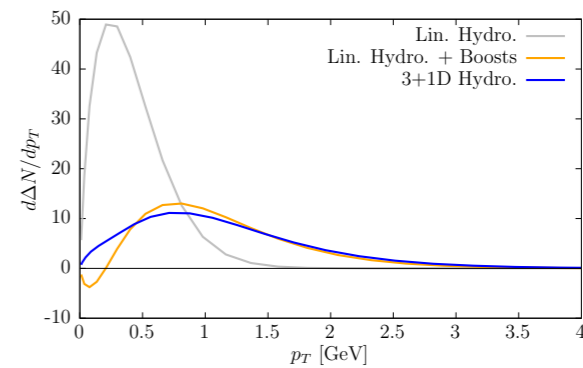
⊙ Harder

⊙ Narrower

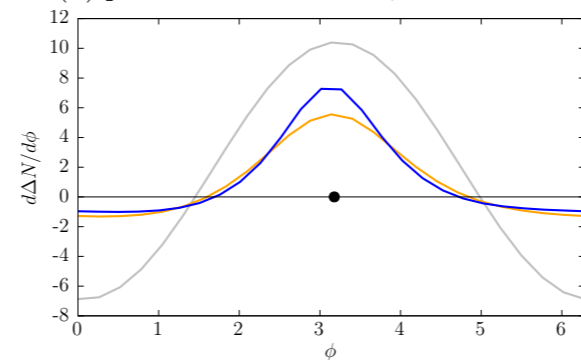
⊙ Less “negative”



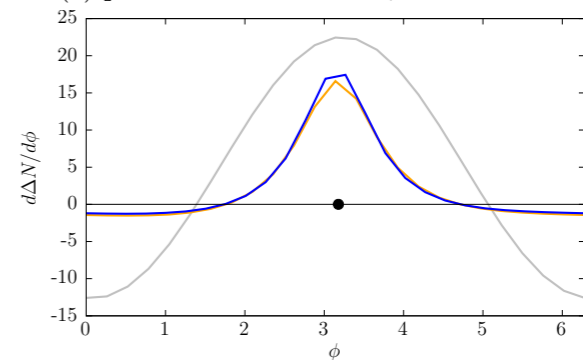
(b) p_T distribution for $E_i = 10$ GeV.



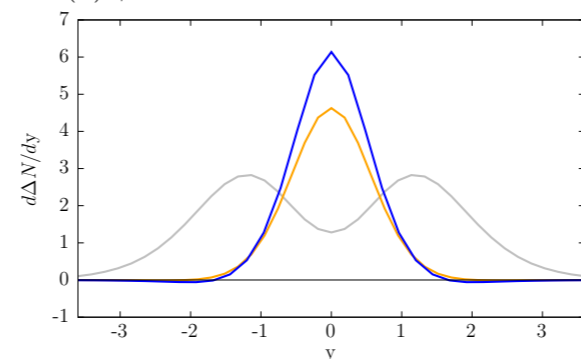
(c) p_T distribution for $E_i = 50$ GeV.



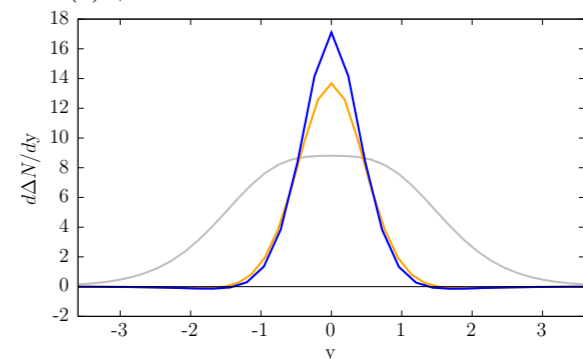
(d) ϕ distribution for $E_i = 10$ GeV.



(e) ϕ distribution for $E_i = 50$ GeV.



(f) y distribution for $E_i = 10$ GeV.

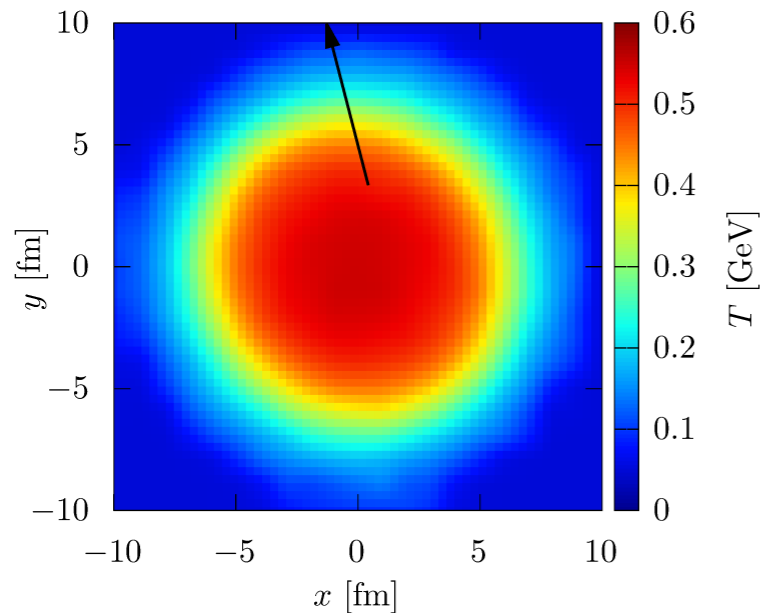


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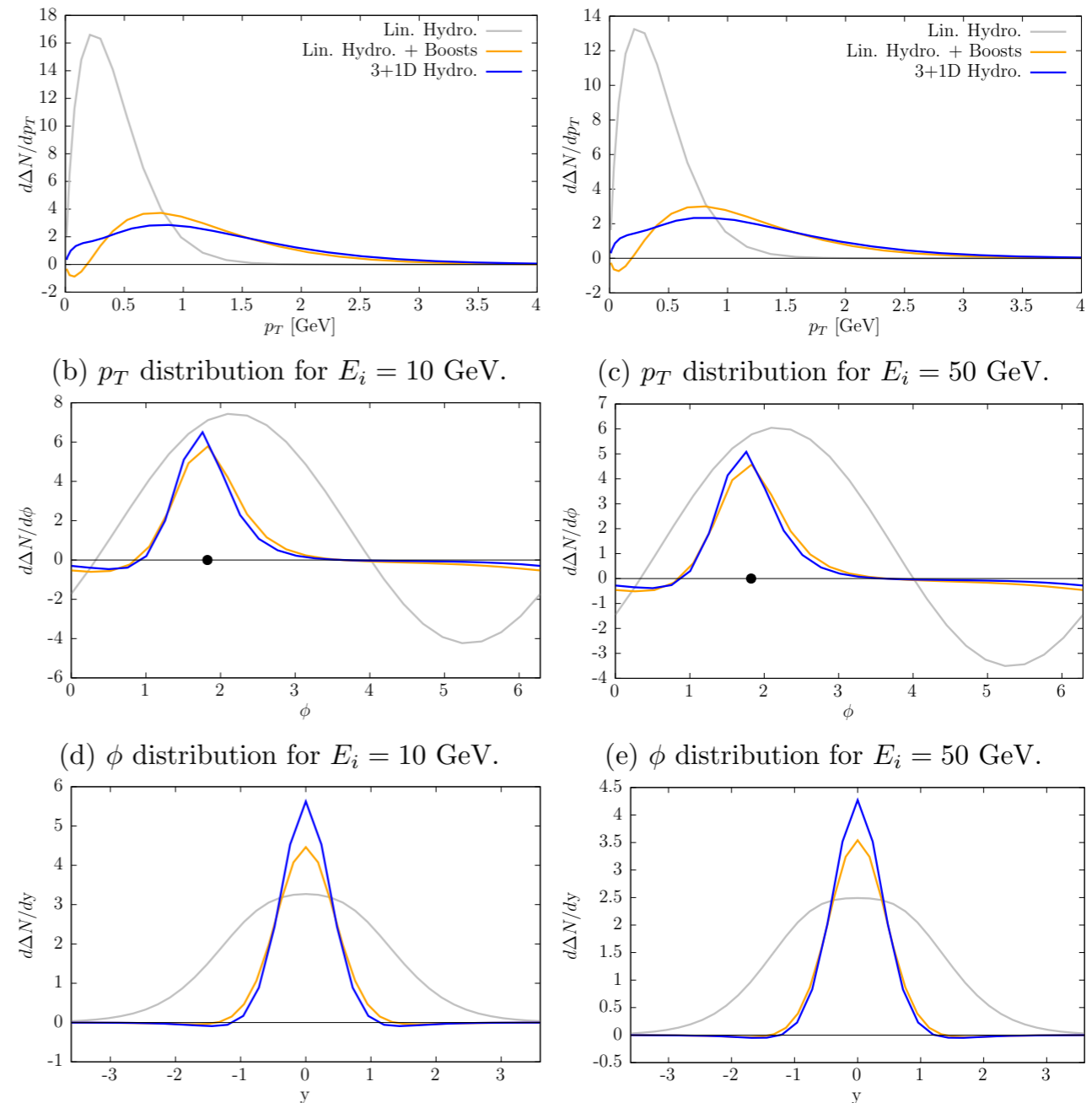
Non-linear hydro response from Music

Other non-linear response: Tachibana et al.; CoLBT

Calibration Against Full Hydro



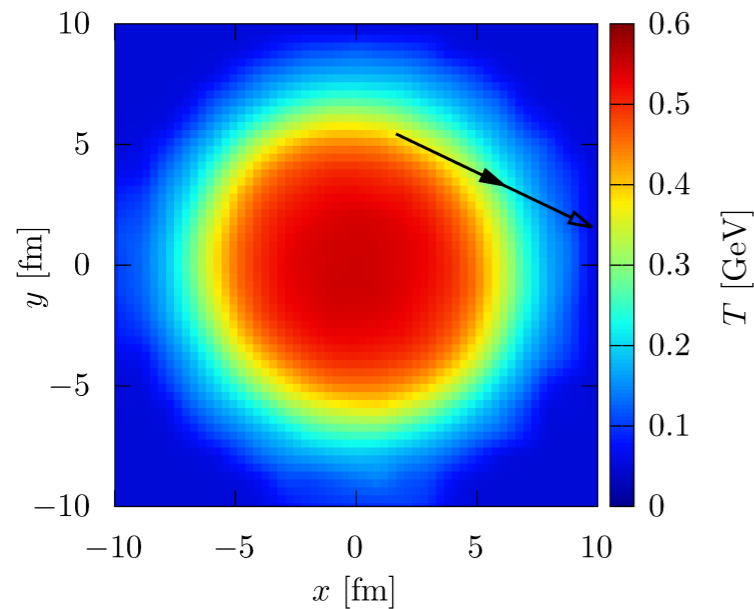
- Very good agreement with non-linear hydro
- Soft particle spectrum changes event by event



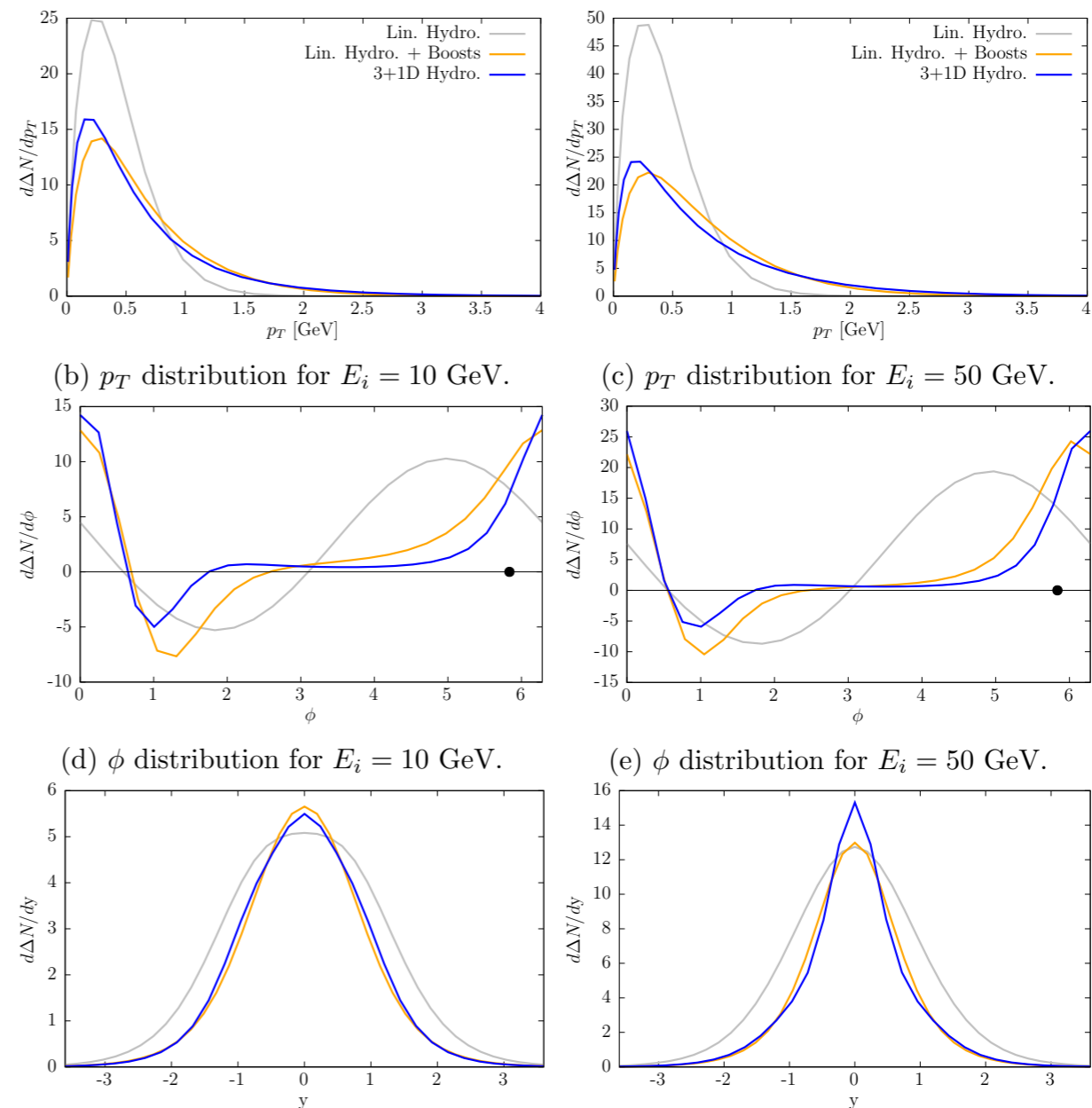
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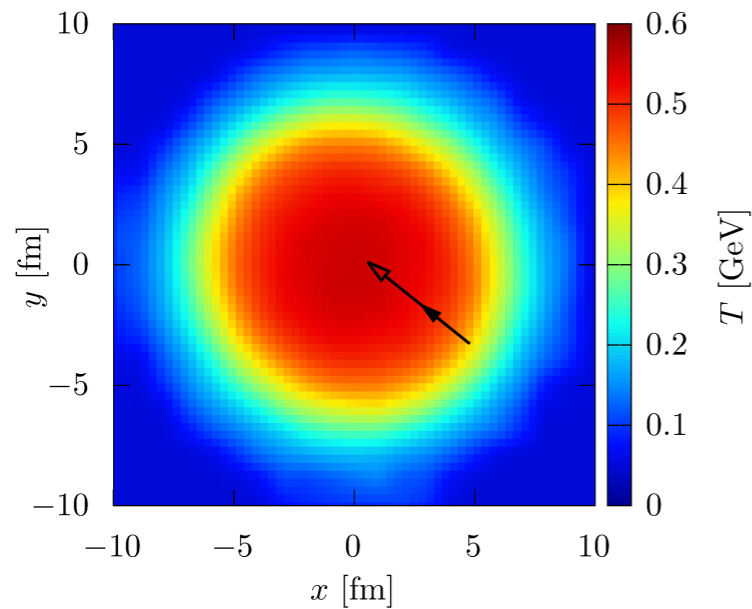
- Good agreement with non-linear hydro
- Soft particle spectrum changes event by event
- Intricate angular patterns depending on point of origin
 - jet direction
 - radial flow encountered



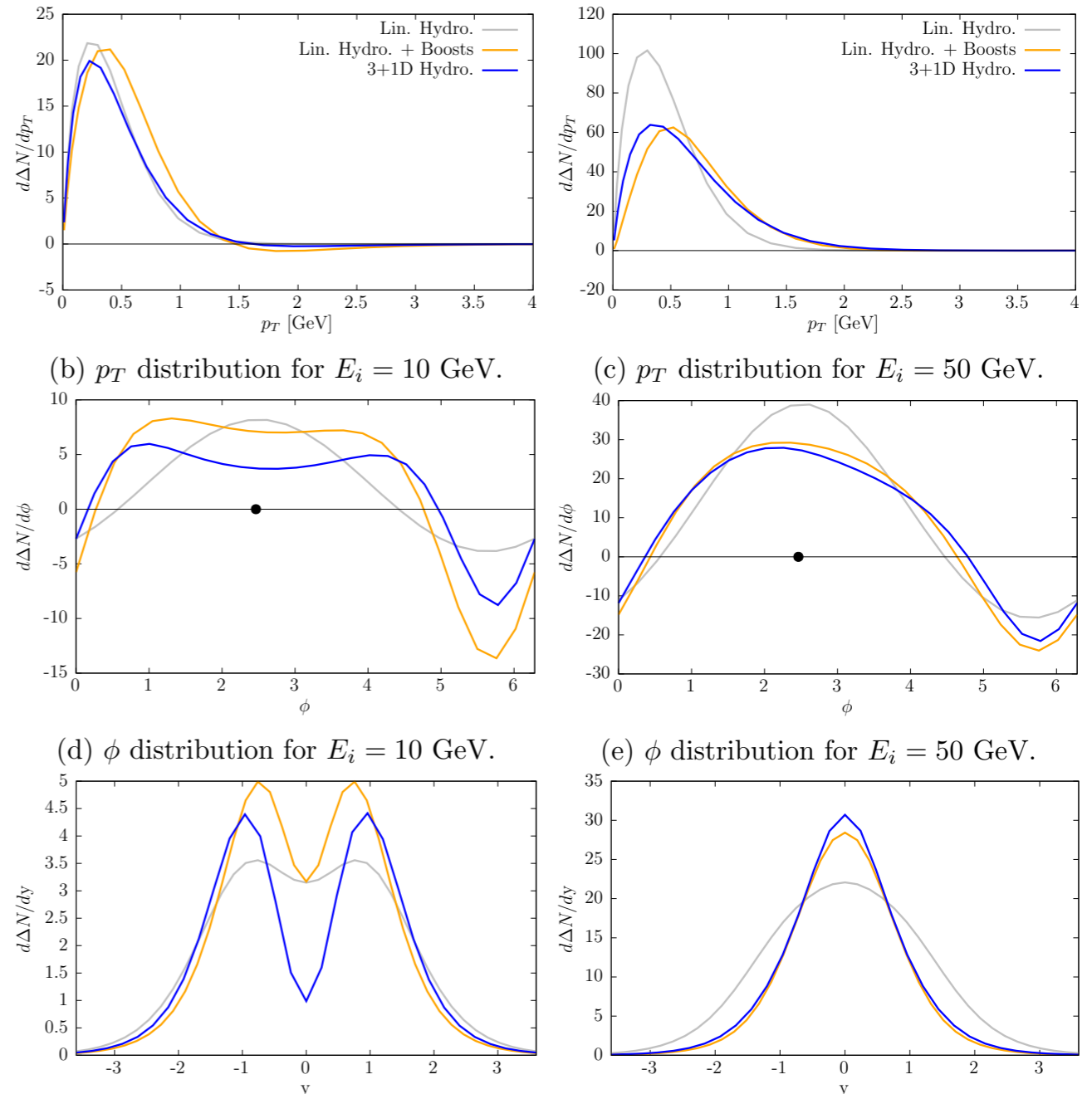
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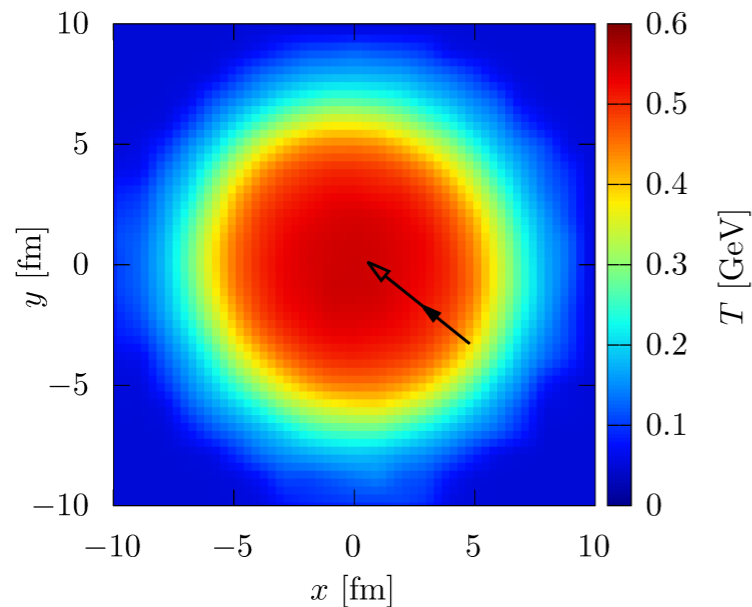


- ⊙ Semi-quantitative agreement with non-linear hydro
- ⊙ Soft particle spectrum changes event by event
- ⊙ Intricate angular patterns

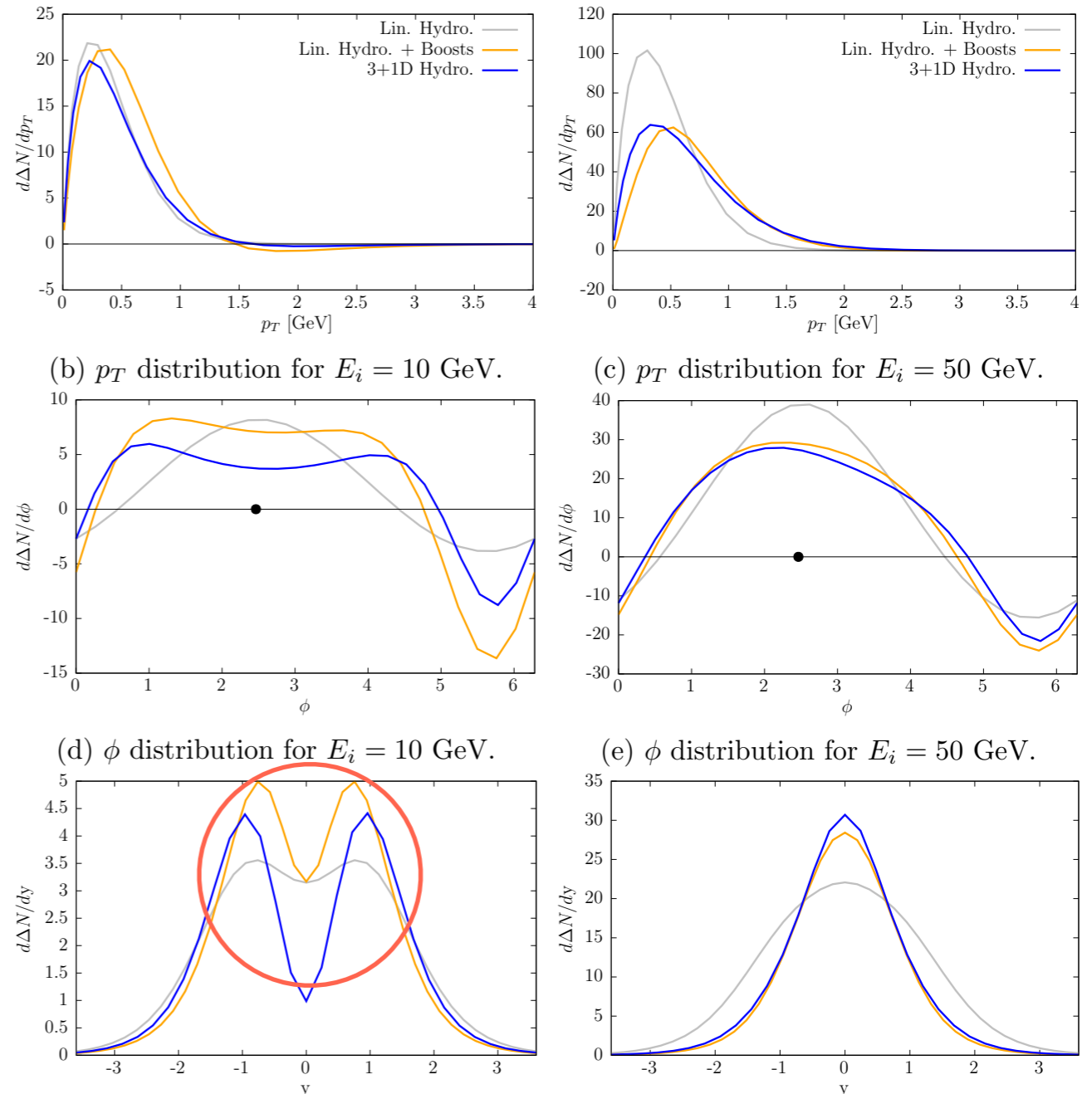


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Calibration Against Full Hydro



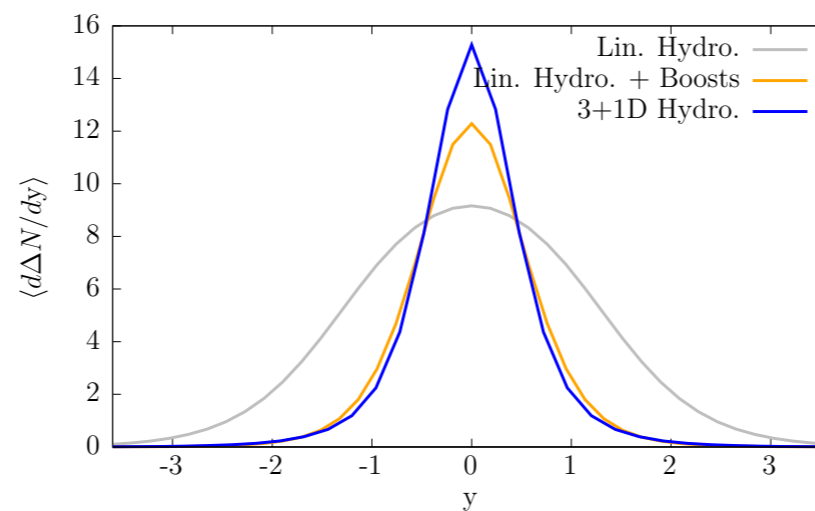
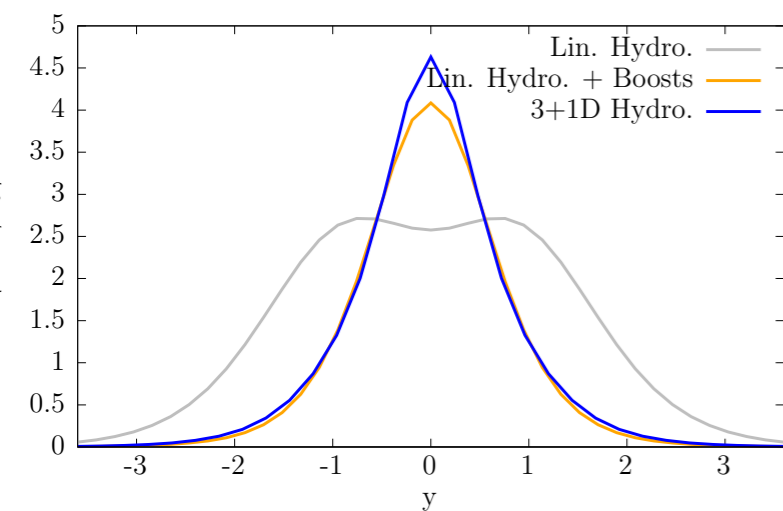
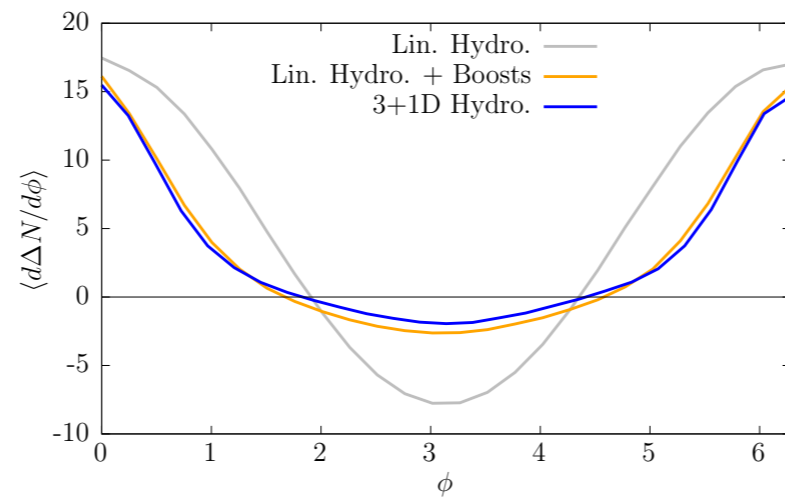
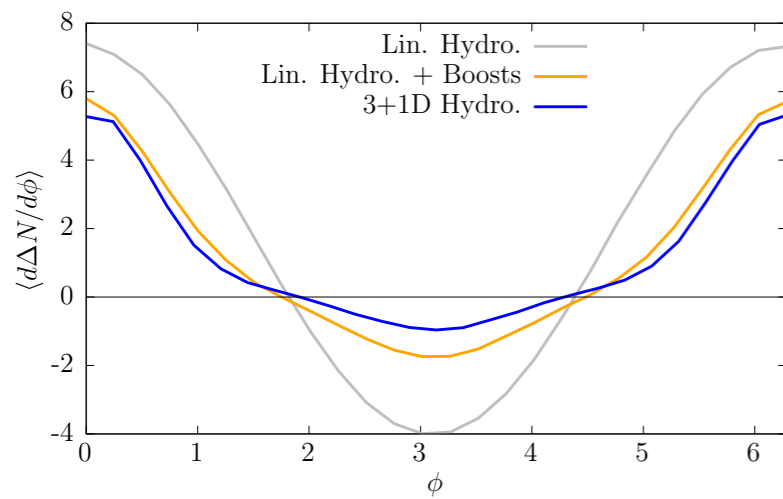
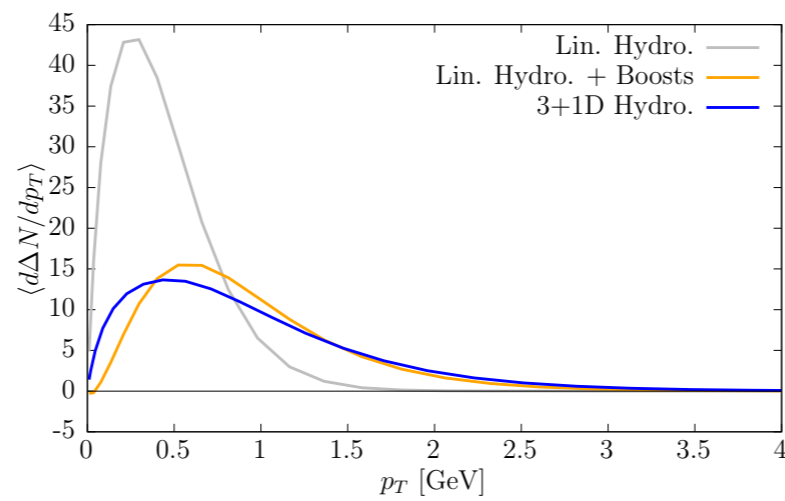
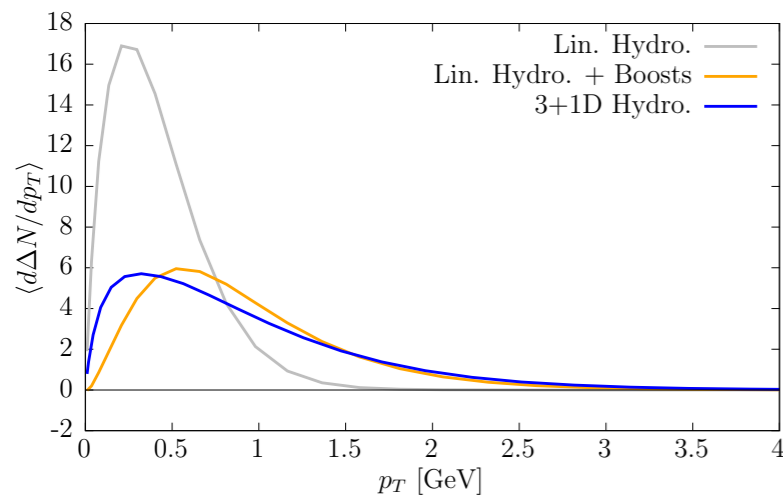
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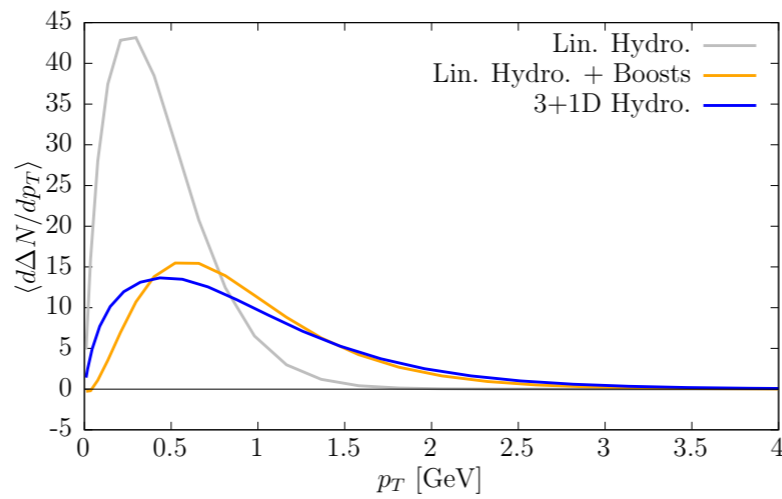
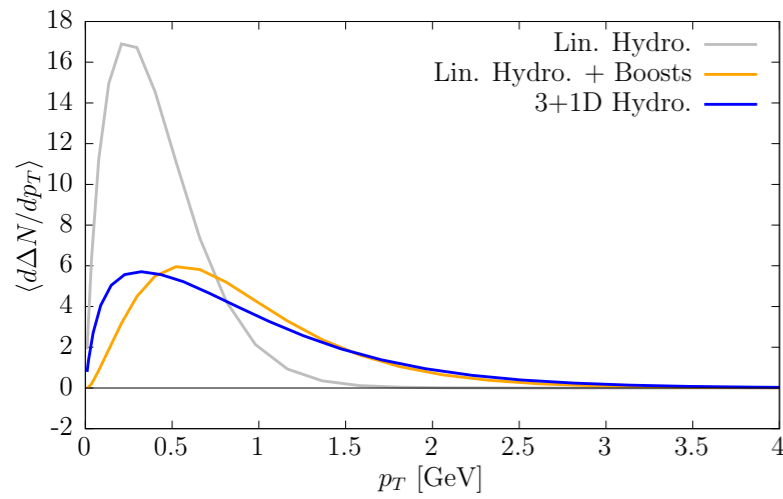
Non-linear hydro response from MUSIC

Manifestation of sound waves in rapidity (for certain configuration)

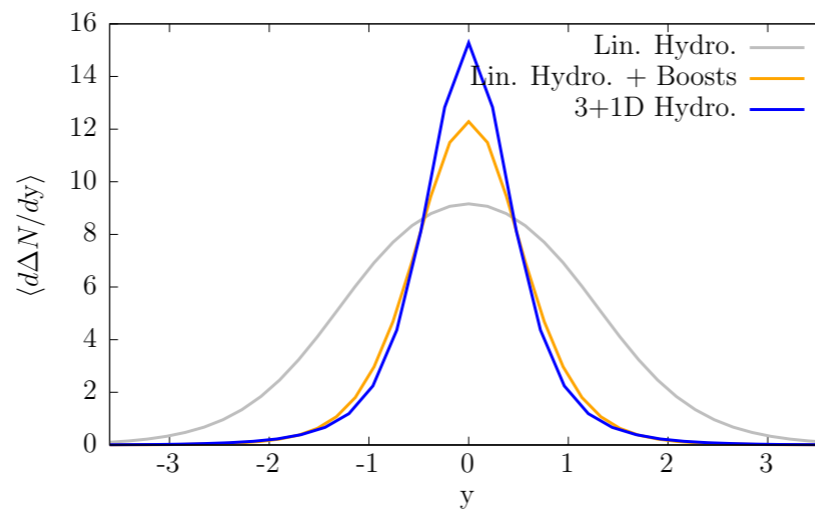
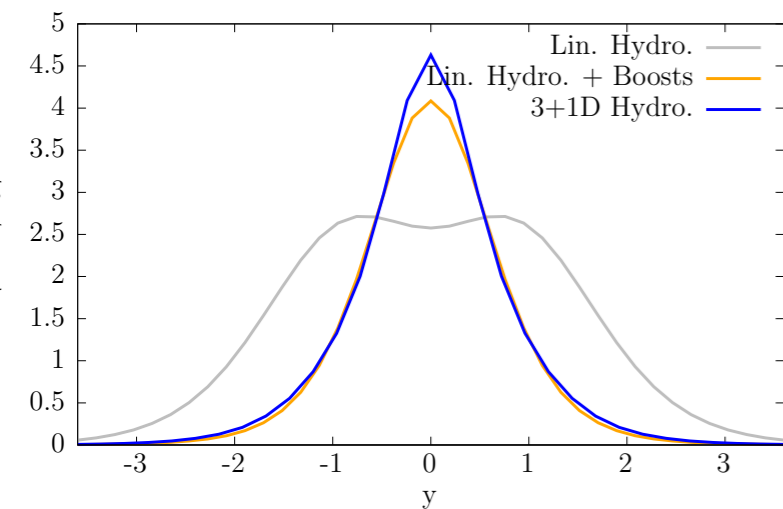
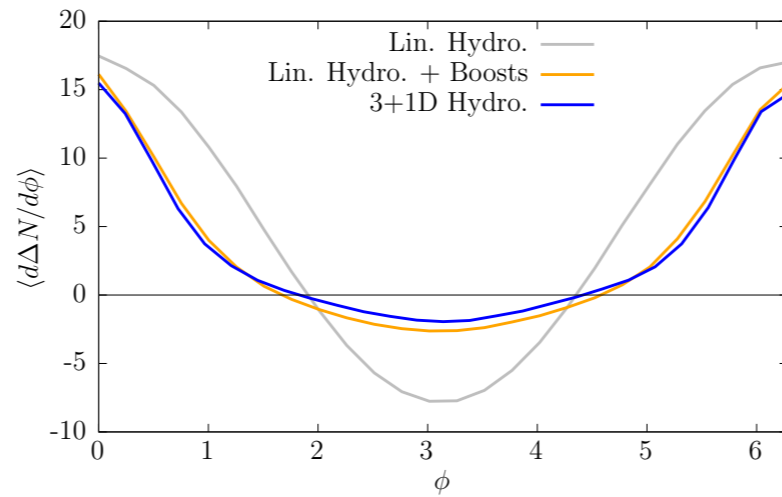
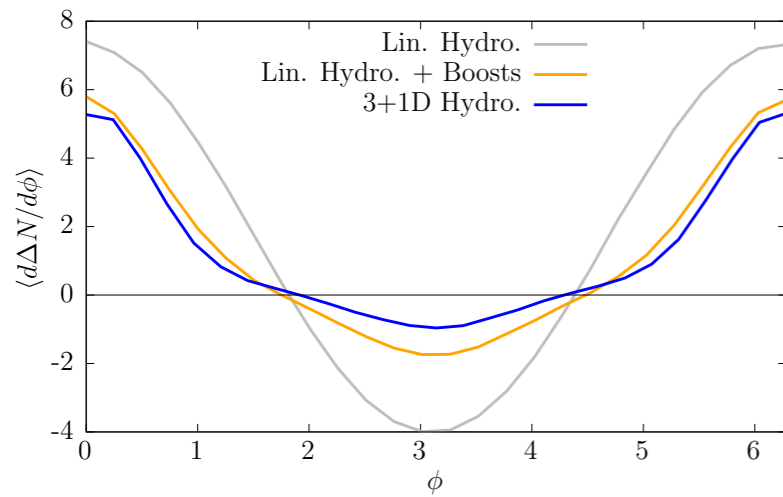
Average over events



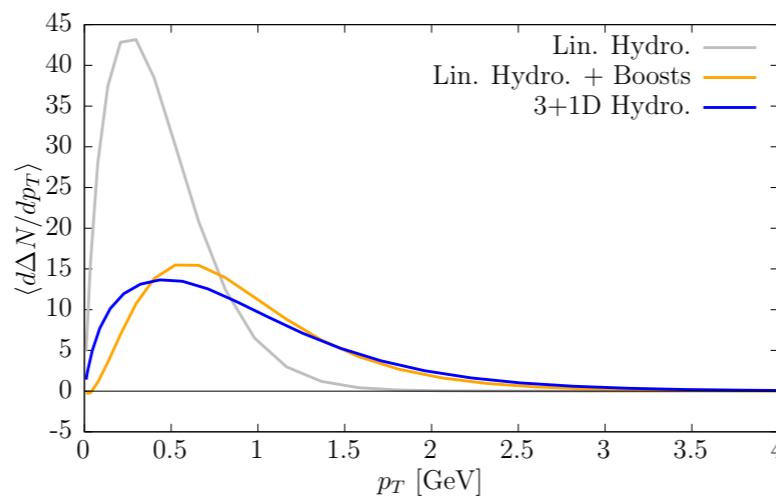
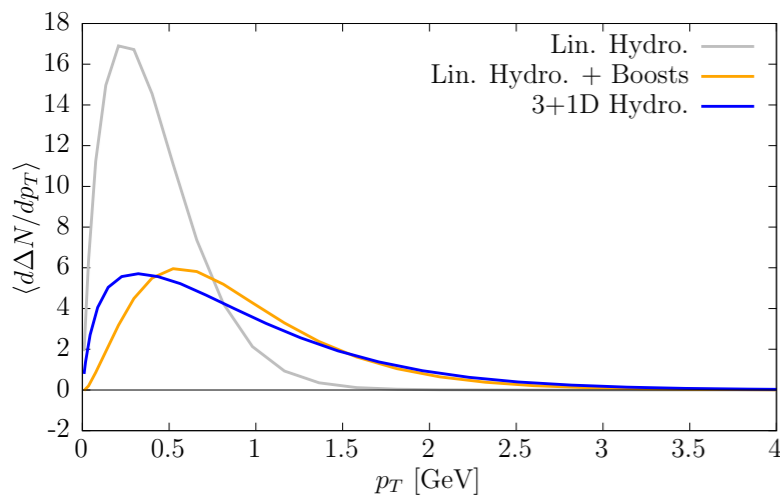
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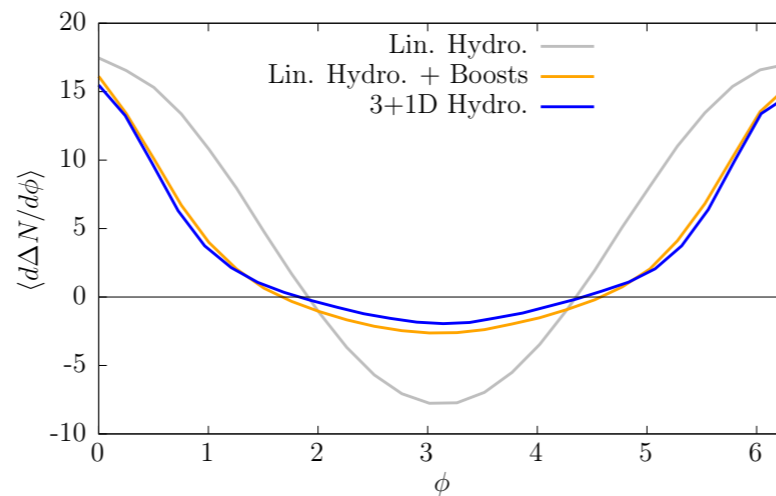
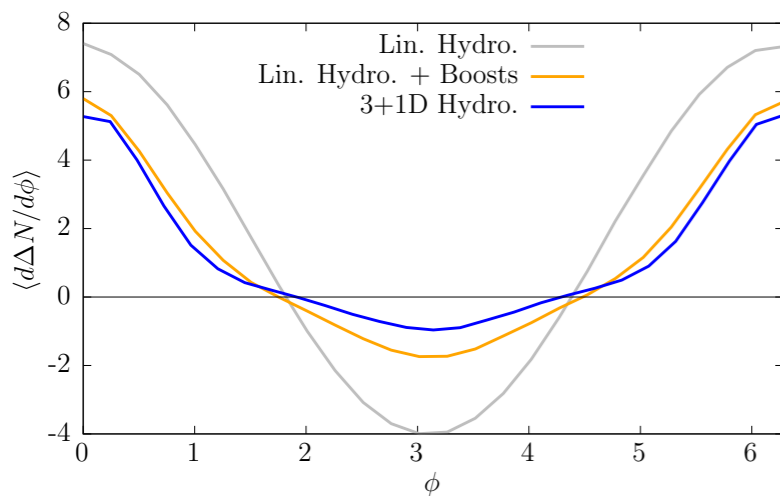
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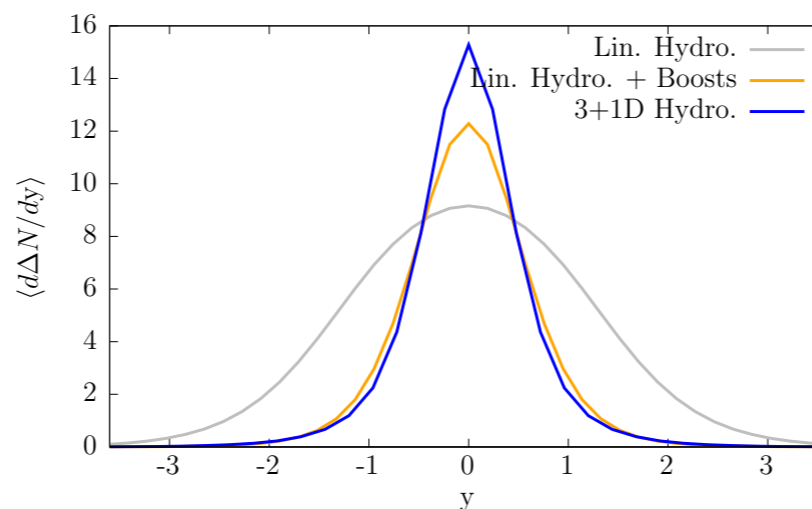
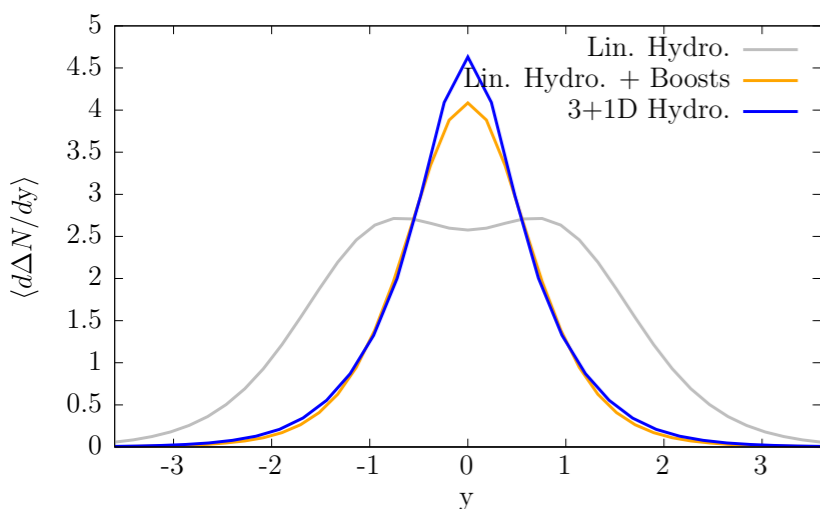
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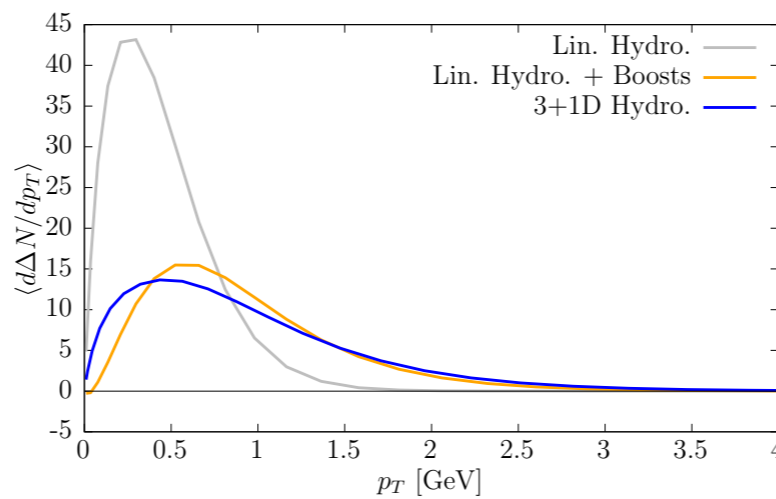
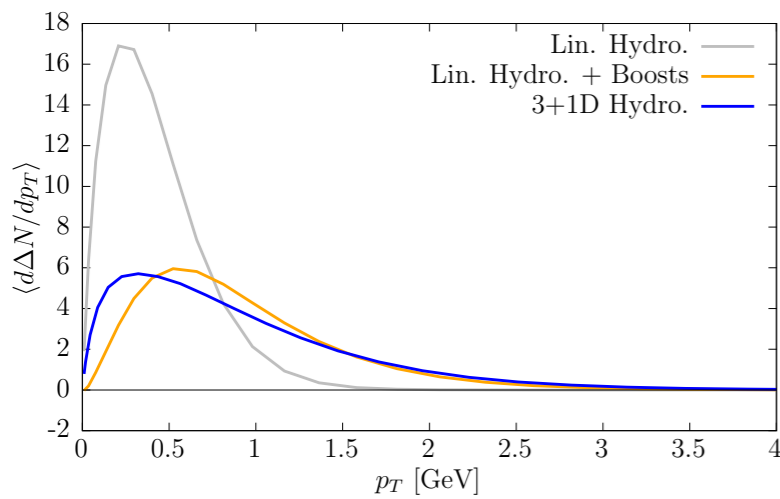
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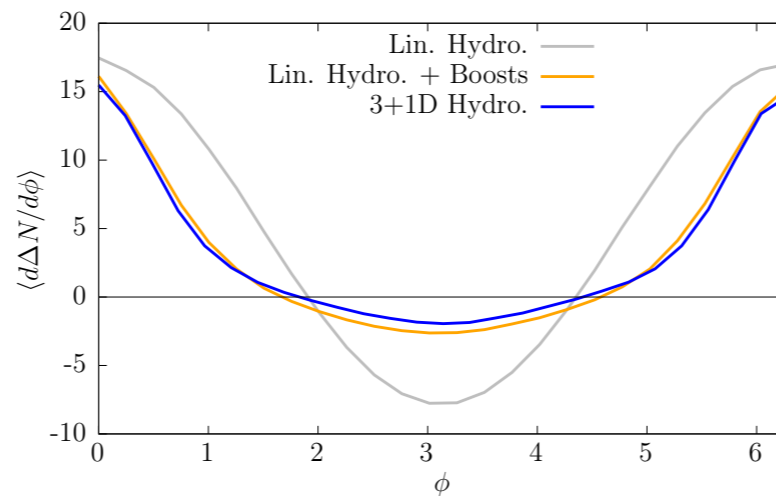
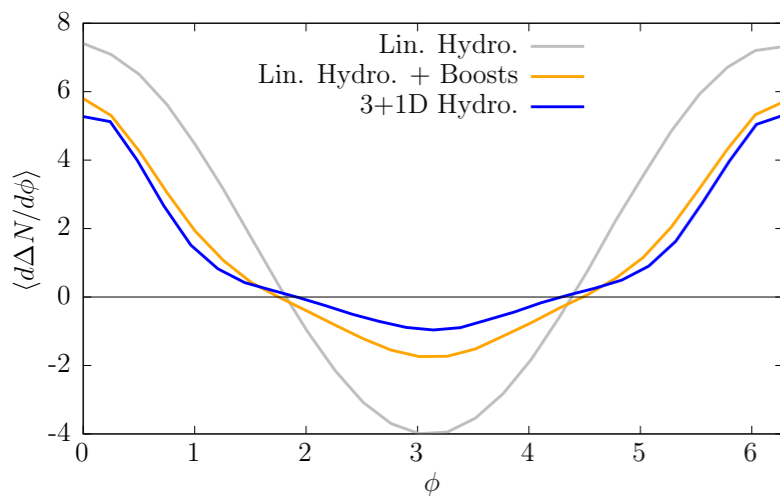
Spectrum becomes
Harder
Narrower
With fewer negatives
than in previous approx.



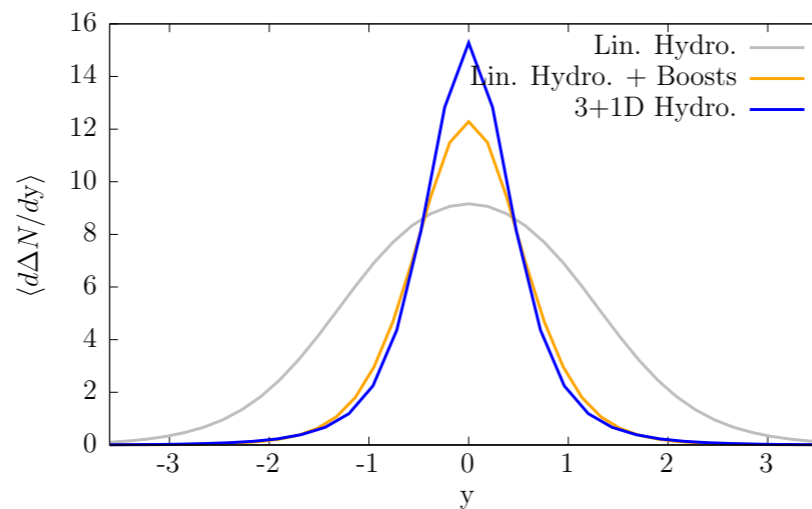
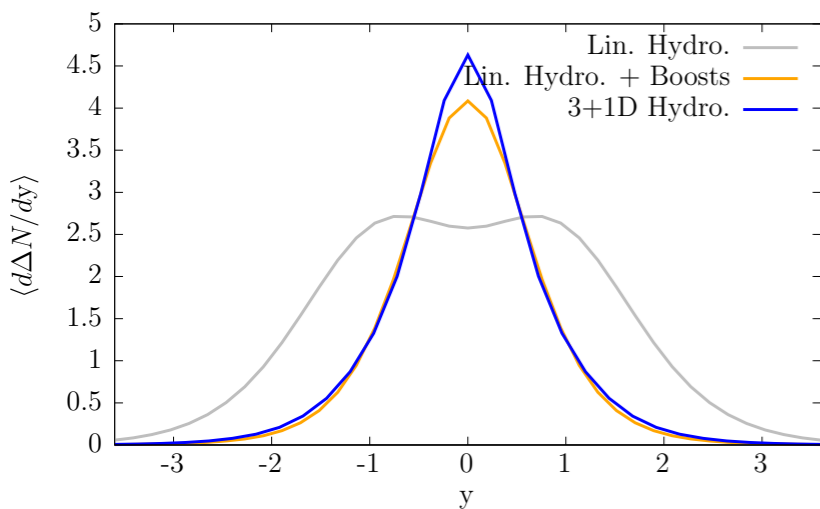
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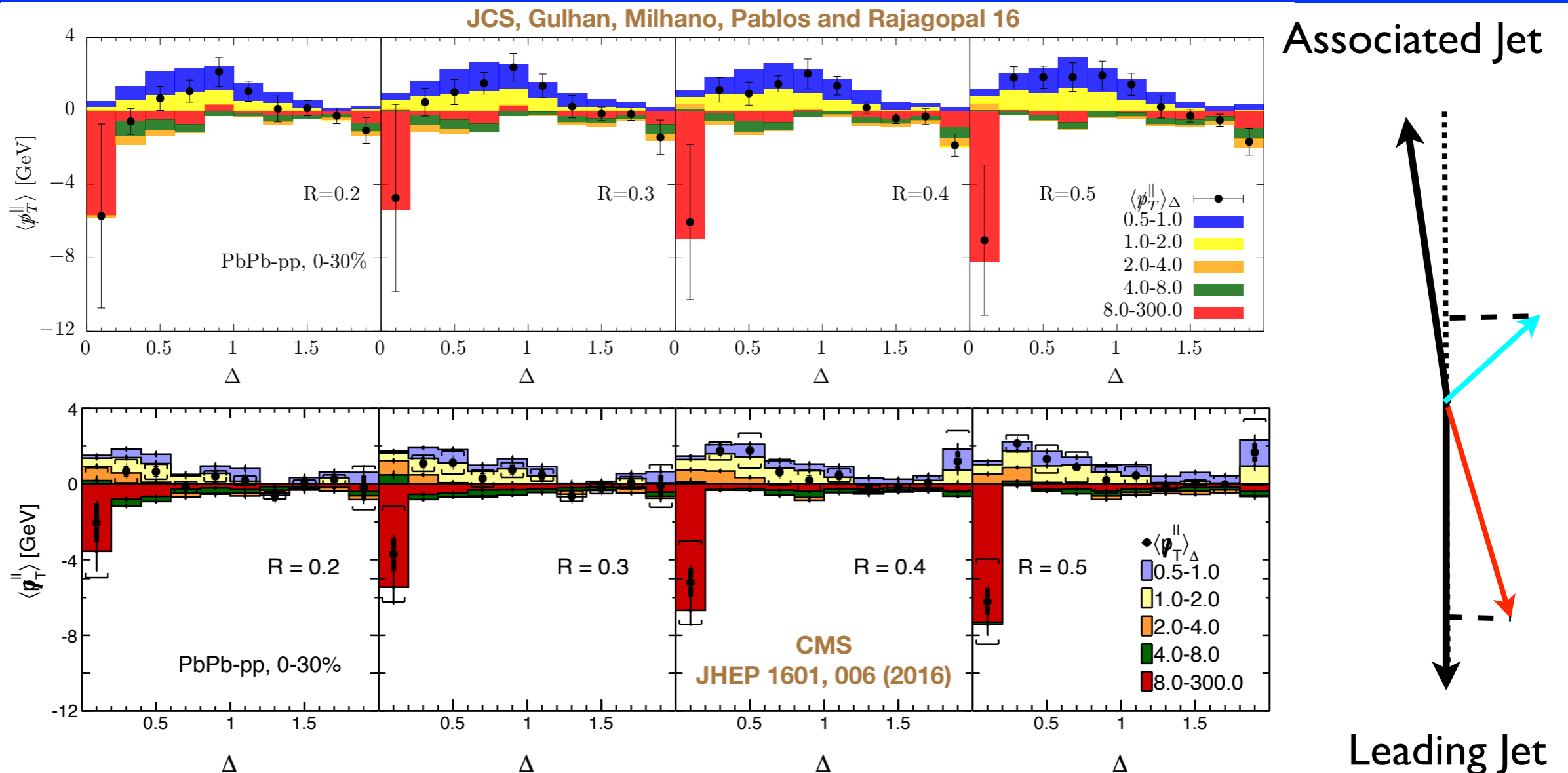
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Conclusions

- ◉ Medium response affects the soft jet structure
 - ◉ They exhibit interesting flow patterns
 - ◉ Depends on collision geometry
 - ◉ Provides complementary tomographic information
 - ◉ May also help to constrain hydrodynamization
- ◉ However, full hydro response is computational expensive
 - ◉ Our procedure captures the main physics of medium response
 - ◉ At least 1000 X faster than non-linear solution
 - ◉ We are now ready for a Monte Carlo implementation

And for a more stringent comparison with RHIC and LHC data

Too simple \Rightarrow Too Soft & Too Wide



- The simple back-reaction implemented in hybrid model:
 - Captures the general features of the energy-degradation
 - Produces too many soft particles at large angles
- In this talk: first steps towards a better description of back-reaction